



CCLRC

Rutherford Appleton Laboratory

# Muon Beam Lines

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ISIS

## The Objectives

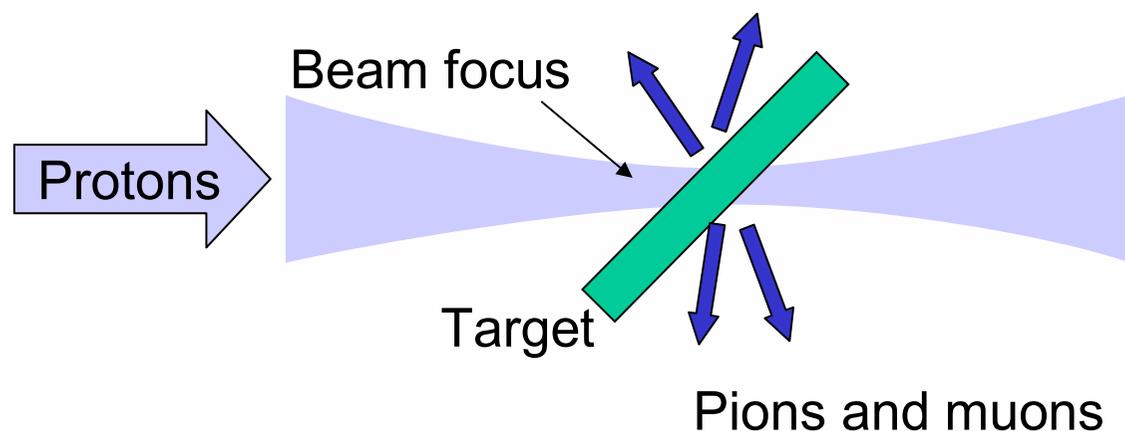
- Deliver muons to a sample
  - Small spot size (match sample size)
  - Well defined energy (penetration depth)
  - Intense beam
  - High polarisation
  - Low contamination with other particles
-

## Muon Production - physics

- High energy protons colliding with nuclei, to form pions
- □ Nuclear reactions such as
  - $p^+ + p^+ \rightarrow p^+ + n + \pi^+$
  - $p^+ + n \rightarrow n + n + \pi^+$
  - $p^+ + p^+ \rightarrow p^+ + p^+ + \pi^0$
  - $p^+ + n \rightarrow p^+ + n + \pi^0$
  - $p^+ + n \rightarrow p^+ + p^+ + \pi^-$
- □ Requires proton energy  $\geq 280$  MeV
- Full production rate for energy 500-1000 MeV  
ISIS 800 MeV, PSI 590 MeV
- Also double pion production  $p^+ + p^+ \rightarrow p + p + \pi^+ + \pi^-$  etc at higher energy
- □ Pions then decay to give muons  $\pi^+ \rightarrow \mu^+ + \nu_\mu$  (lifetime 26ns)  
This decay gives the muon polarisation: 100% polarised opposite to momentum, in the rest frame of the pion

## Muon Production - Targets

- □ Material must have a low atomic number and high melting point
  - High atomic number gives more neutrons by spallation and more scattering of the beam
- □ Usually Graphite, sometimes Beryllium.
- □ Beams are in vacuum. ISIS target heated to  $\approx 600$  °C, cooling by conduction to the edge or radiation.
- Most protons ( $> 95\%$ ) do not produce pions and pass through with little energy loss, so can be used for other purposes (neutrons).

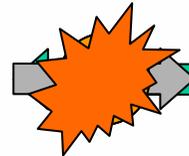


## Muons and Pions

- Some pions escape from the target
  - Capture into beam line, allow to decay in flight
  - Momentum of muon relative to pion determines polarisation
  - both 'forward' and 'backward' decays can be used
  - Select both initial pion momentum and final muon momentum
  - 'Decay' muon beam line
  - High momentum muons to penetrate pressure cells etc.
  - Final polarisation of the muon beam  $\approx 80\%$
- Some pions stop within the target material
  - Decay to muons which escape into the beam line
  - Pions at rest mean muons collected in one direction are all polarised
  - 'Surface' muon beam line - simpler design
  - More intense beam but low momentum muons mean thin windows
  - Fully polarised muon beam

## Pion decays

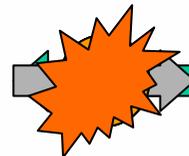
- 'Surface' muons from pions at rest (in the production target)



