

# Stimulation Methods 1:

## *Pulsed Stimulations for $\mu$ SR Experiments*

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# Outline of talk

- **Introduction**

Pulsed stimulations;

Stimulation experiments and muon sources;

What do stimulation experiments bring to  $\mu$ SR?

- **Overview of stimulation experiments**

Example stimulation experiments;

- **Radio-Frequency excitation**

RF experiments;

Potential applications of pulsed RF techniques;

Final state spectroscopy;

- **Combining stimuli**

RF+E-field experiments;



# Introduction

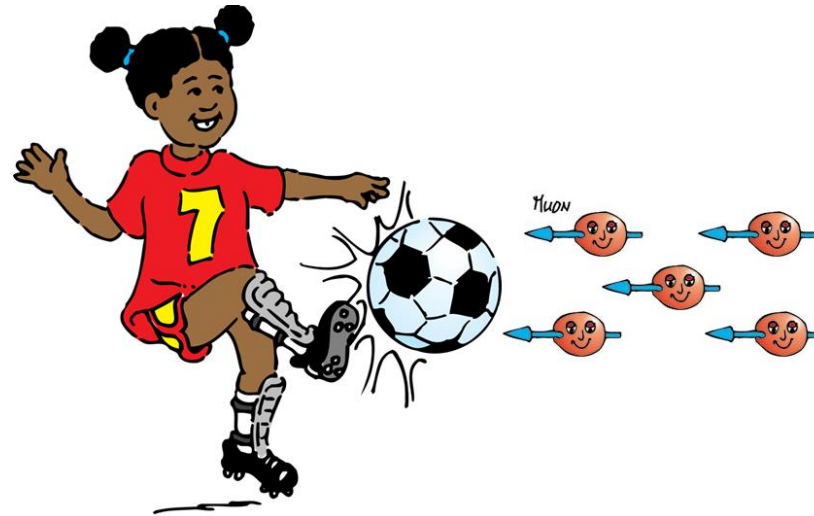


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# Stimulation?

Apply an external stimulation while probing the sample with muons ...



Then hopefully we learn something new about the ~~football~~ sample ...



# Possible Stimulations ...

- Temperature
- Magnetic Field
- Pressure
- Electric Field
- Illumination
- Humidity
- Sound
- Flames
- ...

Many possible!

Some are naturally  
**continuous for experiment**

Others may be applied only  
for a brief period as muons  
are implanted – i.e. **pulsed**  
(like kicking the ball!)



# Pulsed Stimulations...

Many possible, but these are typical ...

- Radio-frequency (RF) resonance
- Currents
- Magnetic fields
- Electric fields
- Acoustic resonance
- Illumination (flash lamp and laser)
- ...



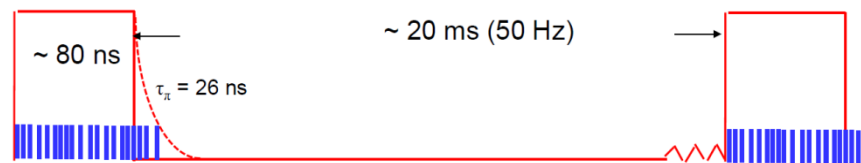
# Why use pulsed stimuli?

- Direct effect of time-varying environment
  - e.g.  $\mu$ SR signal following RF or laser pulse
- Observe slow formation of final muon states
  - e.g. delayed states that are a product of a reaction
- Measure recovery time of sample after a pulse
  - e.g. charge carrier recombination
- Avoid problems with steady state conditions
  - e.g. charge accumulation due to electric field

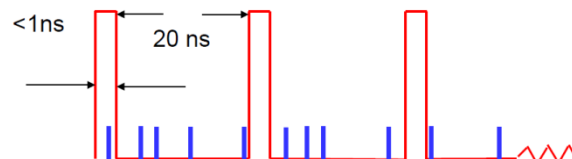


# How to use pulsed stimuli?

- Muon sources come in two ‘flavours’ ...
  - ‘pulsed beam’ (ISIS), all muons in short bunches



- ‘continuous beam’ (PSI), muons arrive randomly





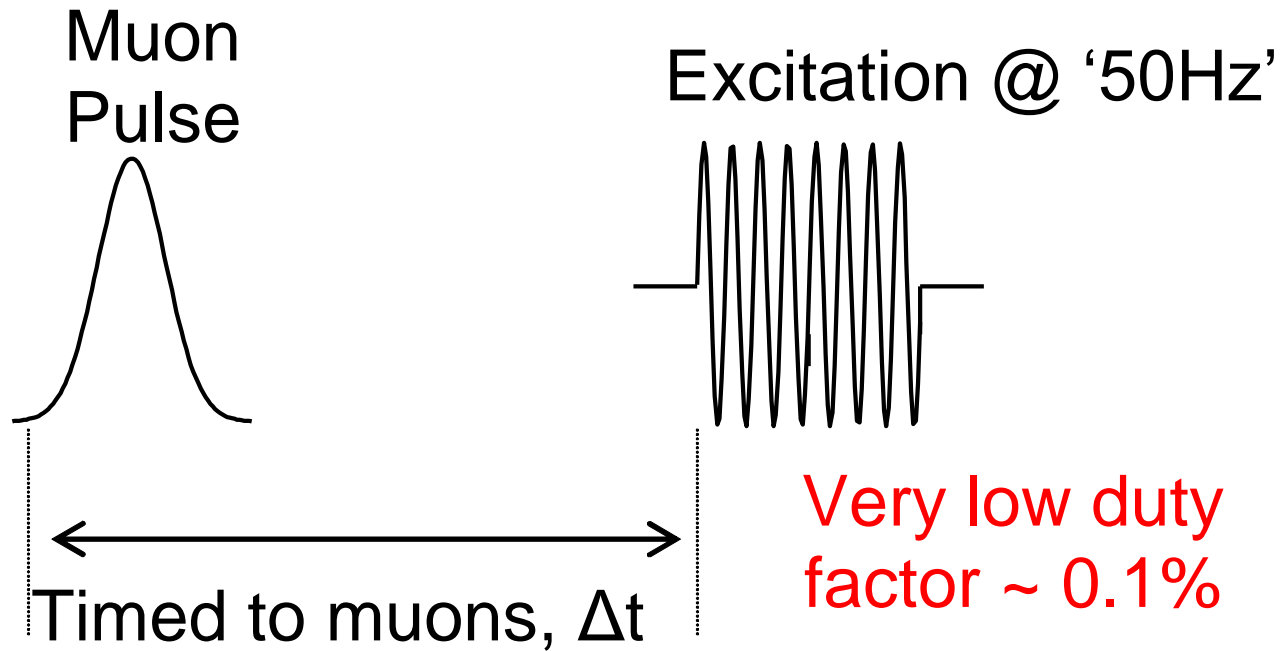
At a pulsed source ...



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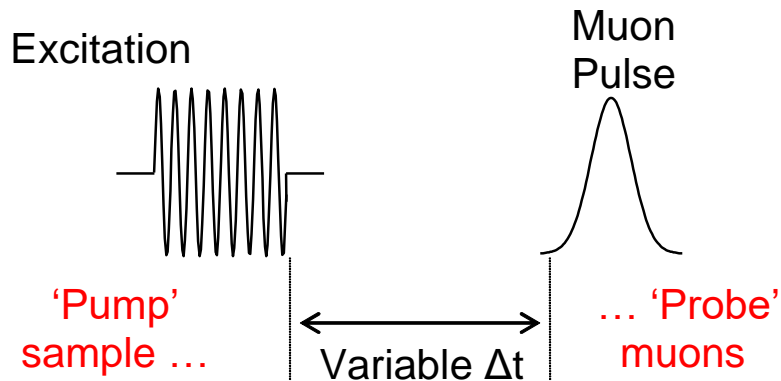
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# Low duty factor ...



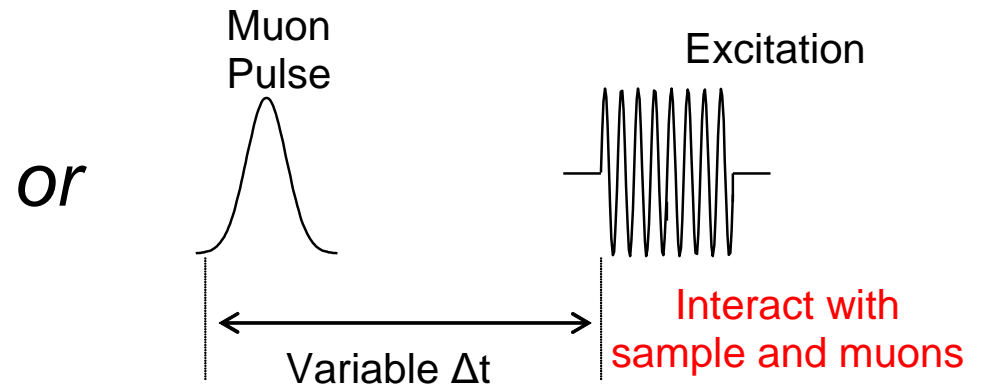
# Time relative to muons ...

