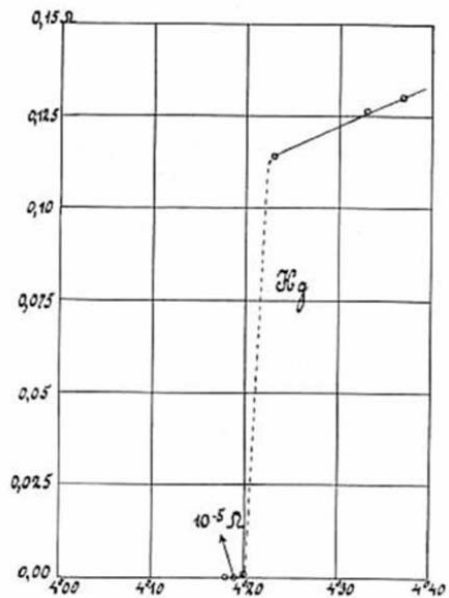


Application of μ SR Superconductors

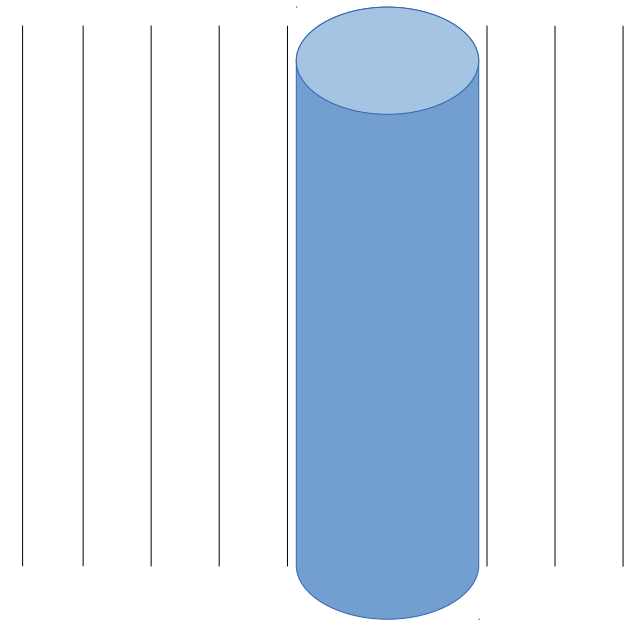


Kamerlingh
Onnes 1911
Hg zero
resistance

Persistent
eddy
currents:
screening

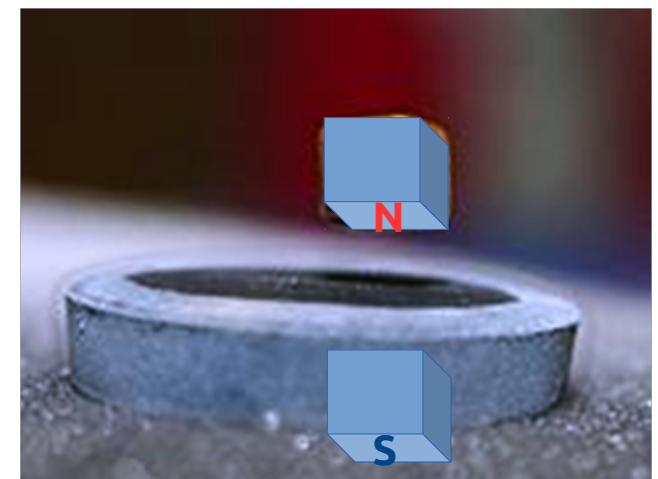
Roberto De Renzi

Dept. SMFI, University of Parma

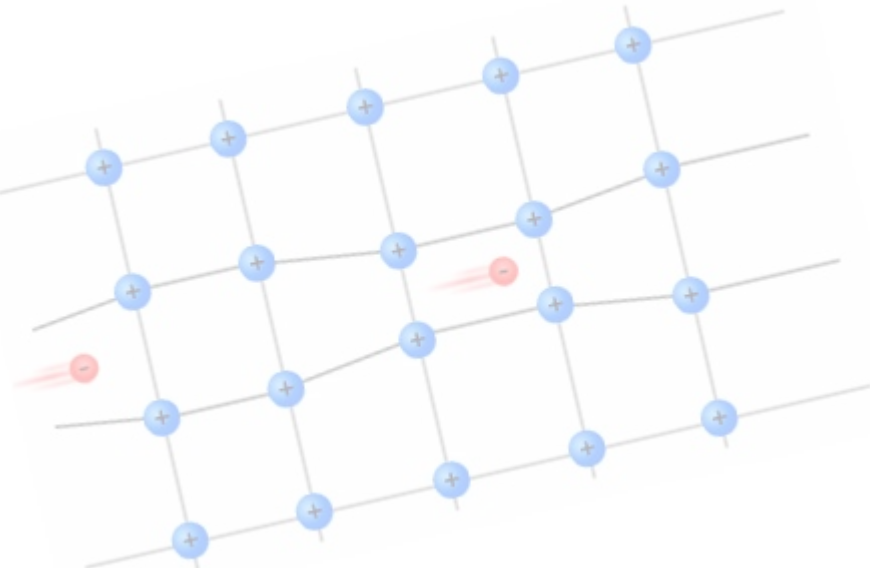


ITER

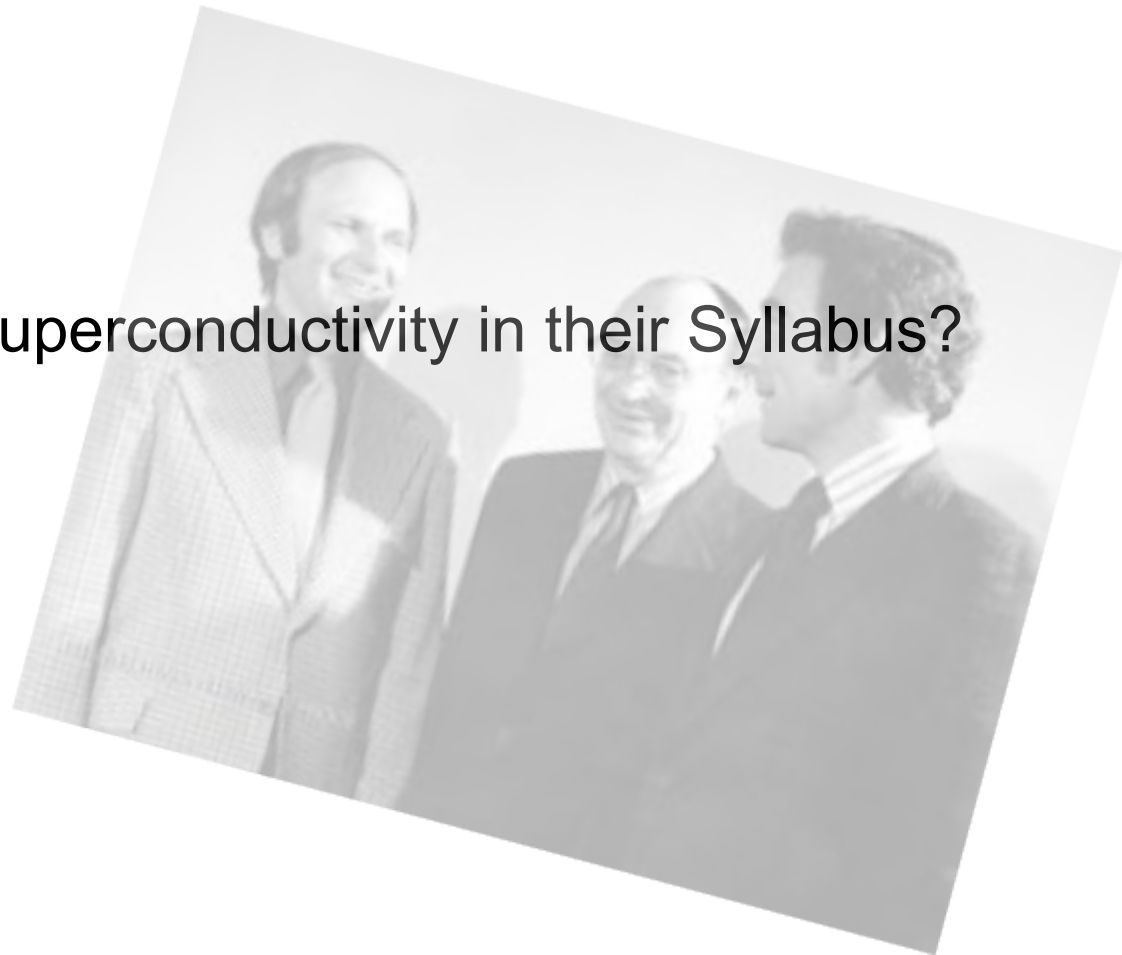
Levitation



μ SR in superconductors

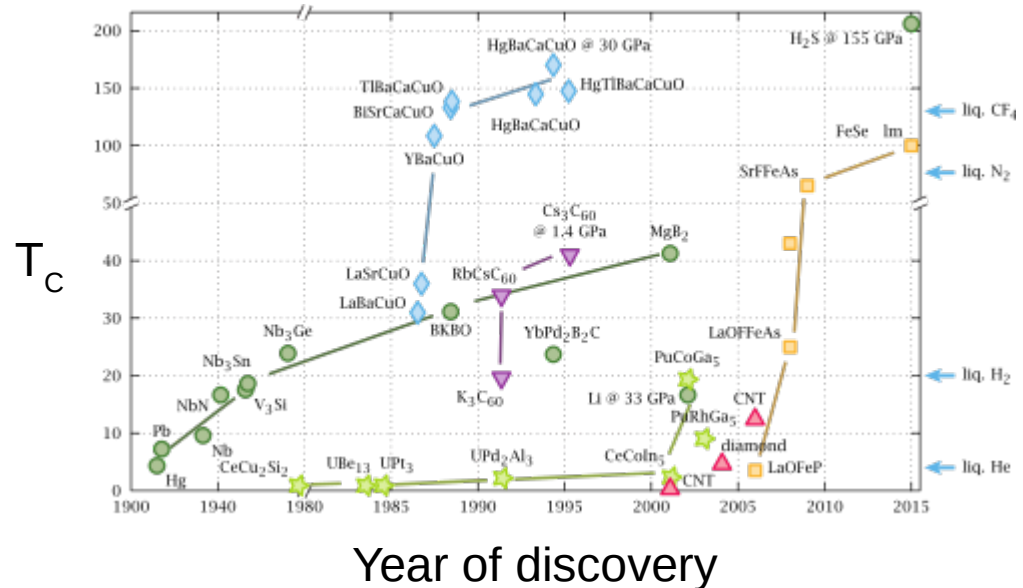


Q0: who did not have any superconductivity in their Syllabus?



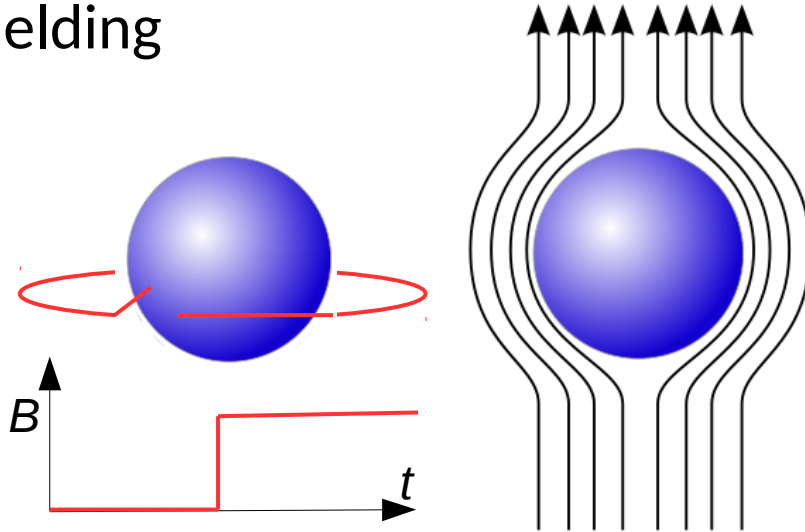
Outline

- Superconductors
 - Meissner effect: magnetic field expulsion