$$p_{\mu} = 27 \text{ MeV}/c$$

$$E_{\mu} = 4 \text{ MeV}$$

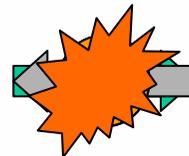
- 'Forward' muons from pions in flight



$$p_{\mu} > p_{\pi}$$

High energy

- 'Backward' muons from pions in flight

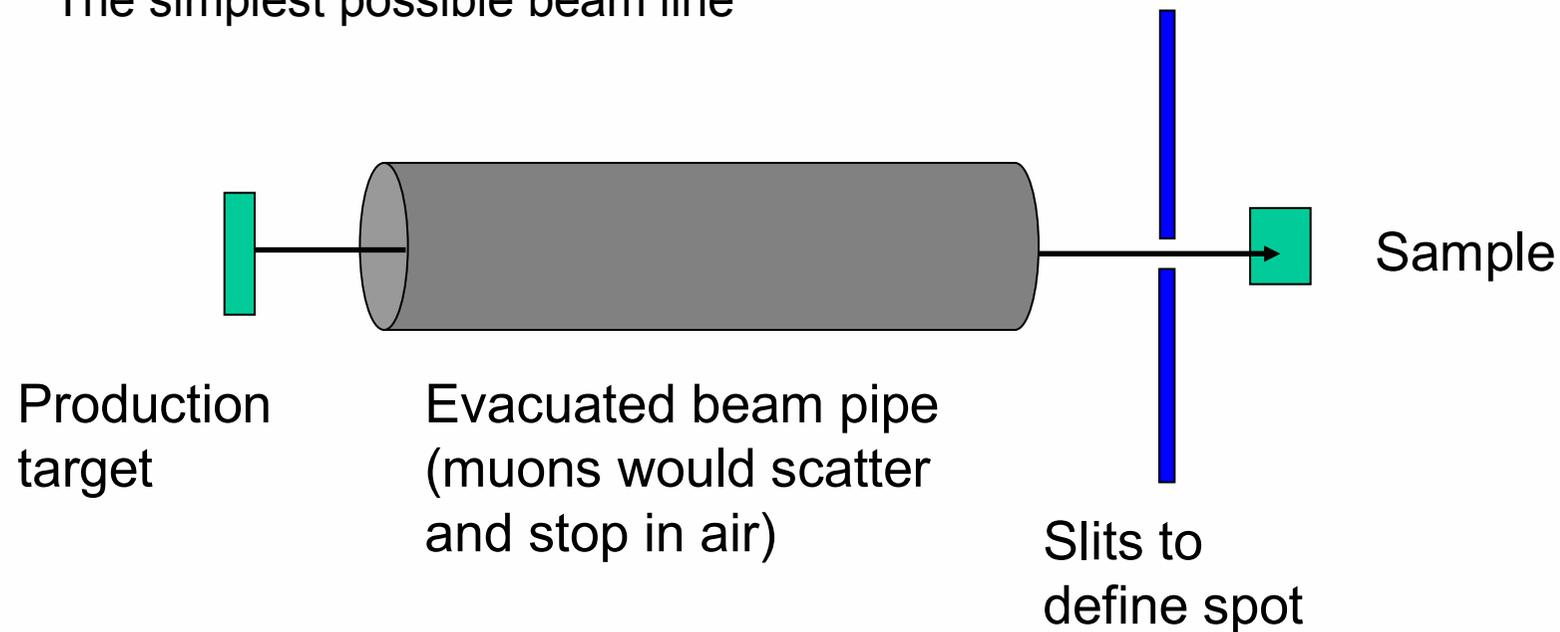


$$p_{\mu} < p_{\pi}$$

High energy

## Beam Line design 1

- The simplest possible beam line



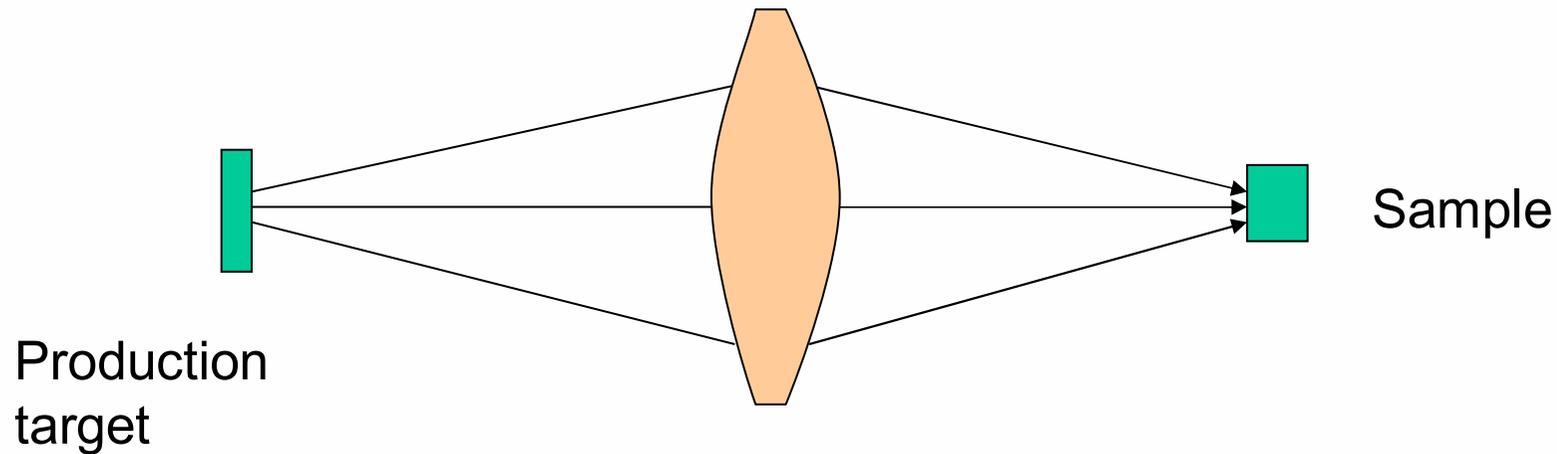
- Main problem - Low muon flux
- Additional problems - other particles transmitted, high radiation level at sample

## Muon Shutters

- □ Need to be able to stop the beam at the sample position to change the sample
  - Do not want to switch off the whole accelerator
  - Some radiation from target even with proton beam off
- □ Shutter required which will stop all particles coming down the beam line.
- □ Beam with direct view of the target □ 1m thick steel block (as in neutron instruments) to stop neutrons, gamma rays, etc.
  - Large motor and gearbox to raise/lower. Slow.
- □ Clean muon beam with momentum  $27\text{ MeV}/c$  □ 5cm thick lead plate
  - Simple compressed air cylinder □ Fast operation.
- □ Interlock system
  - prevents shutter being opened unless the sample area is cleared and locked.
  - closes shutter if any problem eg. 'Beam Off' button
- In addition the interlocks may control some of the beam line magnets.

## Beam line design 2

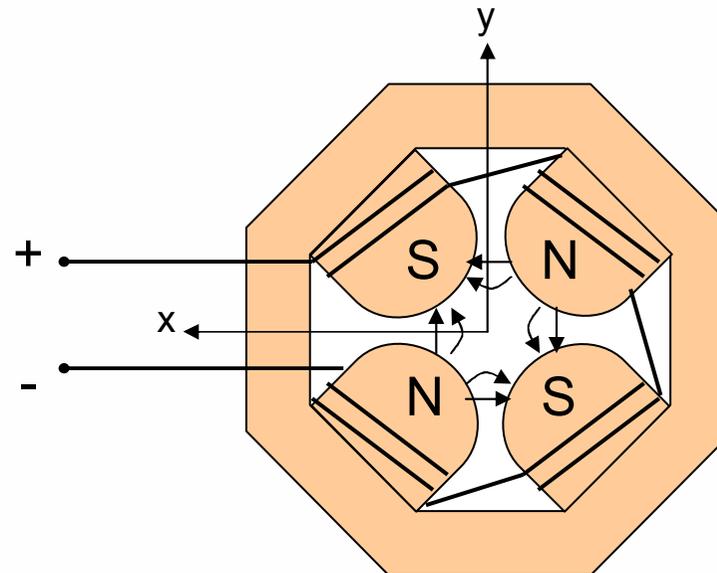
- Use a lens to focus the muons and give larger flux



- Usually use more than one lens
  - First lens close to source to capture large solid angle
  - Sample close to last lens to give smaller beam spot
- Still transmits many other particles if these are poorly focused if the wrong momentum
- Straight-through path for neutrons