*Before ...*



Change  $\Delta t$ ,  
*study relaxation of sample*

*Coincident or after ...*

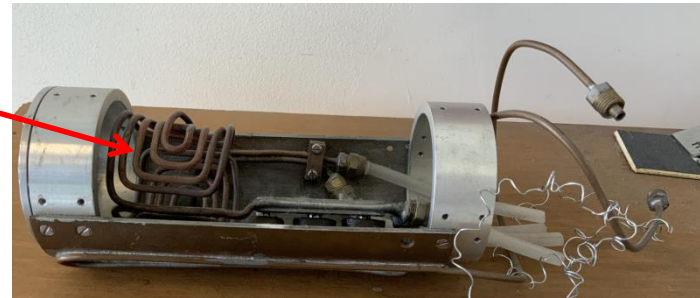
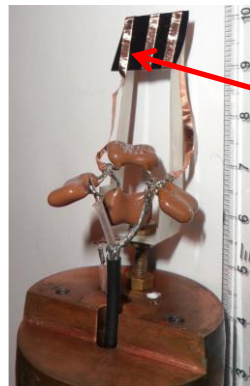


Change  $\Delta t$ ,  
*study muon state kinetics*



# At a continuous source?

- Timing more complex – muons arrive randomly!
- The advantage of the low duty factor is lost:
  - sample/equipment heating can be a problem
  - engineering is more difficult
  - compare RF coils at ISIS and TRIUMF!



*PSI / TRIUMF*



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# Overview of Pulsed Stimulation Experiments



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# Pulsed Stimulations...

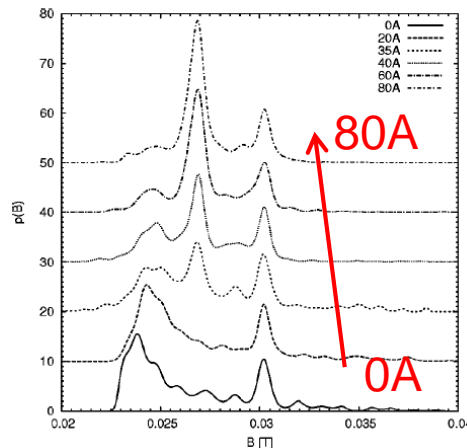
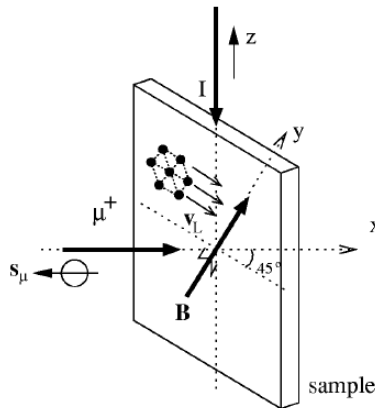
Some examples for ...

- Currents
- Magnetic fields
- Electric fields
- Illumination



# Pulsed Currents

- Current flow in a type II superconductor can lead to flux line motion
- Current measurements allow the study of the moving vortex lattice



**PbIn, 30 mT, TF**

- Pulsed (ISIS), AC (PSI) both contribute to study (higher B-fields at PSI allow smaller currents)

- Motional narrowing of the  $\mu$ SR line shape observed
- Comparison to simulations to understand motion

*D. Charalambous, et al.,  
Phys. Rev. B 66 (2002) 054506  
Phys. Rev. B 73 (2006) 104514*



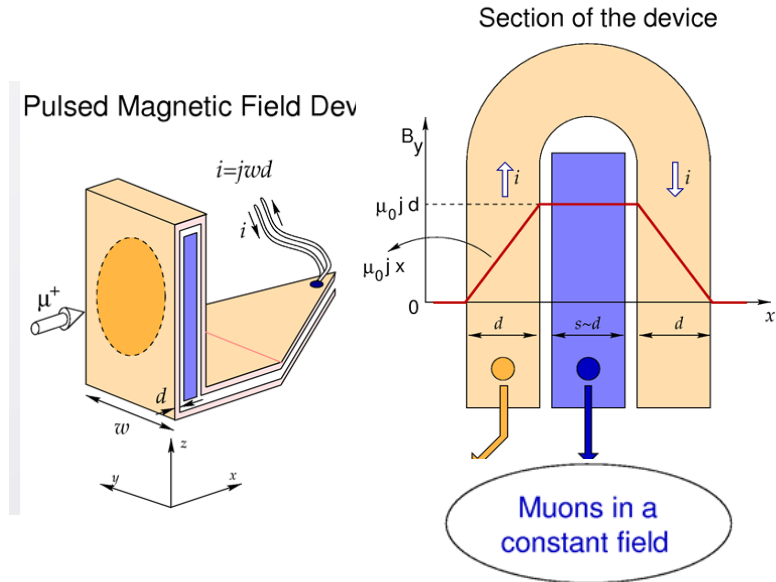
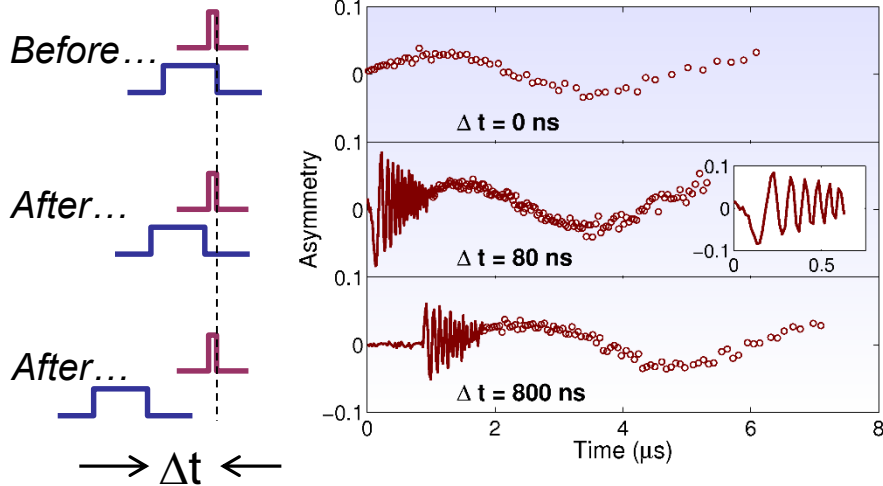
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# Pulsed Transverse Fields

- Removes restriction of finite muon pulse width
- Allows study of slowly formed final muon states

Pulsed transverse field (15G) is applied ...  
 (measuring  $\mu$  formed in Quartz)



*T. Shiroka et al., Phys. Rev. Lett.*  
 83 (1999) 4405

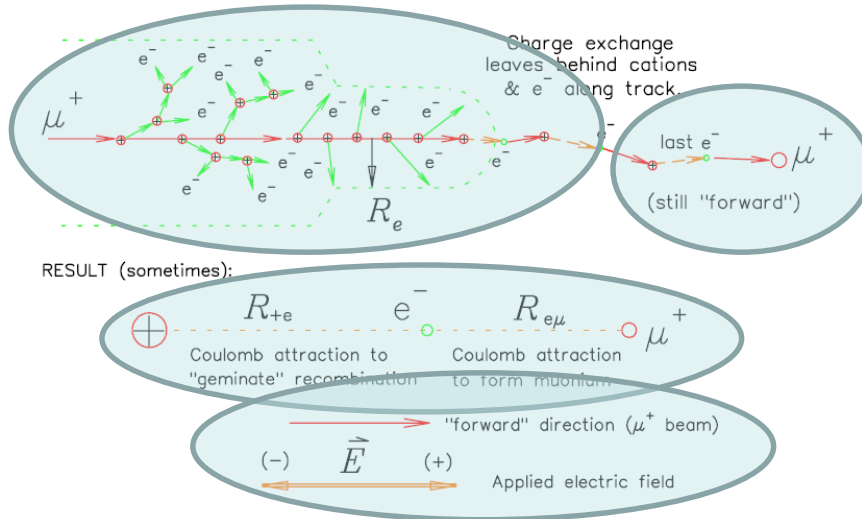




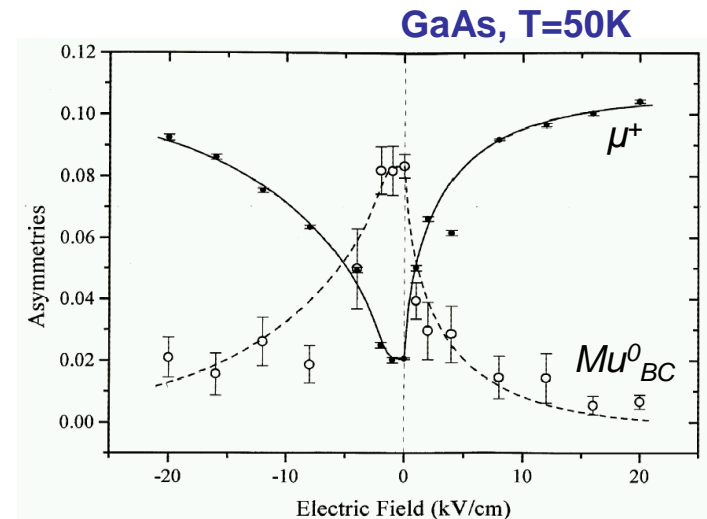
# Electric Fields

- Understanding electron transport in e.g. Rare Gas Solids
- Understanding Mu formation and Mu-H analogy in semiconductors

High energy muons create a track ...