 - London penetration of the field
 - Pairs and free energy
 - The gap and the coherence length
 - Type I and type II
 - Abrikosov flux lattice
- Experimental examples
 - bulk isotropic case
 - anisotropic superconductors
 - LE muons
 - gap fits
 - Uemura plot
 - phase diagrams

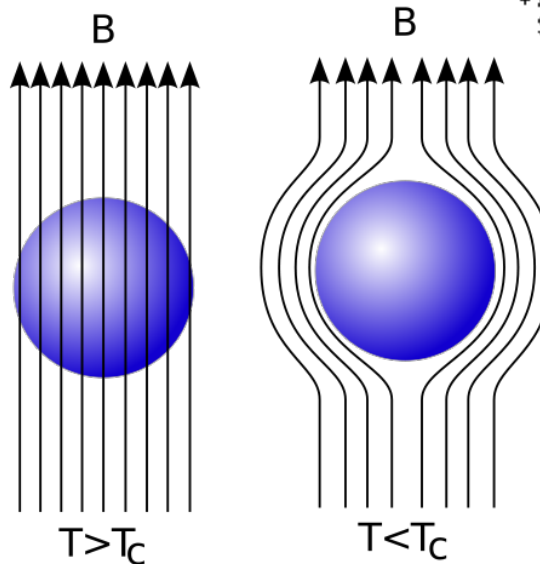


Meissner - Ochsenfeld effect

Shielding



Field expulsion:
cool a sample
below T_c



KNOWN SUPERCONDUCTIVE ELEMENTS

Legend:
 ■ BLUE = AT AMBIENT PRESSURE
 ■ GREEN = ONLY UNDER HIGH PRESSURE

KNOWN SUPERCONDUCTIVE ELEMENTS										KNOWN SUPERCONDUCTIVE ELEMENTS																									