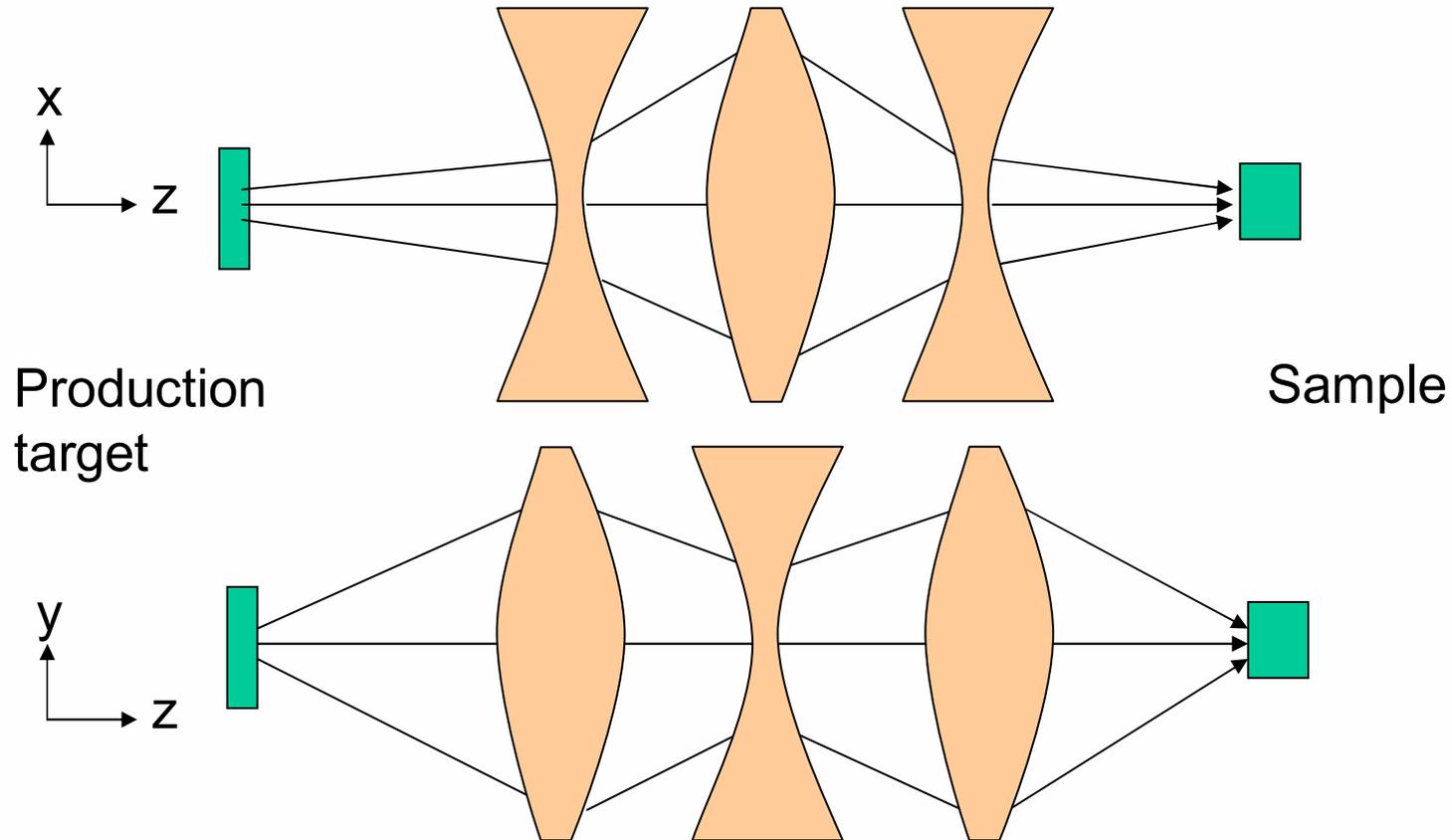
## Practical muon lenses

- Muons deflected in transverse magnetic (or electric) fields
  - Deflection  $\theta \approx d B q / p$  or  $\theta \approx d E q / p v$
- Uniform field bends the beam through the same angle at any position off axis
- Field Gradients give deflection varying with position  $\hat{=}$  focusing possible
- Quadrupole magnet
  - Beam in  $+z$  direction (into screen)
  - Along axis,  $B=0$  and no deflection
  - Displaced in  $+x$  direction
    - $B$  along  $+y$  and  $E$  in  $-x$  direction
    - Focusing (convex lens)
  - Displaced in  $+y$  direction
    - $B$  along  $-x$  and  $E$  in  $+y$  direction
    - Defocusing (concave lens)
- Can't focus both axes simultaneously!



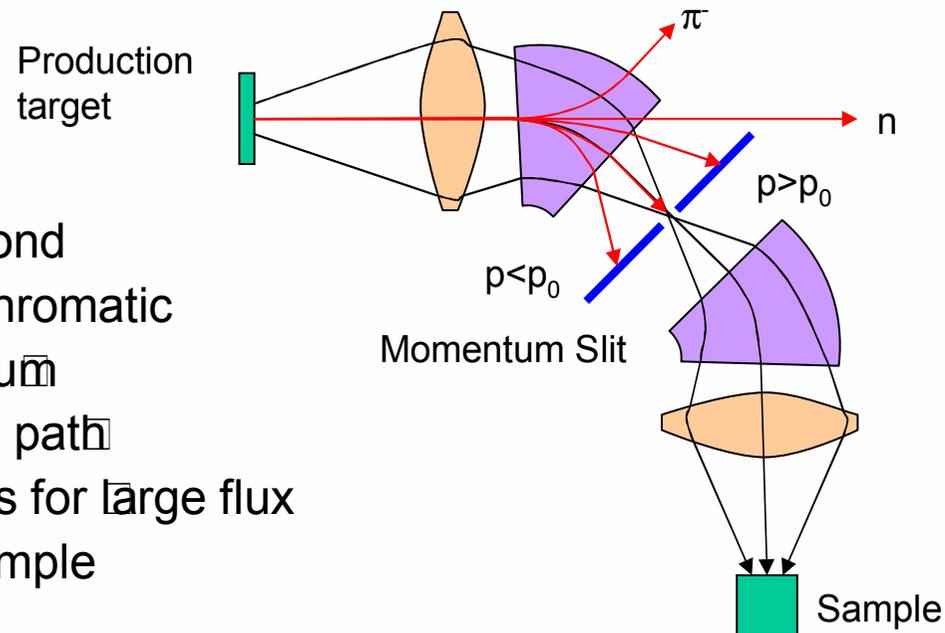
## Practical muon lenses

- For focusing on both axes we use a Doublet or Triplet
- □ Doublet gives different magnification in  $x$  and  $y$
- □ Triplet can preserve image shape