E-Fields transport excess charge ...  
 $\mu^+$ /Mu fractions modified



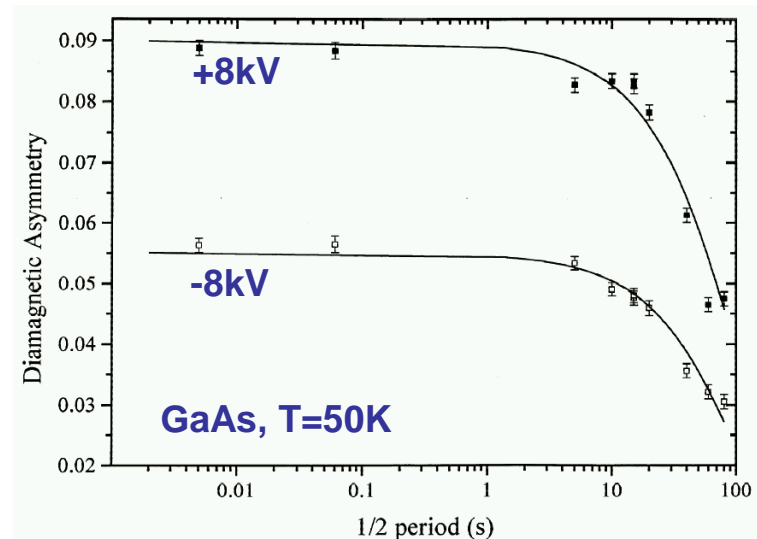
*D.G. Eshchenko et al., Physics Lett. A 264 (1999) 226*



# Switched or Static E-Fields?

- Static E-Fields easily to implement and used in first experiments
- However, results erratic – likely connected with build up of charge at the sample electrode interface (electrode gap and charge mobility)
- Solution was periodic reversal of E-field polarity

- Dependence of  $A_D$  on period of switching

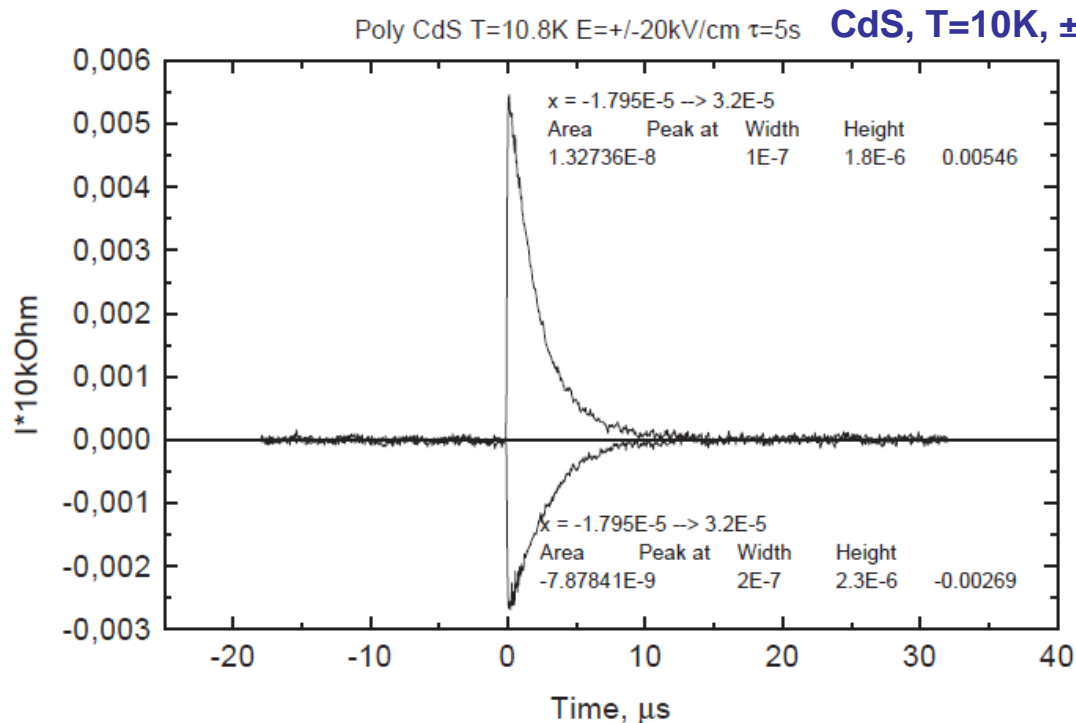


*D.G. Eshchenko et al., Physics Lett. A*  
264 (1999) 226



# Track-induced Current

- Muon track-induced current – Bulk effect of microscopic process!



# Illumination

- Flash lamps and ...



- See Koji's talk on Thursday!



# Radio-Frequency Stimulation



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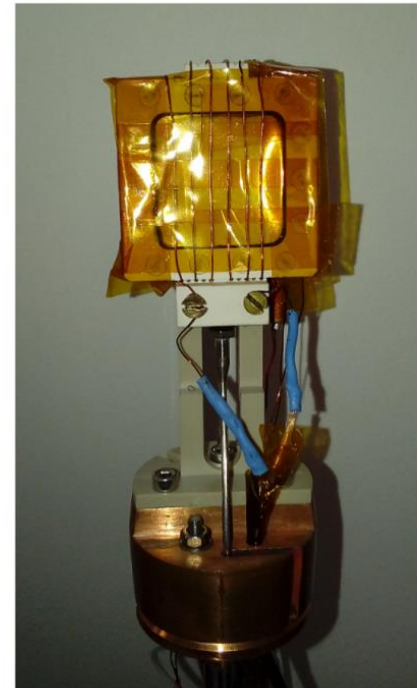
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# Resonance Experiment

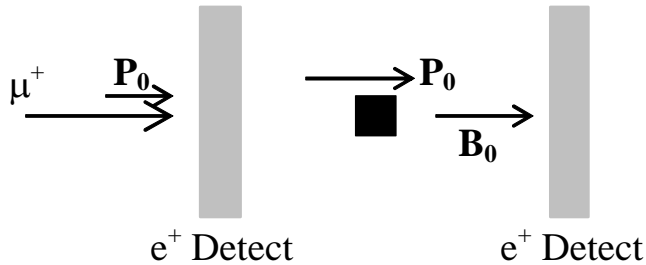
Apply an **RF Field**,  $\mathbf{B}_1$ , perpendicular to a **static field**  $\mathbf{B}_0$ ;

Adjust the **RF frequency**,  $\omega_0$ , to equal  $\gamma\mathbf{B}_0$   
(Larmor equation,  $\gamma = 13.5534$  kHz/G for  $\mu^+$ )

Just the same as doing an  
NMR experiment

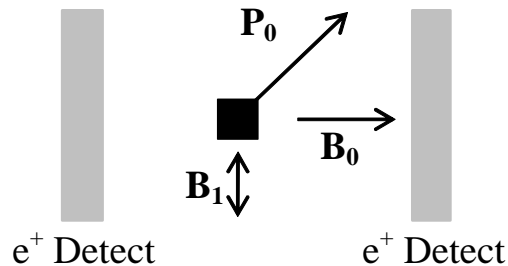


# RF Resonance

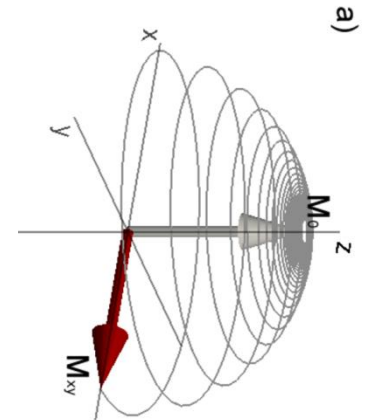


Implant muons: polarisation,  $P_0$ , parallel to static field  $B_0$

Turn on RF Field,  $B_1$  ...



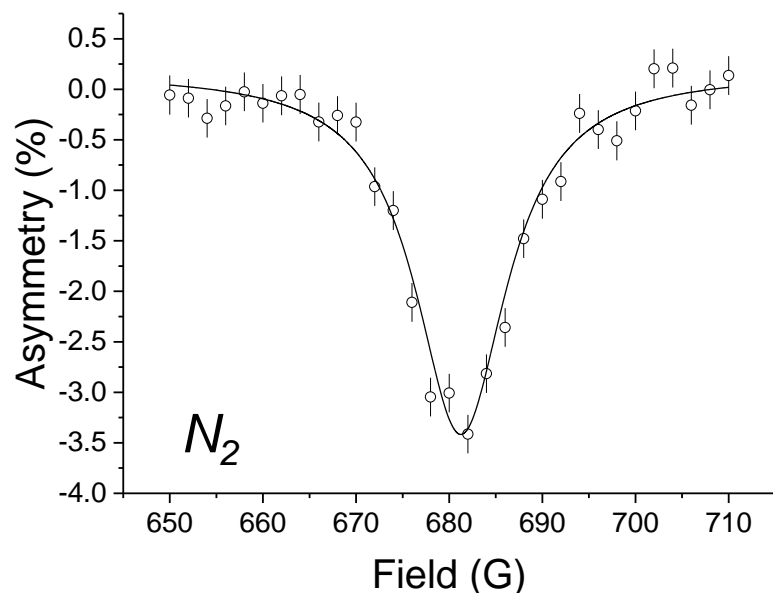
Muons couple to  $B_0$  and  $B_1$ , complex motion



# Resonance Experiment

Condition for resonance given by Larmor equation  $\omega_0 = \gamma B_0 \dots$

Scan frequency or field to determine ... but generally easier to scan field



Form of curve:

$$A_{\text{RF}}(B) = A_{\text{RF}}(B_0) \frac{\Delta B^2}{(B - B_0)^2 + \Delta B^2}$$

$\Delta B$  depends on:

- RF power
- Depolarization
- Chemical reaction



Field scan ( $\omega_0 = 9.2\text{MHz}$ )

CW NMR!