										III A	IV A	V A	V I A	V II A																					
1	H											5	B	6	C	7	N	8	O	9	F	10	Ne												
2	Li	4	Be											13	Al	14	Si	15	P	16	S	17	Cl	18	Ar										
3	Na	12	Mg	III B	IV B	V B	V I B	V II B	VII	IB	IIB	31	Ga	32	Ge	33	As	34	Se	35	Br	36	Kr												
4	K	20	Ca	21	Sc	22	Ti	23	Y	24	Cr	25	Mn	26	Fe	27	Co	28	Ni	29	Cu	30	Zn	49	In	50	Sn	51	Sb	52	Te	53	I	54	Xe
5	Rb	38	Sr	39	Y	40	Zr	41	Nb	42	Mo	43	Tc	44	Ru	45	Rh	46	Pd	47	Ag	48	Cd	81	Tl	82	Pb	83	Bi	84	Po	85	At	86	Rn
6	Cs	56	Ba	*La	Hf	72	Ta	73	W	74	Re	75	Os	76	Ir	77	Pt	78	Au	79	Hg	80	Hg	81	Tl	82	Pb	83	Bi	84	Po	85	At	86	Rn
7	Fr	88	Ra	+Ac	Rf	104	Ha	105	106	107	108	109	110	111	112																				