## Beam line design 3

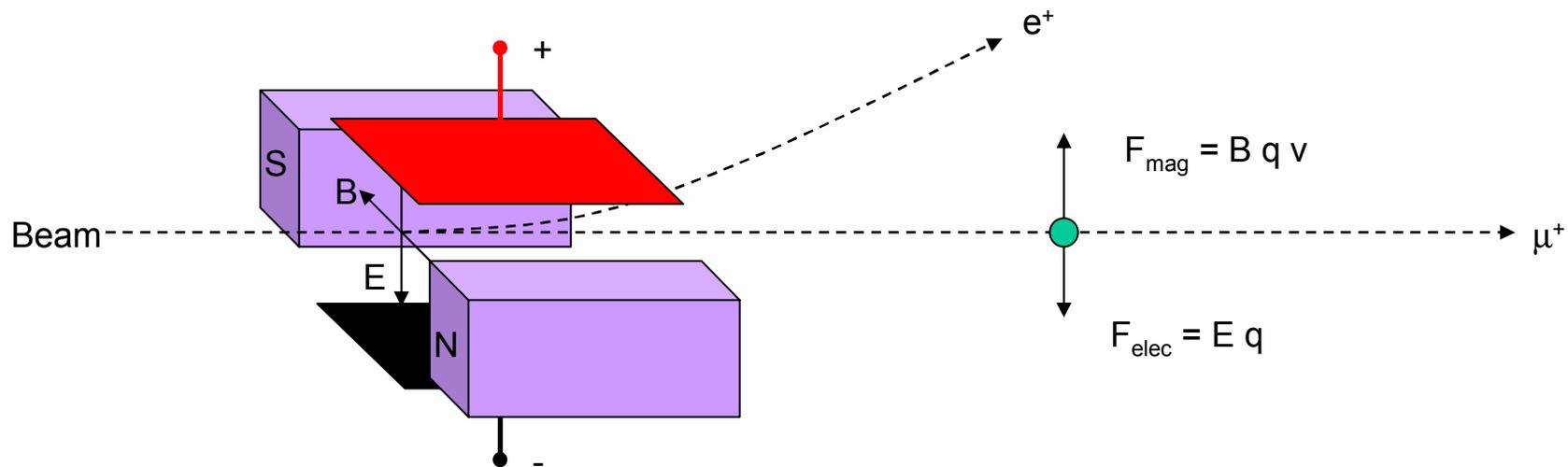
- Include a Bend (uniform field, dipole magnet)
- Excludes uncharged particles ( $n$ ,  $\gamma$ ) and those with wrong charge ( $\pi^+$ ,  $e^+$ )
- Separates particles with different momentum  
 use Slits at a suitable point to define the momentum range passed



- More quadrupoles and a second bend can make the beam Achromatic
  - particles of any momentum are returned to the same path
  - can open momentum slits for large flux but same spot size at sample
- Problem □ still passes positrons if they have the same momentum

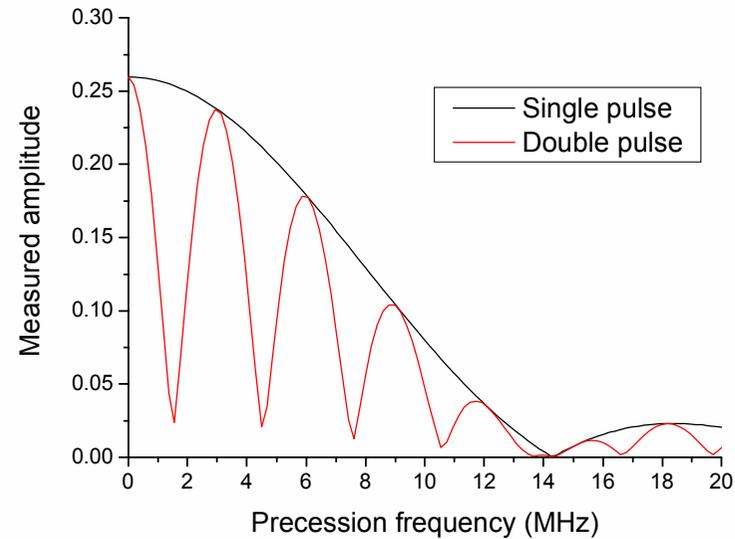
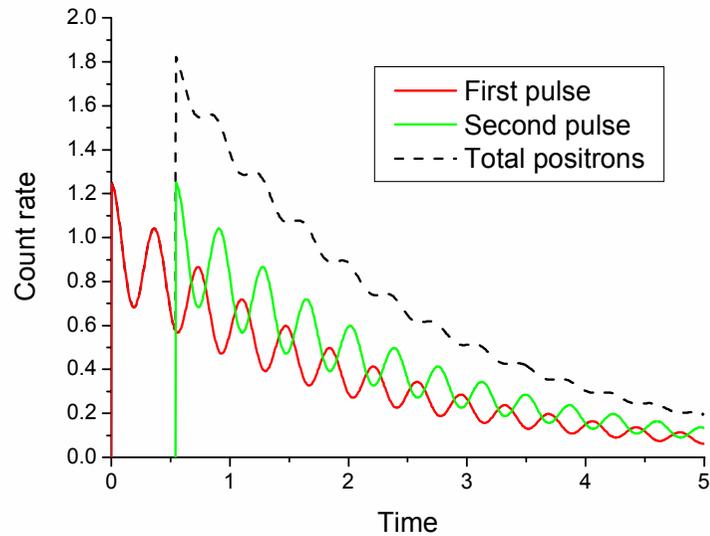
## Beam line design 4

- Magnetic beam line selects momentum only
- Need to separate out positrons with  $p=27 \text{ MeV}/c$  ( $v \approx c$ ) from surface muons (also  $p=27 \text{ MeV}/c$  but  $v = 0.24 c$ )
  - these arise from muon decay in the target and have the same time structure as the positrons from the sample
- Use Crossed field separator
- Electrostatic and magnetic forces cancel for particles of the correct velocity