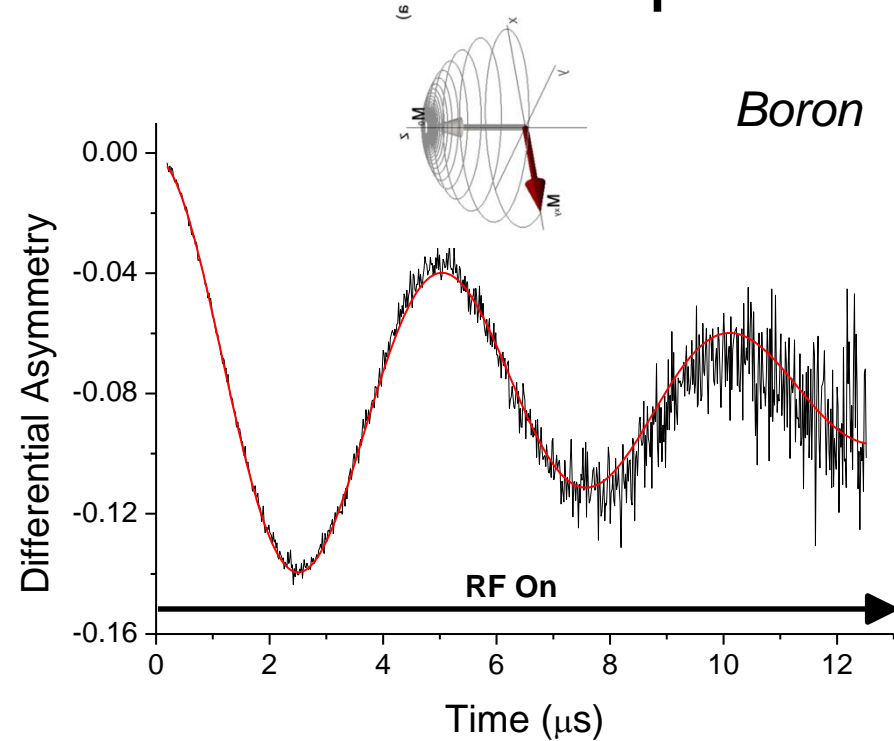
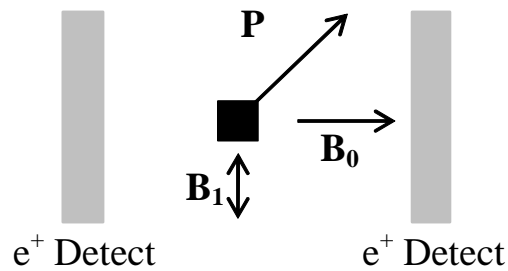
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# 'Longitudinal' $\mu$ SR signal – precession about $B_1$

At resonance ...

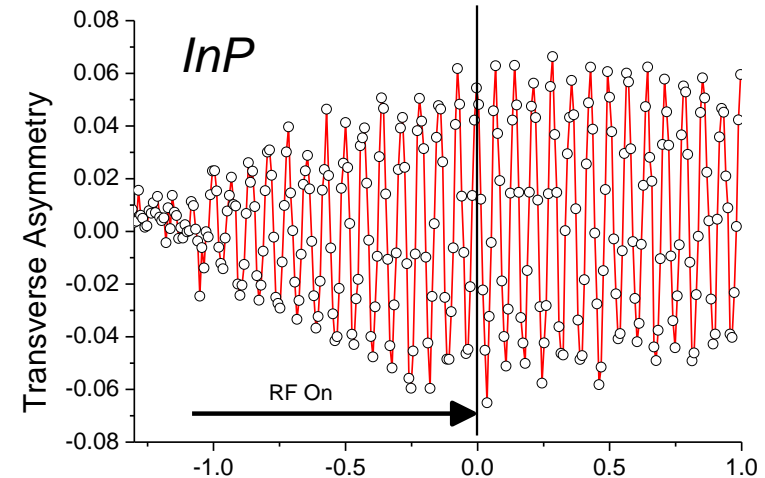
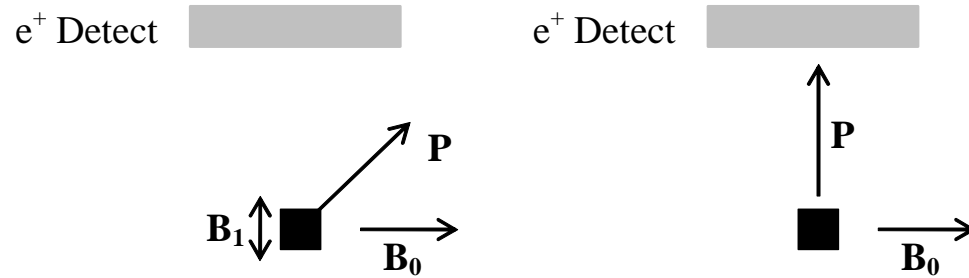


Precession about RF field,  $B_1$ , determined as  $\sim 15$ G from fit

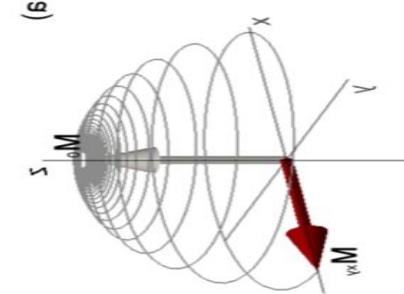


# 'Transverse' $\mu$ SR signal – precession about $B_0$

At resonance ...



Amplitude of 'transverse'  $\mu$ SR signal grows      Turn off RF field after  $90^\circ$  rotation of  $P_0$

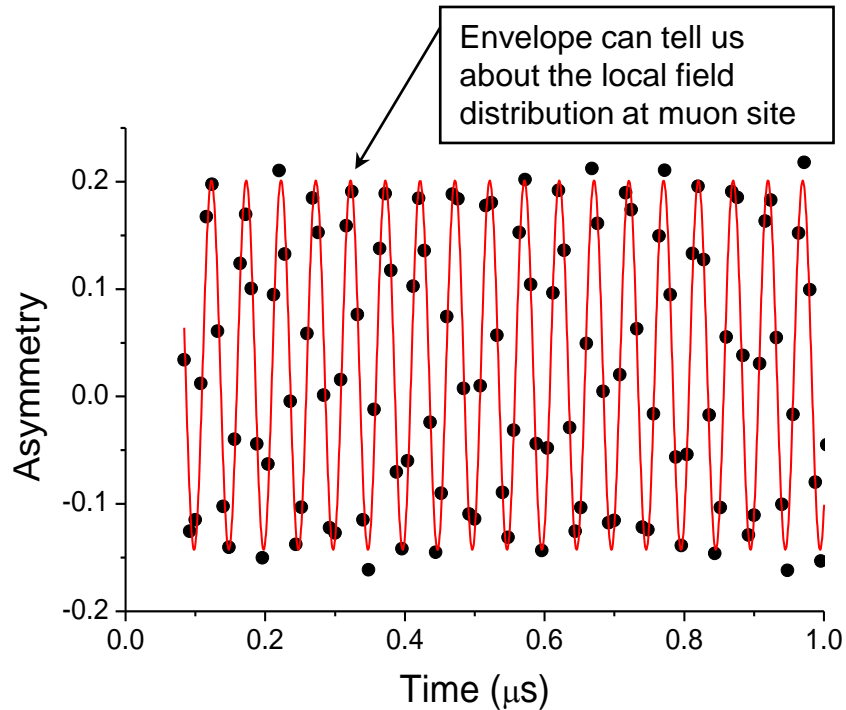


Muon precession at  $\sim 20$  MHz,  
 free precession signal following a  $1.3 \mu\text{s}$  RF pulse  
 In NMR terms, this is a  $90^\circ$  pulse!