SUPERCONDUCTORS.ORG

* Lanthanide Series

58	Ce	59	Pr	60	Nd	61	Pm	62	Sm	63	Eu	64	Gd	65	Tb	66	Dy	67	Ho	68	Er	69	Tm	70	Yb	71	Lu
----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----

+ Actinide Series

90	Th	91	Pa	92	U	93	Np	94	Pu	95	Am	96	Cm	97	Bk	98	Cf	99	Es	100	Fm	101	Md	102	No	103	Lr
----	----	----	----	----	---	----	----	----	----	----	----	----	----	----	----	----	----	----	----	-----	----	-----	----	-----	----	-----	----

<http://www.superconductors.org/Type1.htm>

Meissner-Ochsenfeld effect

London model: the penetration depth

A first lengthscale

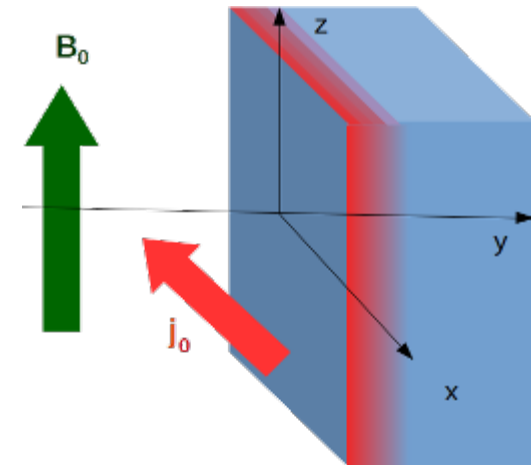
$$\lambda = \sqrt{\frac{m}{\mu_0 n e^2}}$$

Ampere Maxwell law

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{j}$$

Guess the solution

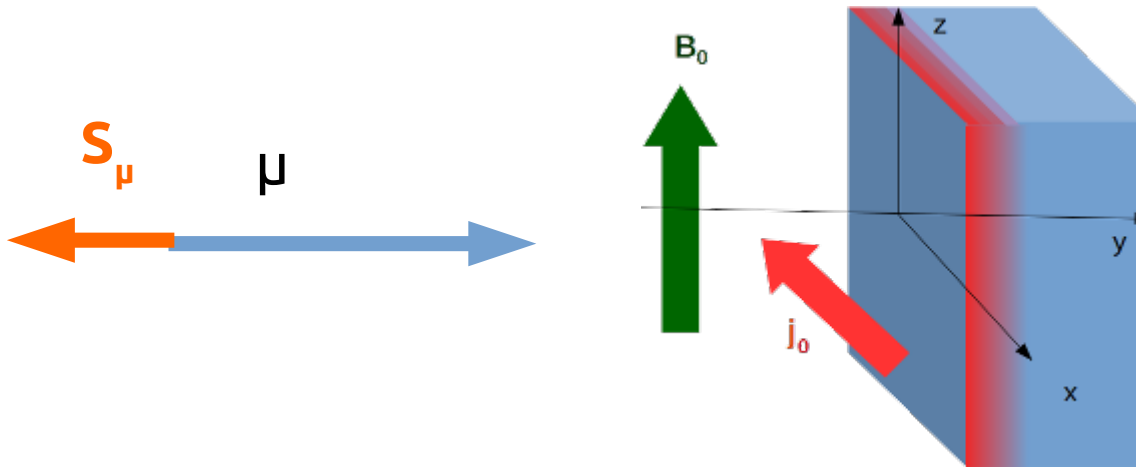
$$\mathbf{B} = B_0 e^{-y/\lambda} \hat{z}$$



Right!

$$\nabla \times \mathbf{B} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ \partial_x & \partial_y & \partial_z \\ 0 & 0 & B_0 e^{-y/\lambda} \end{vmatrix} = \underbrace{-\frac{B_0}{\lambda} e^{-y/\lambda} \hat{x}}_{\mu_0 \mathbf{j}}$$

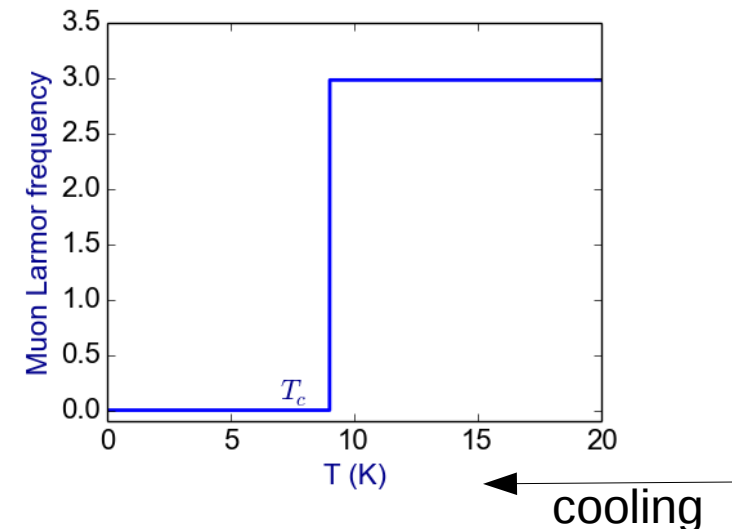
Imagine



Q1: Implant muons in a Meissner state superconductor. What do you detect?