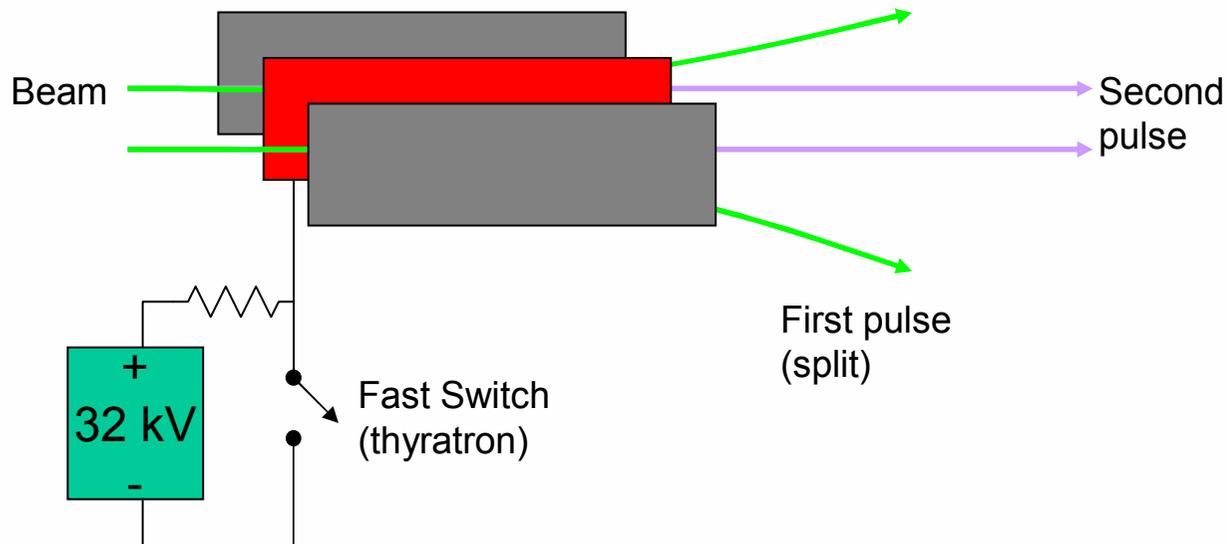
## Beam line design 5

- ISIS produces a double proton pulse, separation 330ns (repeated at 50Hz)
  - Muon lifetime  $2.2\mu\text{s}$
  - Therefore the muon decay spectra overlap
  - Transverse precession signals can interfere and cancel
- Must remove one pulse.



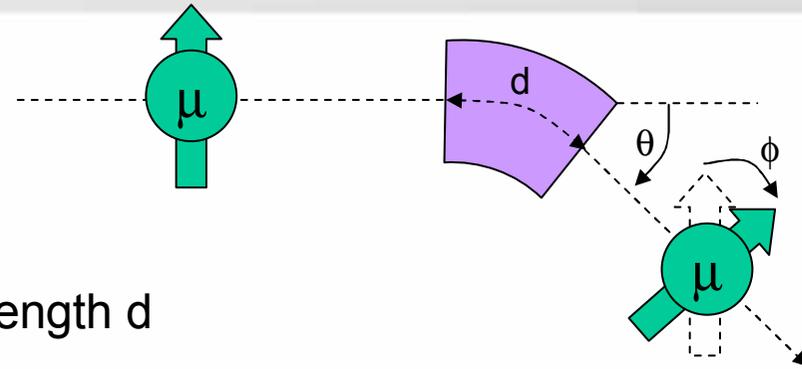
## The Kicker

- First used 'UPPSET' electrostatic kicker to throw away one pulse
- Improved design - divert the second pulse elsewhere - EC electrostatic kicker
- RIKEN uses a magnetic kicker, better for high momentum muons



- Also useful for
  - Slicing pulses for higher frequency response
  - Lower background at continuous sources - MORE at PSI

# Spin Rotation



For a magnetic bend of field  $B$  and path length  $d$

Deflection  $\theta \approx \frac{d B e}{p}$

Spin precession  $\phi \approx B \gamma t = \frac{d B g e}{2p}$

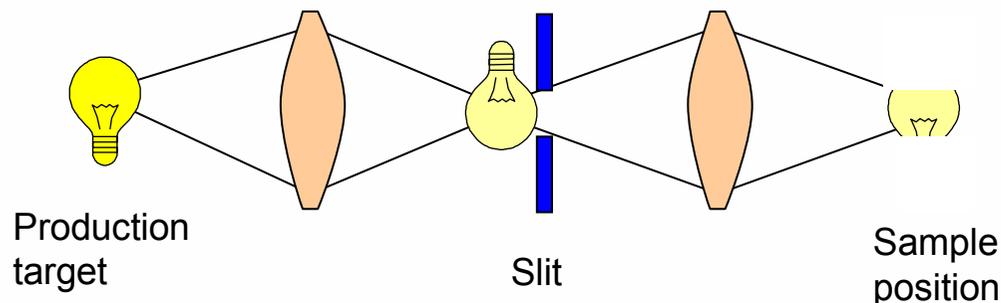
Exact match for  $g=2.0$ . Muon  $g=2.00233$  so the spin follows the momentum along any simple magnetic beam line.

Muon storage rings can measure  $(g-2)$  after many turns

- Electrostatic deflection leaves the spin unchanged but rotates the momentum  
ISIS kicker gives  $4^\circ$  horizontal spin rotation for EMU and DEVA
- A crossed field device rotates the spin without changing the momentum  
ISIS separator gives  $6^\circ$  rotation (vertical)
- Higher fields and/or longer path length give a 'spin rotator' ideally  $90^\circ$   
useful for transverse field experiments, muons enter sample along field  
 $\sim 45^\circ$  allows simultaneous measurement of longitudinal and transverse relaxation