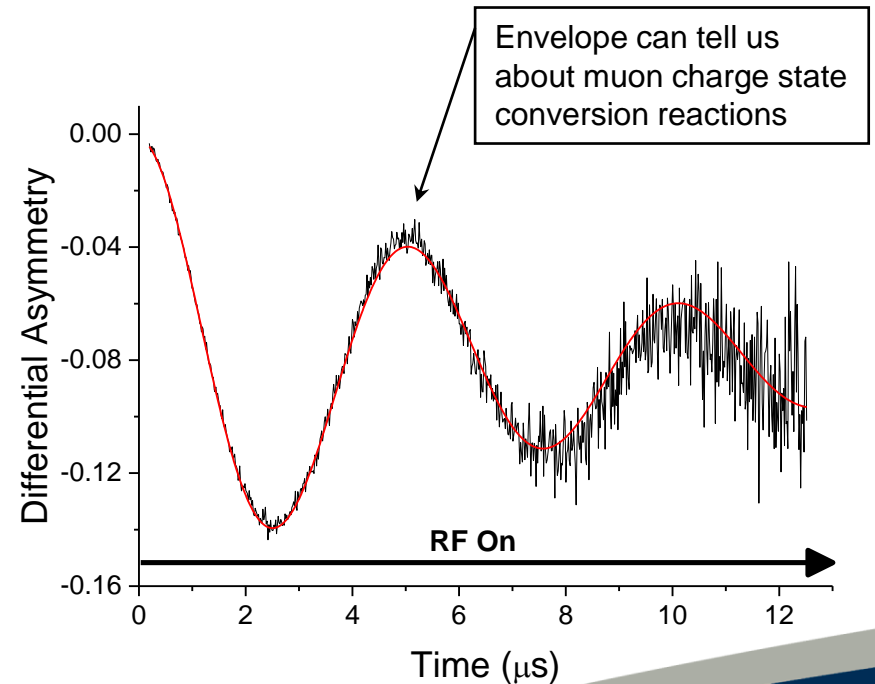


# RF $\mu$ SR – What are we Learning?

‘transverse’  $\mu$ SR signal –  
free precession

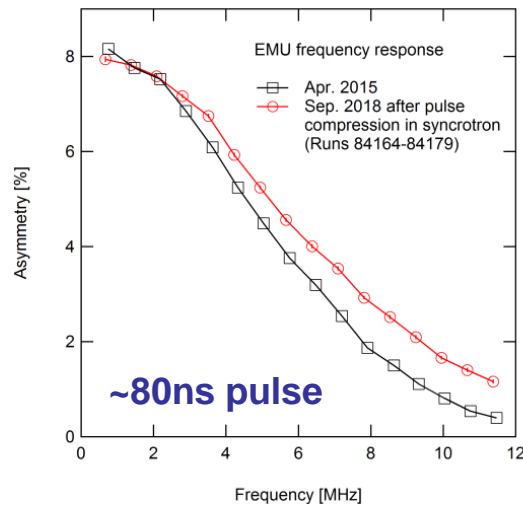


‘longitudinal’  $\mu$ SR signal



# Muon Precession at 20MHz!?

For *Pulsed Muon Sources*, finite muon pulse width limits maximum useable frequency ...



~80ns ISIS pulse corresponds to a ~6MHz frequency bandpass

So how come we're seeing muon precession signals at ~20MHz?

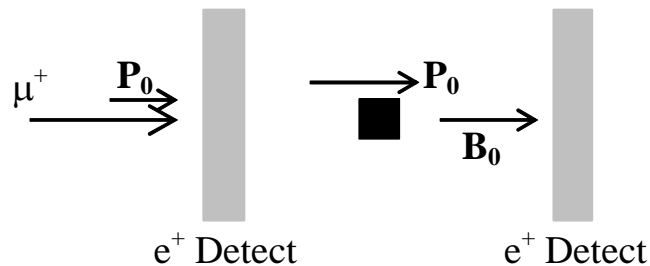


# 90°: 'Beating the Pulse Width'

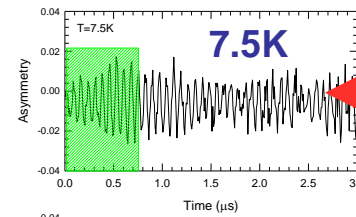
For RF experiments:

- muons implant in a large longitudinal field
- time structure of muon pulse removed

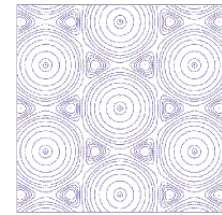
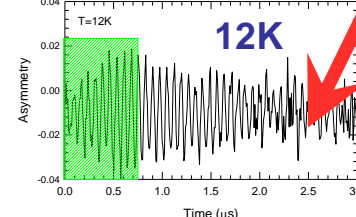
Frequency limit extended!



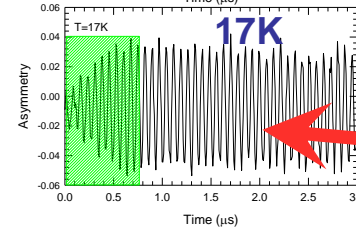
Example taken from study of  $\text{YNi}_2\text{B}_2\text{C}$  ...  
 (A.D. Hillier et al., *Physica B* 326 (2003) 275)



Superconducting  
(mixed) state



( $T_c = 15\text{K}$ ,  $\lambda = 103\text{nm}$ ,  $\xi_0 = 8\text{nm}$ )



Normal state

$B_0 = 1034\text{G}$  (13.6MHz)



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# Applications



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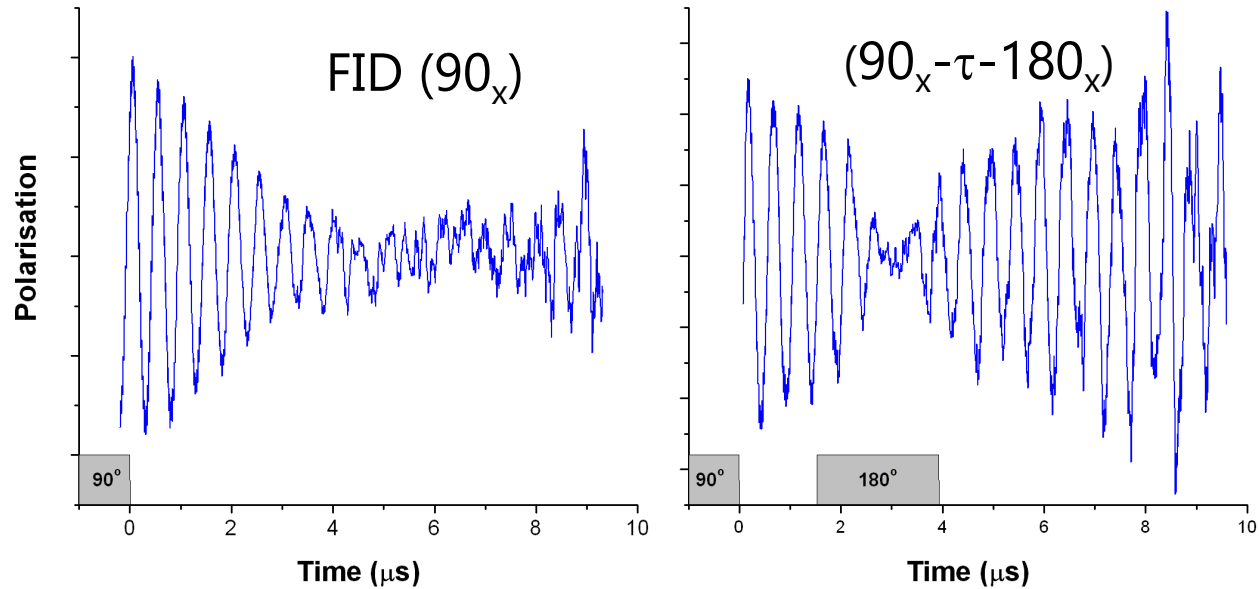
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# RF $\mu$ SR – Benefits / Limitations?

- Many RF techniques from NMR/EPR might be applied to benefit for new science in  $\mu$ SR
- Uniquely, polarisation can be directly measured during RF pulses (compare to NMR)
- However, lifetime of muon can make implementing methods challenging – require short, high power RF pulses!



# NMR-style pulse sequences

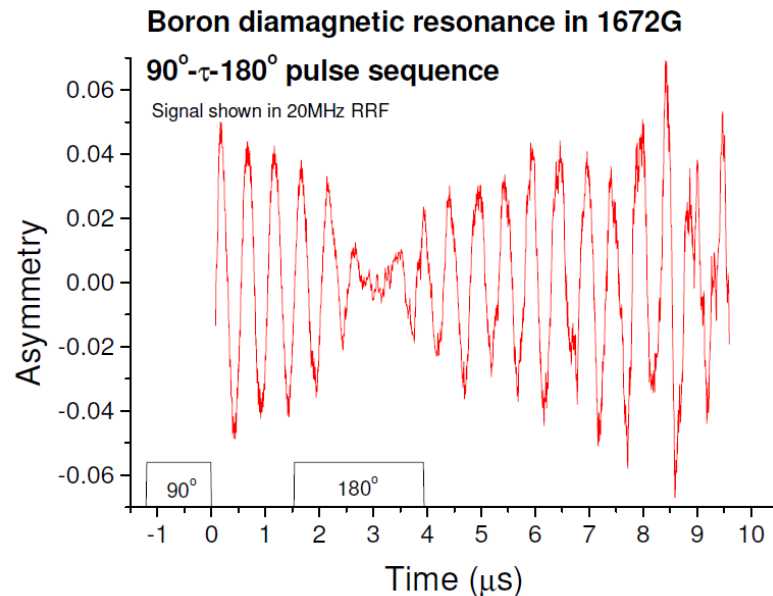


Examples: RF- $\mu$ SR of diamagnetic muons in boron



# 180°: Echoes and Hop Rates

- Precession damped by random nuclear fields
- Re-focus spins with 180° pulse at time  $\tau$ , echo at  $2\tau$
- Potential for studying muon hop rates