Above T_c a precession

When cooling below T_c the precession disappears



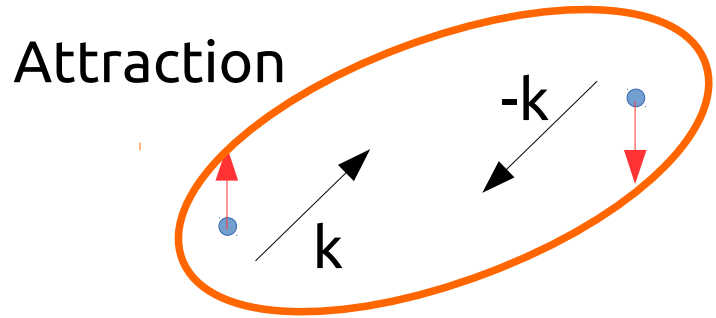
Summary of superconductor facts

- Only for $T < T_c$ (pretty low)
- Only below a critical field ($H < H_c$)
- Zero electrical resistance
- Magnetic field expulsion, requires a lengthscale

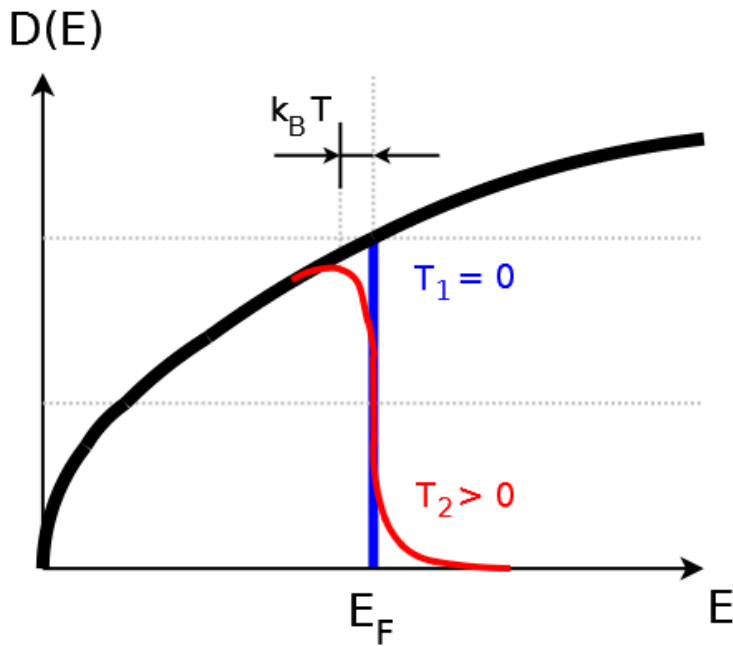
$$\lambda = \sqrt{\frac{m^*}{\mu_0 n e^2}}$$

How can this be explained?