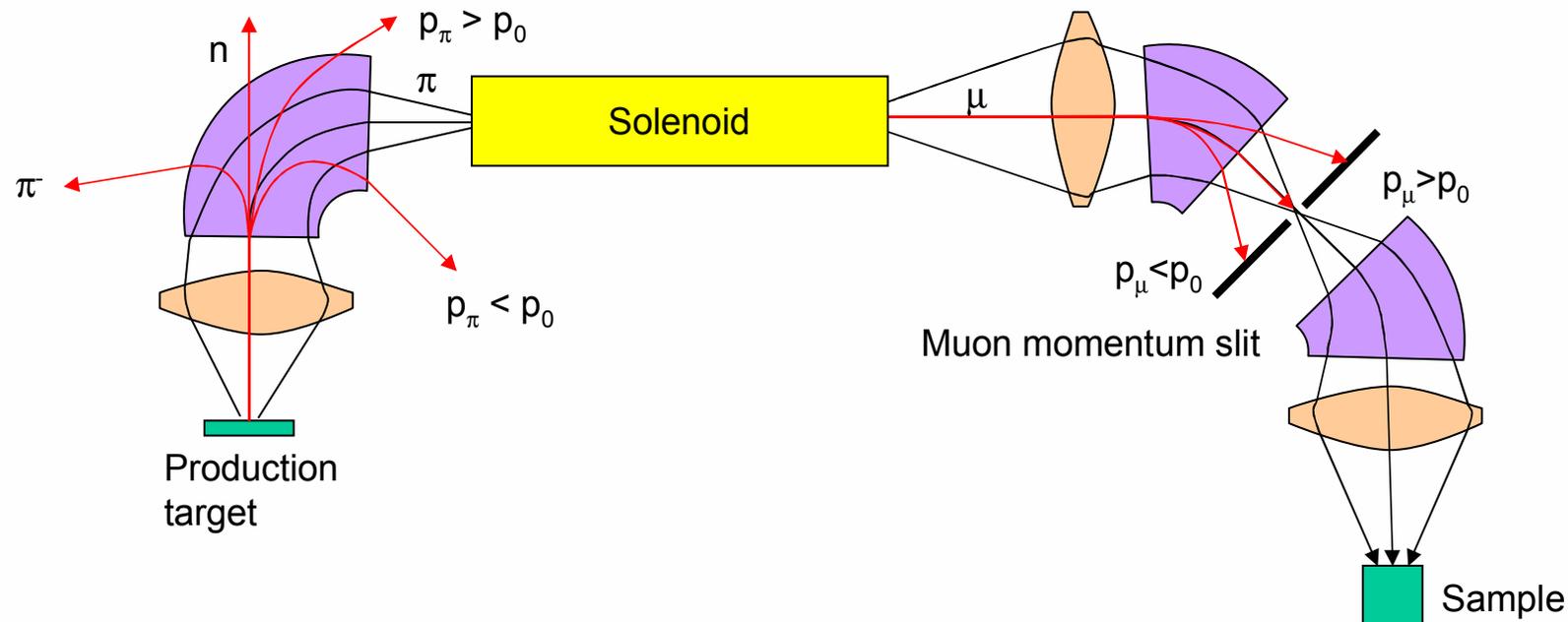
## Beam line design 6

- The muon spot is the image of the production target – often too large
- We could use collimators near the sample
- Unwanted muons stop in the collimator and decay as normal
  - These positions must be stopped from reaching the detectors while not blocking those from the sample. Difficult to achieve in practice
- □ Solution – Remote collimation
  - Intermediate focus earlier in the beam line
  - Slits at that point reduce the spot size
  - Positions from the slits cannot reach the detectors
  - Slits imaged onto the sample



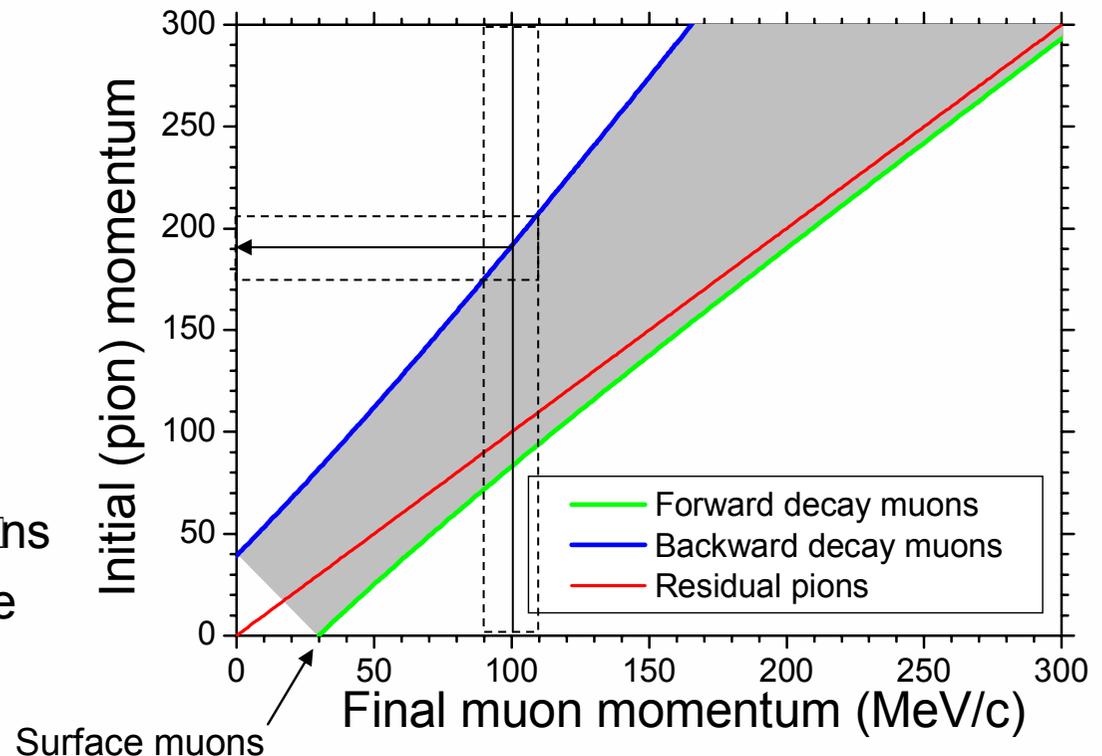
## Decay beam line

- Pions decay to muons at different positions along the beam
  - 100 MeV pions decay over a mean path length 5.5m
- Must keep the muons in the same path although different momentum
- Solenoid (high longitudinal field) where the particles spiral round the field lines
- Inject pions into solenoid, selecting initial momentum for decay
- Exit of solenoid is muon source. Select final momentum and focus onto sample



## Decay muon beam tuning

- We can use either 'backward' or 'forward' muons
- Backward muons are easier to separate from remaining pions (or muons formed before initial momentum selection)
- Select muon energy
- Tune muon section of beam
- Look up required pion energy
- Tune pion section
- Continuum of muon energies between forward and backward
- Actual energy of muons and pions optimised for flux at the expense of some polarisation