S.R. Kreitzman / RF resonance techniques for continuous muon beams 1067

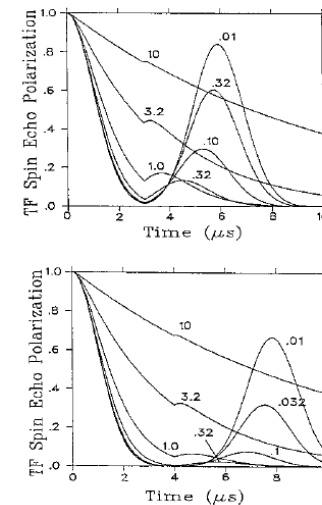
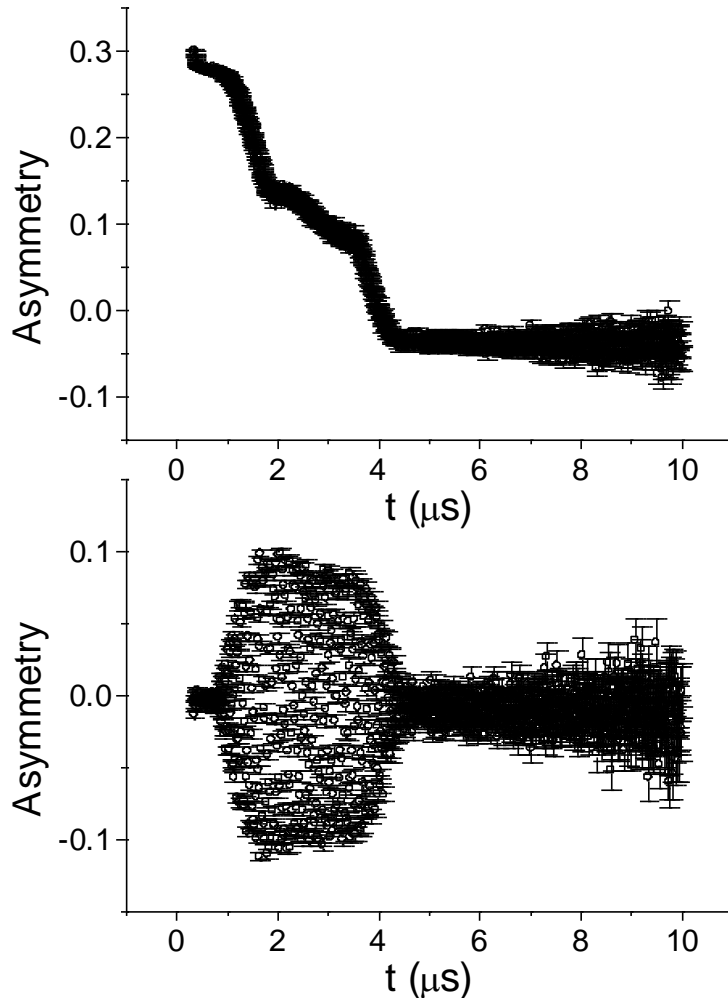


Fig. 6. Theoretical spin echo response for various hop rates. The value of  $\Omega_2$  is  $1 \mu\text{s}$  and pulses are tacitly assumed to be *ideal*. The numerical captions denote hop rates in units of  $1/\tau$ , which for fig. (a) is  $3 \mu\text{s}$  and for fig. (b) is  $4 \mu\text{s}$ . Note that even for reasonably rapid hop rates, the echo position can be distinguished.



# Composite Pulses



Muon RF coils frequently poorly shaped – inhomogeneous fields

Overcome imperfect inversion of  $180^\circ$  pulse using composite sequence  $90^\circ_x 180^\circ_y 90^\circ_x$

Z component shows more complete inversion

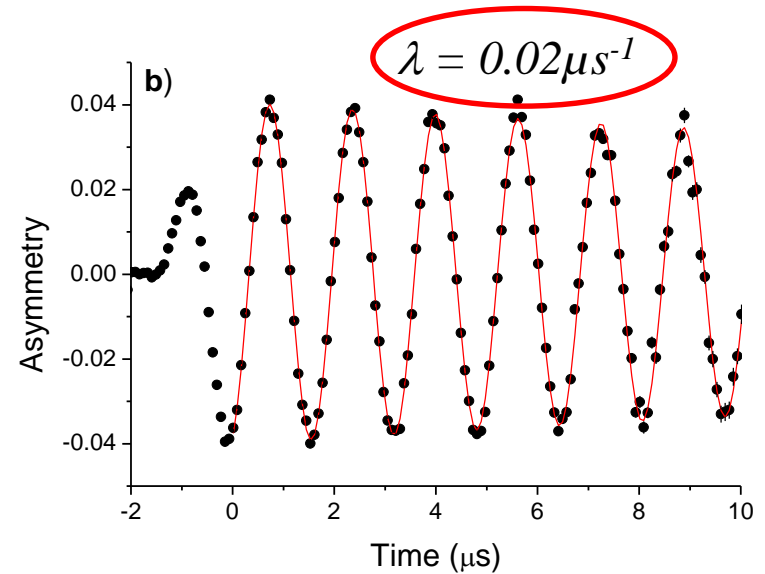
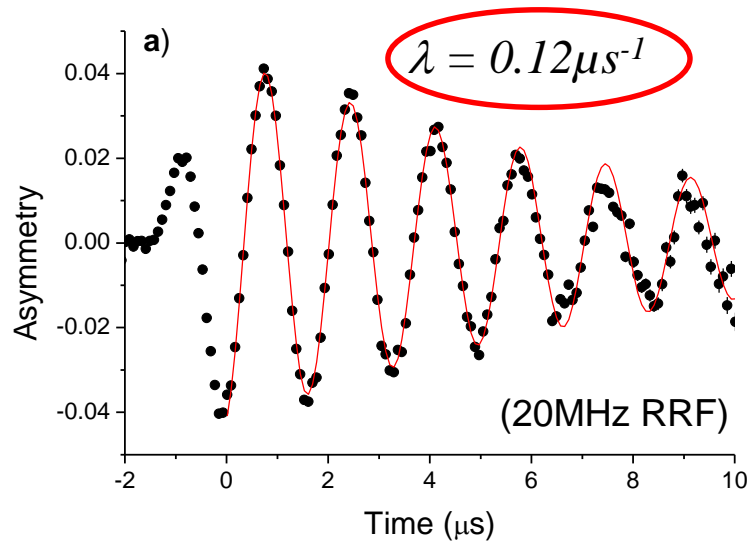
Bonus! With  $\mu$ SR we can see the operation of each component of the composite pulse

# RF Decoupling



# Demonstration: $\text{Ca}(\text{OH})_2$

Continuous Wave RF Decoupling –  $\mu^+$ -H dipolar coupling in  $\text{Ca}(\text{OH})_2$

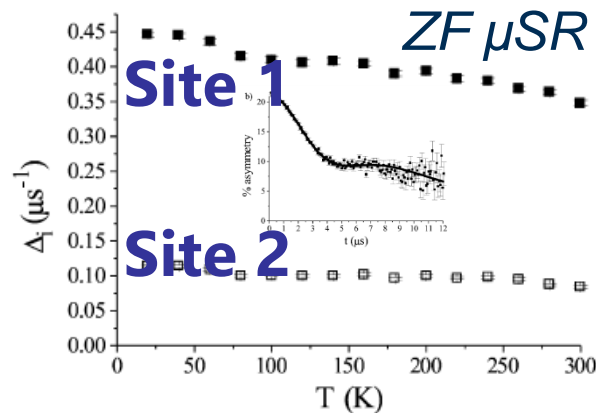


Free precession of  $\mu^+$  following  $90^\circ$  pulse  
**proton coupling causes depolarisation**

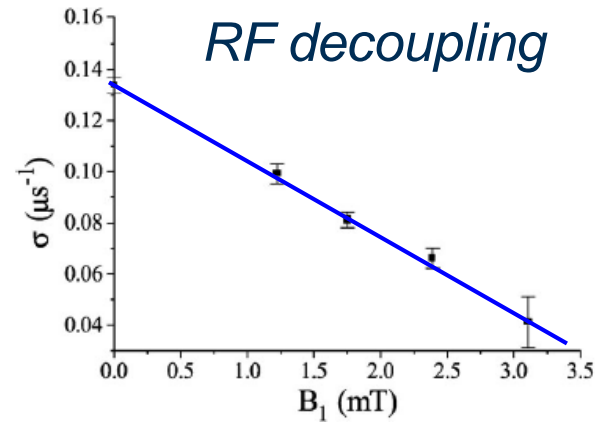
40 G decoupling pulse at proton resonance  
'stir' nuclear spins / measure muon signal  
**proton coupling removed**

# Muon Site Determination

Determining muon's site is an important step in understanding mobility data for proton conductor  $\text{Zr}(\text{H}_2\text{PO}_4)(\text{PO}_4)\cdot 2\text{H}_2\text{O}$  ...



and



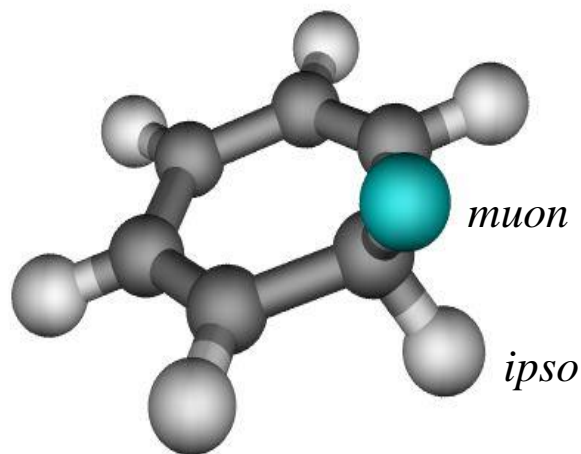
- Two component ZF relaxation implies two muon stopping sites
- Site 1 confirmed by  $^1\text{H}$  RF decoupling - large  $^1\text{H}$  coupling consistent with muon incorporated into water (HMuO) and ZF relaxation for site 1
- Site 2 weaker coupling consistent with formation of P-O-Mu,  $\mu^+$  far from  $^1\text{H}$  spins