Microscopic model Prototype: BCS



Cooper pair, compound boson
condensation energy (binding) Δ



normal metal

The Nobel Prize in Physics 1972



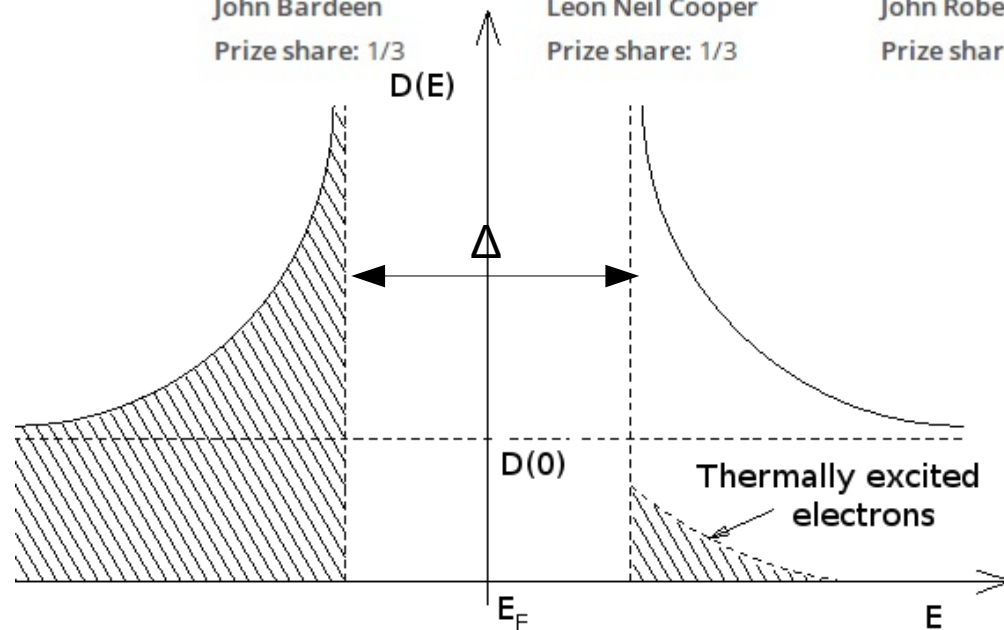
John Bardeen
Prize share: 1/3



Leon Neil Cooper
Prize share: 1/3



John Robert Schrieffer
Prize share: 1/3



Ginzburg-Landau

$$F - F_n = \alpha |\psi|^2 + \frac{\beta}{2} |\psi|^4$$

order parameter

magnetic free energy easy to add

$$F - F_n = \alpha |\psi|^2 + \frac{\beta}{2} |\psi|^4 + \frac{1}{2} m \left(\frac{j}{ne} \right)^2 + \frac{|\mathbf{B}|^2}{2\mu_0}$$

supercurrents $\hat{j} = \frac{e}{m} \hat{p} = \frac{e}{m} (-i\hbar \nabla - e\mathbf{A})$

The Nobel Prize in Physics 2003



Alexei A. Abrikosov
Prize share: 1/3



Vitaly L. Ginzburg
Prize share: 1/3

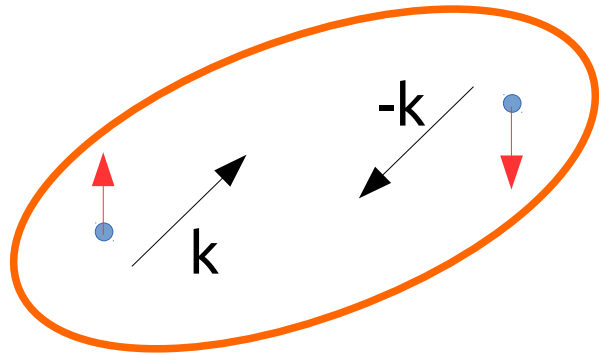


Anthony J. Leggett
1962



Lev Davidovich Landau
Prize share: 1/1

The gap: a second lengthscale



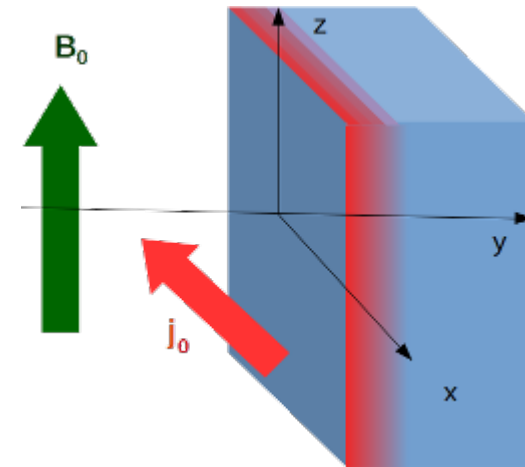
Cooper pair

Coherence length ξ

- how far can you pull a pair apart?

Inject an electron in a superconductor

- how far from the surface does it start to pair (feel the attraction)?