## Positive and Negative Muons

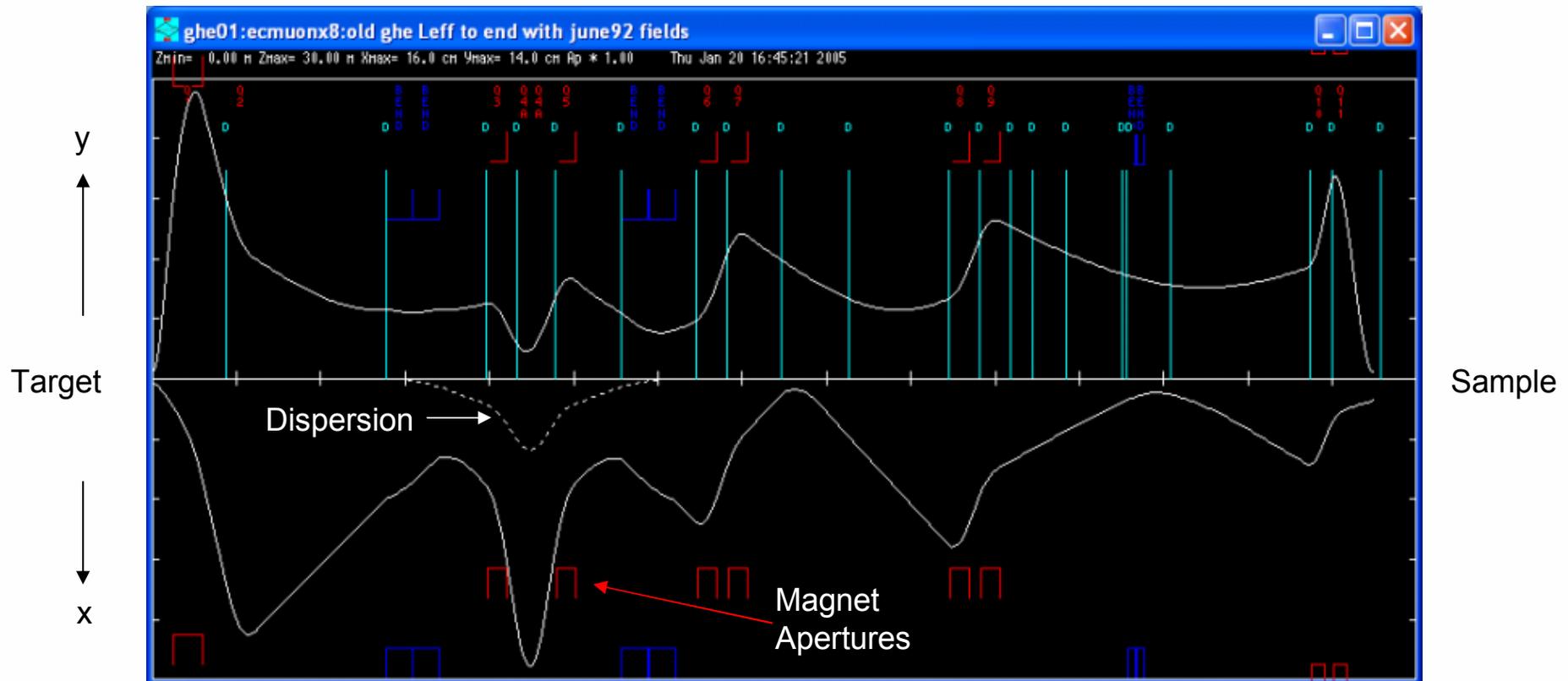
- Most muon experiments use positive muons produced in the decay of positive pions
- Negative muons are also produced, from negative pions
  - Lower yield of  $\pi^-$  than  $\pi^+$  from positive proton beam striking positive nuclei
  - No 'surface'  $\mu^-$  because any negative pion coming to rest in matter is rapidly captured by a nucleus and reacts with it
- Negative muons are also captured into orbits around nuclei
  - Muonic X-rays emitted as muon cascades down to 1s level, characteristic of the elements present
  - Very strong coupling between muon and nuclear spin
  - Muon lifetime reduced by capture reactions  $\hat{=}$  greater effect for larger nuclei
- Can use the same decay beam line to produce a negative muon beam
  - Reverse the fields in all the bending magnets (and quadrupoles)

## Continuous and Pulsed beams

- □ Continuous beam (eg. PSI)
    - DC, or any time structure  $\ll \tau_{\mu}$
  - Each muon counted into the sample and its positron counted out
  - Rate limited if two muons in sample at once  $\hat{n}$  also depends on time range measured
  - □ Background from stray positrons or muons which fail to be counted in
  - Can use veto counters to reduce effective spot size, and exclude positrons (no separator may be needed)
  - Precession frequency range depends on timing accuracy of detectors (500 MHz +)
  - Can remove muon counter and just measure positrons giving average polarisation (ALC) at higher rate
- Pulsed beam (eg. ISIS)
    - pulse length  $\ll \tau_{\mu}$  and spacing  $\gg \tau_{\mu}$
  - Start signal from accelerator at average position of muon pulse, just count positrons out
  - Rate limited only when detectors saturate close to  $t=0$  (segmented)
  - □ Background usually low, time range longer ( $> 10 \tau_{\mu}$ )
  - Must use collimation or 'fly-past' for small samples, and positron-free beam
  - Precession frequency range limited by pulse width (10 MHz)
  - Time dependent polarisation always available 'for free'