# Muonium Chemistry

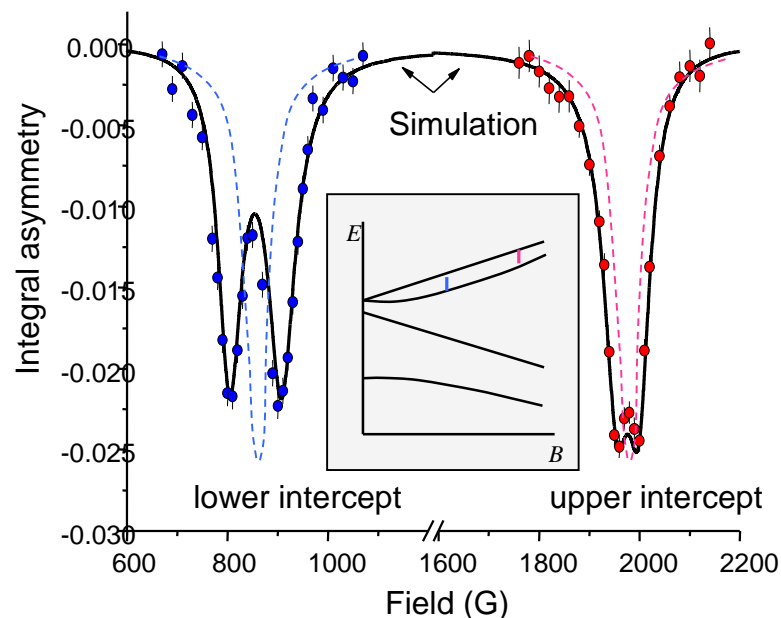
- Easily applied to spectroscopy of muoniated radicals (method for directly measuring  $A_\mu$  at a pulsed source)
- Particularly useful for studying slowly formed species or dilute systems when high TF measurements aren't possible



# Cyclohexadienyl Radical



Looking at the promptly formed radical state at 218 MHz



From fitting (Quantum), Isotropic hyperfine coupling:

$$A_{Mu} = 514.25(1) \text{ MHz at 298K (514.4 MHz [1])}$$

$$A_H = 128.5(3) \text{ MHz 'ipso' proton (126.04 MHz [1])}$$

[1] Dake Y.U. et al, Chemical Physics 142 (1990) 229 – LCR data.

I. McKenzie et al,  
*J. Phys. Chem. B* 117 (2013) 13614



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# Dynamic Processes



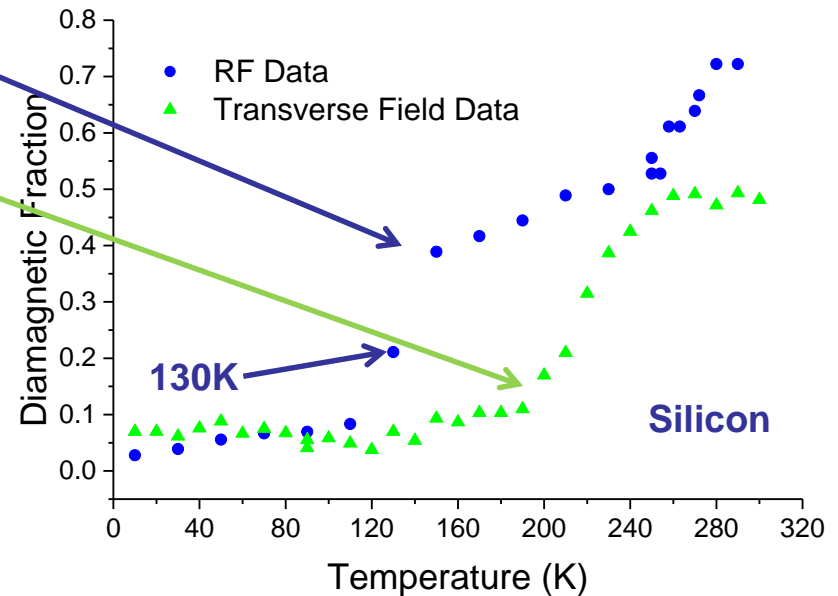
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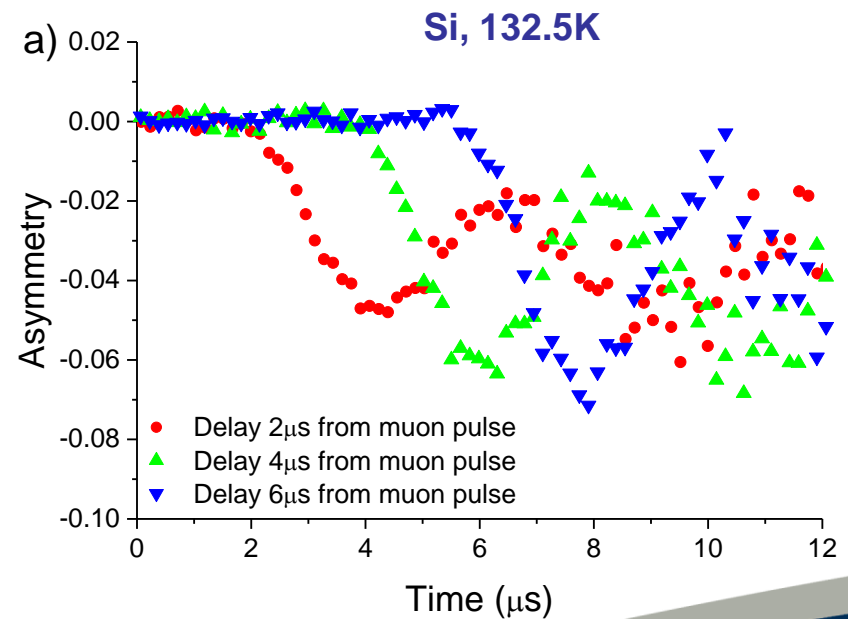
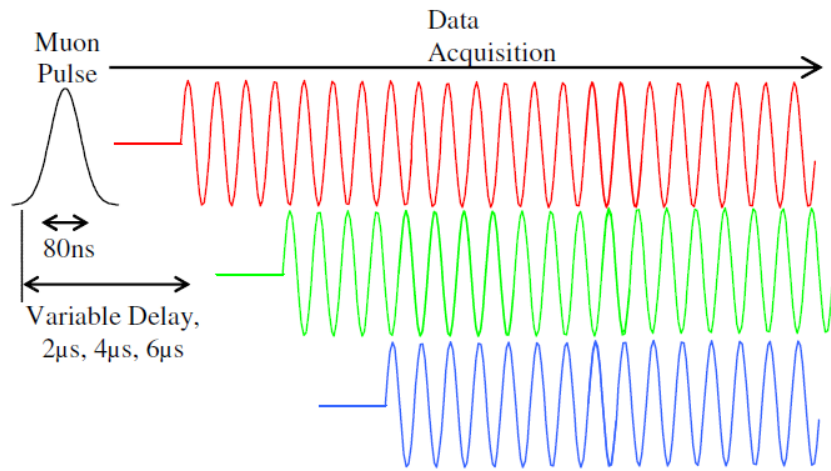
# Final State Spectroscopy

- RF shows appearance of diamagnetic species when TF  $\text{Mu}^{\text{BC}}$  signal disappears
- No diamagnetic signal in TF until much higher temperature
- In TF muons spend a short time as  $\text{Mu}^{\text{BC}}$  and dephase
- In the RF experiment, muon spins are 'locked' along high LF before the RF pulse



# State Kinetics

- For favourable rates ( $\mu\text{s}^{-1}$ ), can directly follow conversion of muon charge state (ionization of  $\text{Mu}^{\text{BC}}$  in this case, for Si)
- Follow the build-up of the final diamagnetic state using delayed RF excitation



# Combining Stimuli

## *RF + E-Field*

*D.G. Eshchenko et al., Physica B*  
*404 (2009) 876*

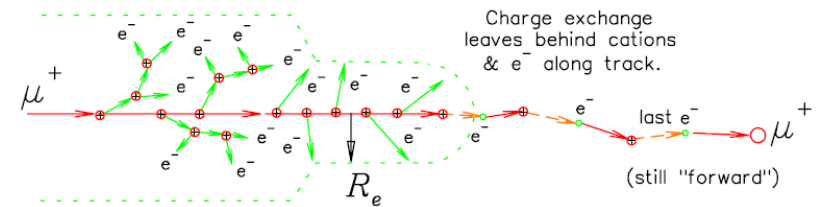
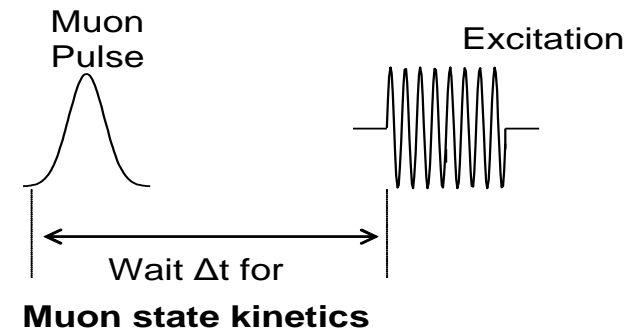


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# Why?