$$\xi = \frac{\hbar}{\sqrt{2m|\alpha|}}$$

- Ginzburg Landau definition

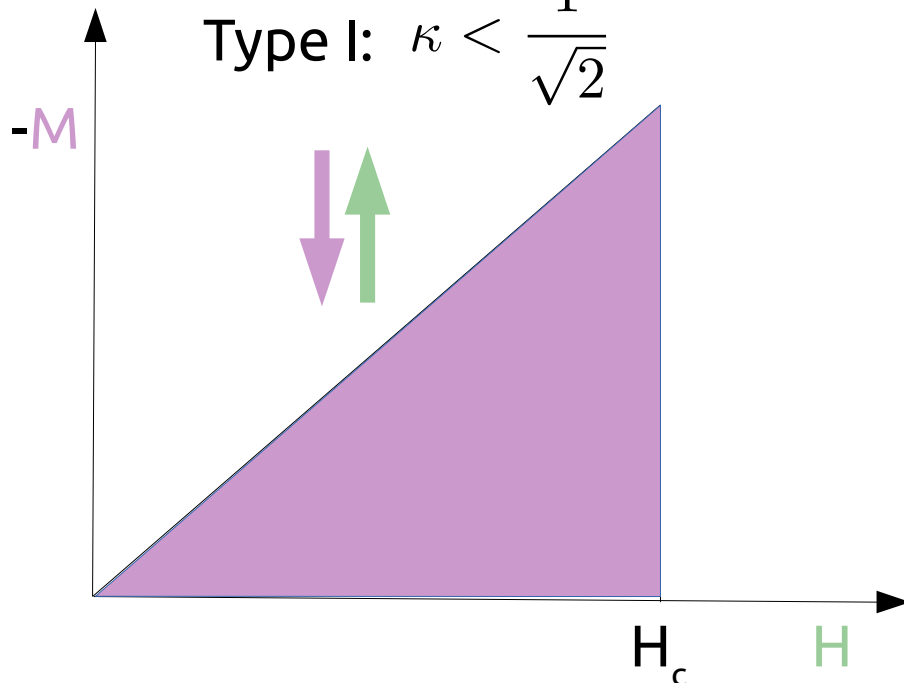
Type I and Type II superconductors

Ginzburg Landau parameter

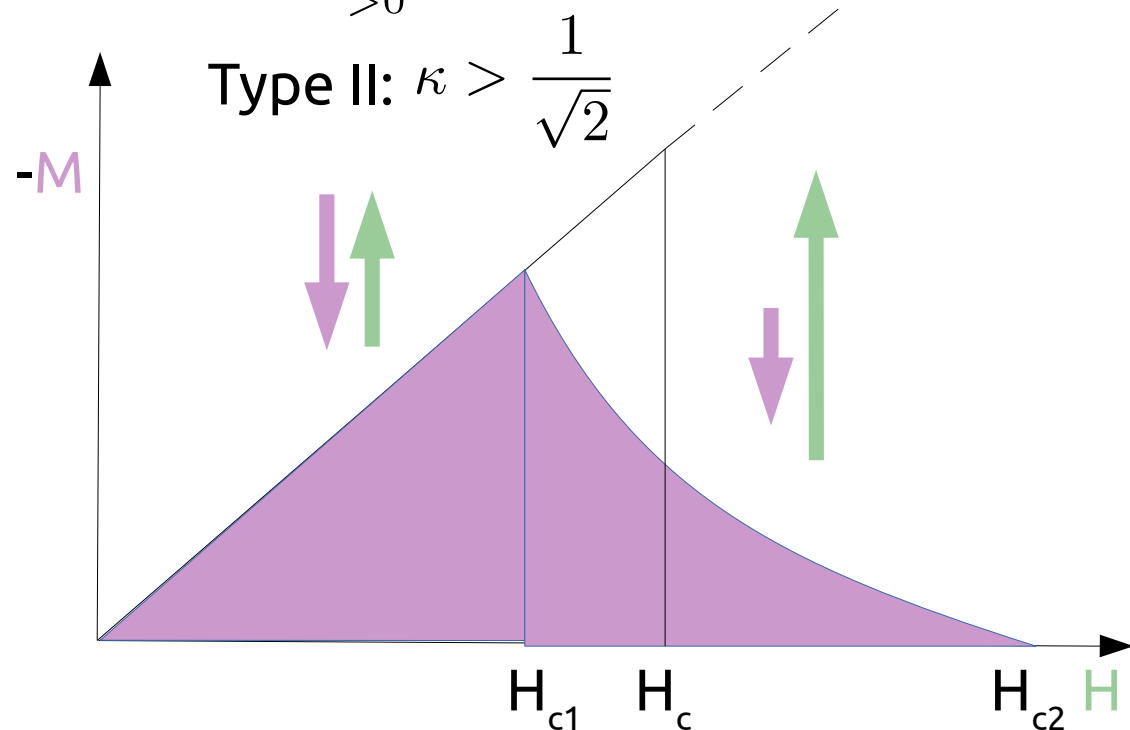
$$\kappa = \frac{\lambda}{\xi}$$

$$\Delta F = \underbrace{\alpha|\psi|^2 + \frac{\beta}{2}|\psi|^4}_{<0} + \underbrace{\frac{1}{2}m \left(\frac{j}{ne}\right)^2 + \frac{|\mathbf{B}|^2}{2\mu_0}}_{>0}$$