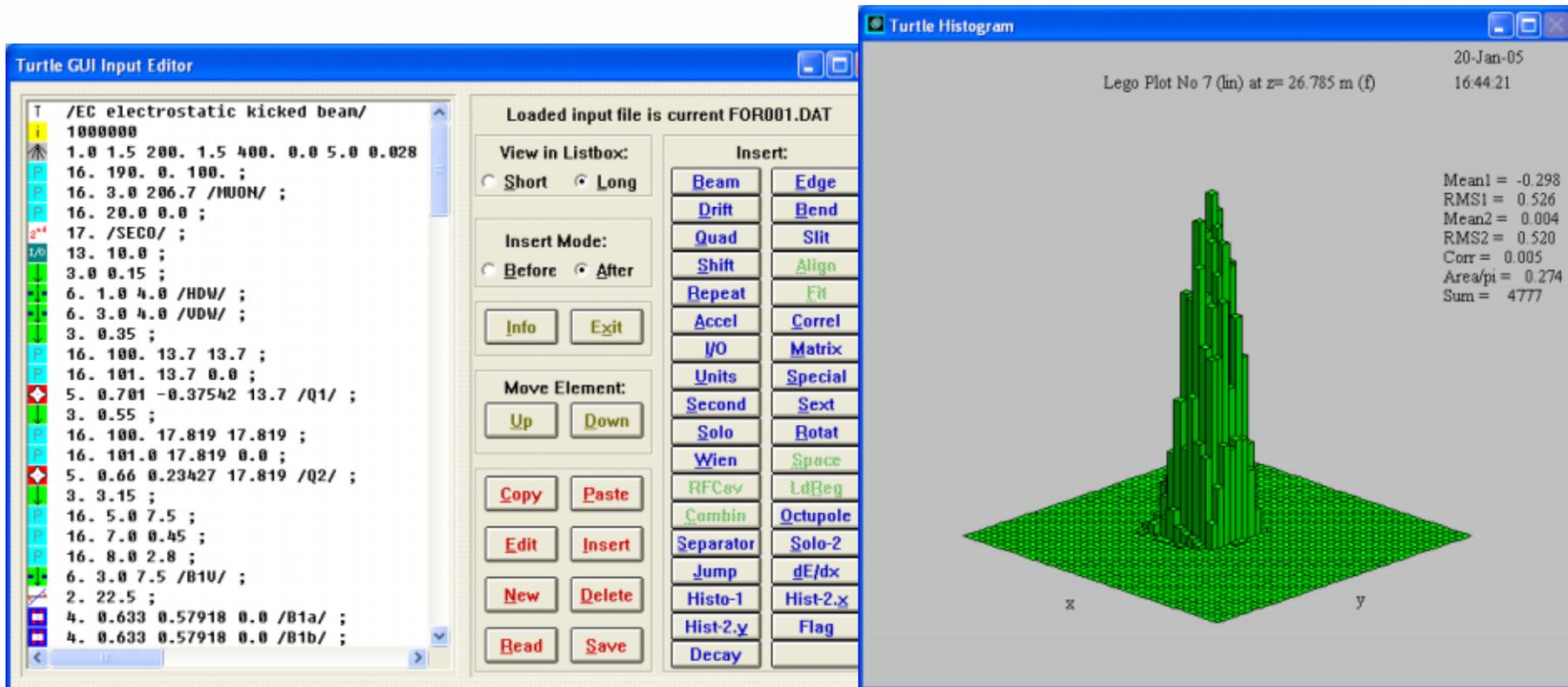
## Designing a beam line

- Computer calculation of the focusing effect of all elements - TRANSPORT
- 'Transfer matrix' method to first or second order - fast calculation
- Finds required fields to focus the beam correctly and best locations for slits
- Plots beam envelopes along the beam line



## Designing a beam line

- Computer calculation by ray tracing individual muons - TURTLE
- More computer time needed - was slow on old computers
- High order corrections and arbitrary apertures included
- Calculate flux at sample and identify where other muons are being stopped



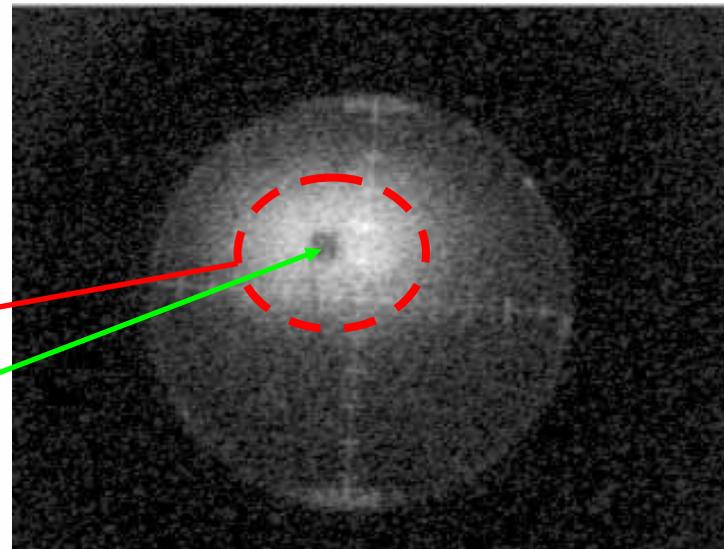
## Monitoring the beam line

We may need to check the performance of the beam line or adjust the focusing, separator voltage, etc:

- □ Measure rates of muons arriving at instrument
  - using either a large sample plate or small fly-past sample at centre
- □ Standard samples for beam steering and spot size measurements
  - combination of materials giving different relaxation signals
- □ Slit Counters □ thin strip of scintillator along the edges of the slits
  - measure muons hitting edge of slit, can adjust slit and measure profile
  - also confirm correct kicker timing
- □ Beam Camera for direct spot imaging at the sample position
  - plate of scintillator viewed by a sensitive CCD camera

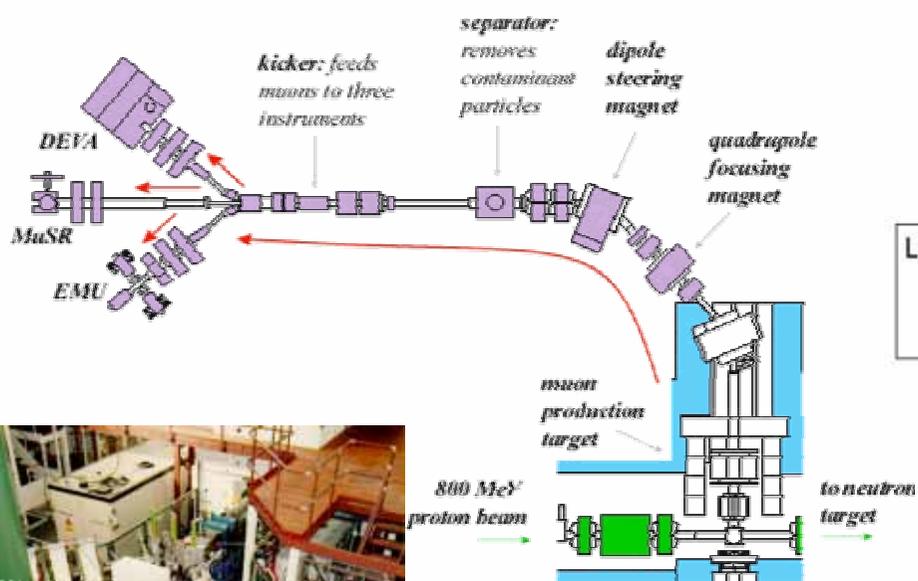
Beam Spot

Marker (sample holder)



## The ISIS muon beam lines today

South side (EC Muons)



North side (RIKEN)