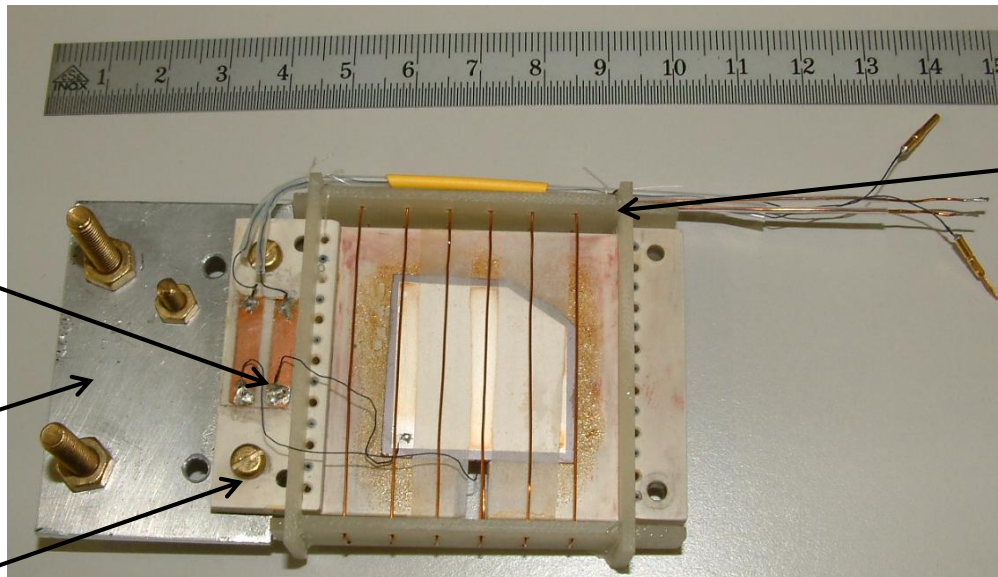
- **RF** to probe final muon state
- **E-Field** to investigate track processes
- Prompt and final states can be compared by combined RF and TF measurements (as for Si)



# Equipment

- Kit gets progressively more complex as stimuli are combined
- Requires care with design ... and sometimes perseverance to get everything working together!

E-field terminal,  
with fine wires  
linking front and  
back electrodes



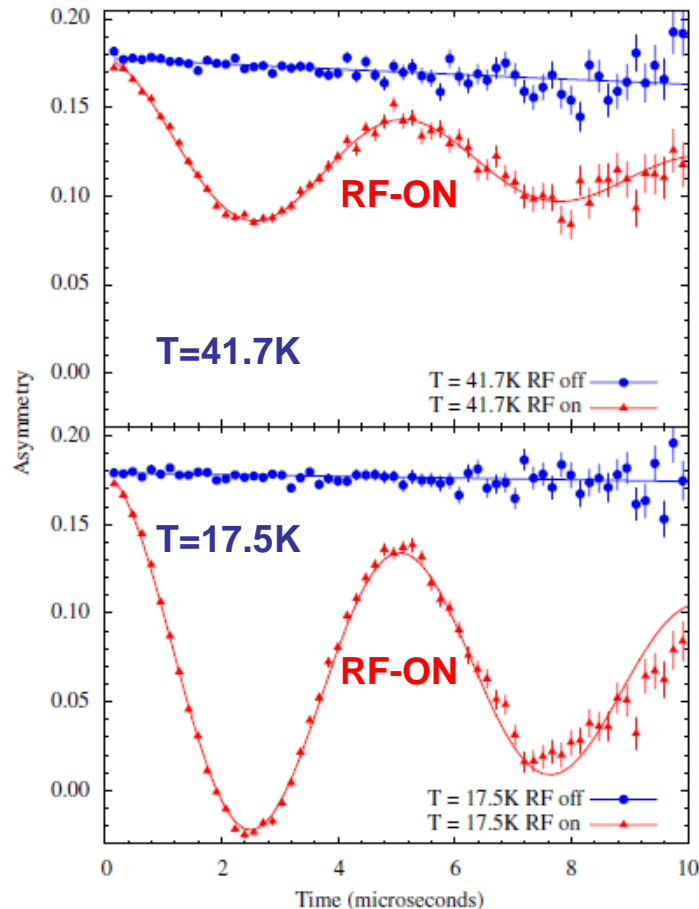
RF coil wound on  
a carrier that can  
be removed for  
sample access

Using CCR, so  
cool by conduction  
through plate

Sample mounted on ceramic plate  
for electrical isolation,  
Shapal chosen since also a  
'good' thermal conductor



# Measurements for GaP



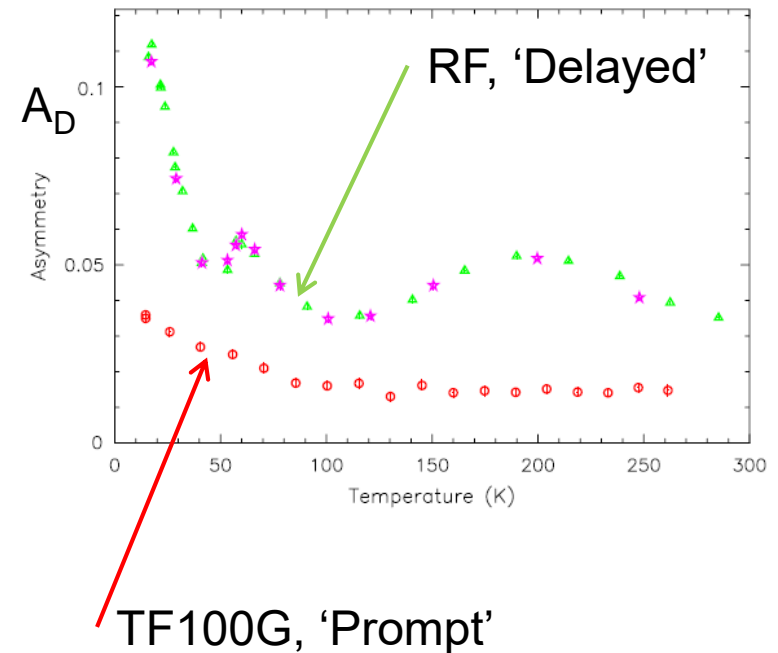
At resonance with  $\mu^+$ ,  
(20.3MHz,  $\sim 1498\text{G}$ )

- Clear precession about the RF field (red curve),
- Amplitude of RF signal increases at low temperature



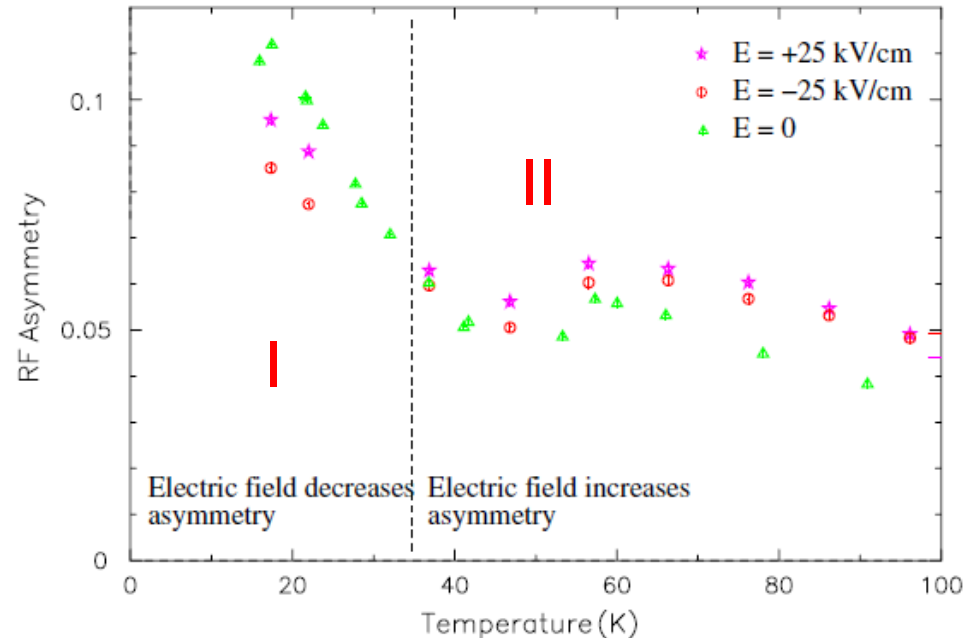
# What was learnt for GaP?

- Dramatic increase in RF asymmetry,  $A_D$ , at  $T < 40\text{K}$
- Explained by considering interaction of  $\text{Mu}_T^0$  with track  $e^-$  or  $h^+$  ...  
 *$\text{Mu}_T^0 \rightarrow \text{Mu}^+$  or  $\text{Mu}^-$  conversion*
- Conversion time can be estimated by
  - analysing the RF phase shift
  - delayed RF measurements*Conversion estimated  $< 800\text{ns}$*



# What was learnt for GaP?

- E-Field *reduces* RF asymmetry in region I, and *increases* it in region II
- Explanation for increase in region II with E-field:  
 *$Mu_{BC}^0$  ionisation (as for GaAs)*
- Explanation for decrease in region I with E-field:  
*Reduction in the cross section for  $Mu_T^0$  capture or  $e^-$  or  $h^+$*





Lots can be done with pulsed techniques ...  
and there's plenty of interest!



**2005 pulsed techniques workshop held in Oxford  
(following  $\mu$ SR 2005)**



Science & Technology Facilities Council

**ISIS**