Type I: $\kappa < \frac{1}{\sqrt{2}}$

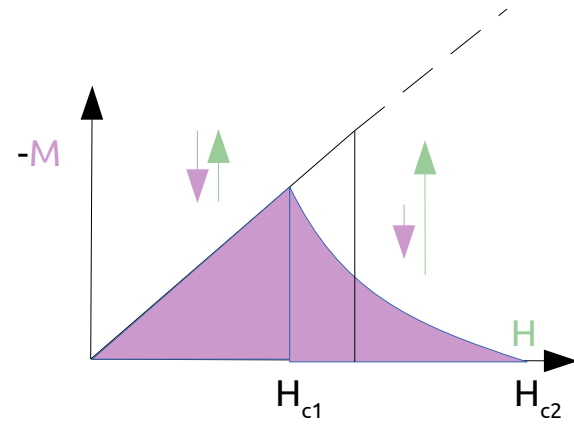


Type II: $\kappa > \frac{1}{\sqrt{2}}$



Abrikosov flux lattice

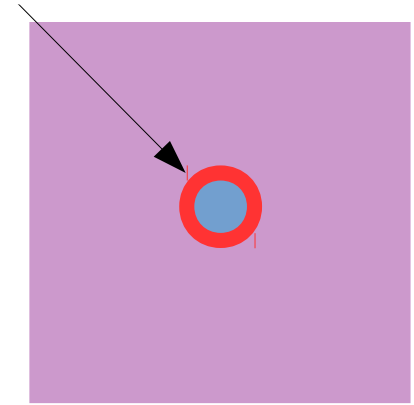
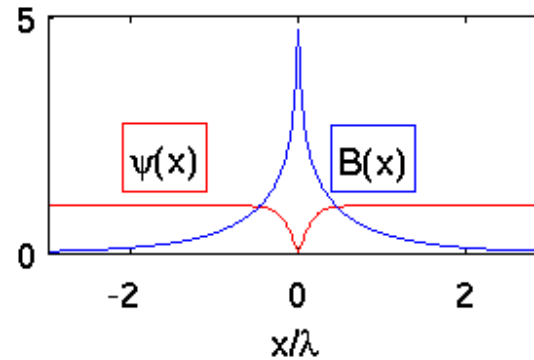
magnetic flux quantum $\Phi_0 = \frac{h}{2e} = 2.07 \cdot 10^{-15} \text{ Wb}$



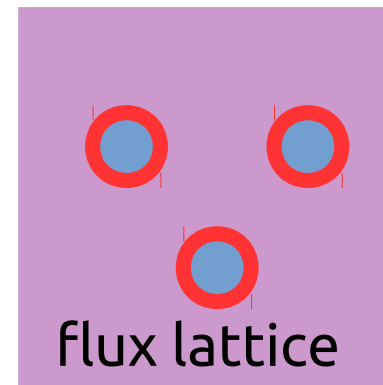
$H > H_{c1}$ partial field penetration

for $\kappa > \frac{1}{\sqrt{2}}$
periodic solution
of GL equations

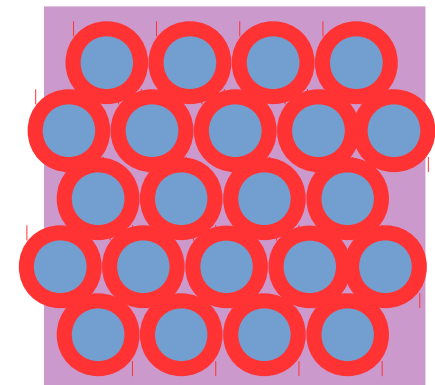
$H = H_{c1}$



$H > H_{c1}$

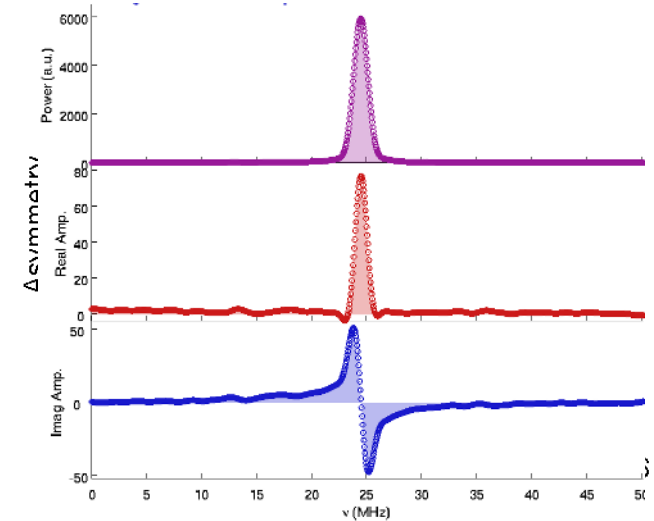
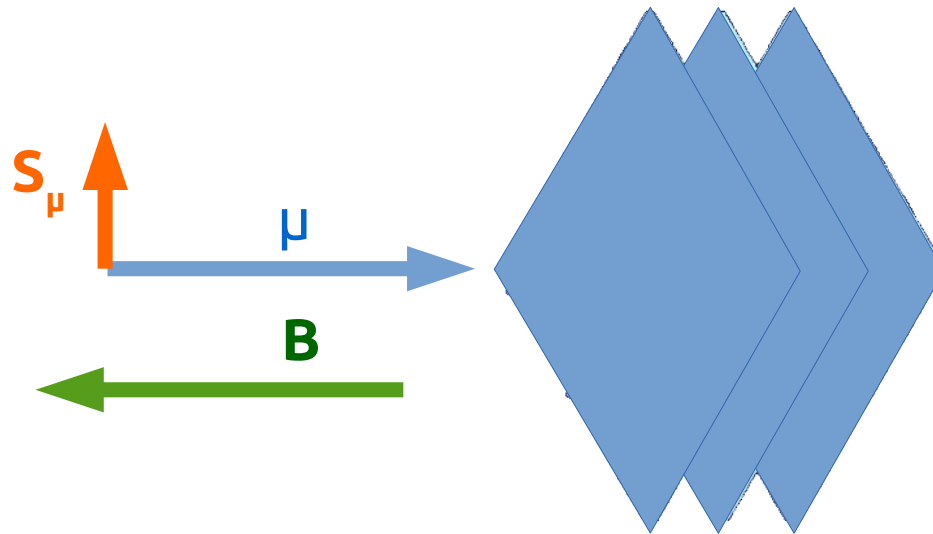


$\Delta F = 0$

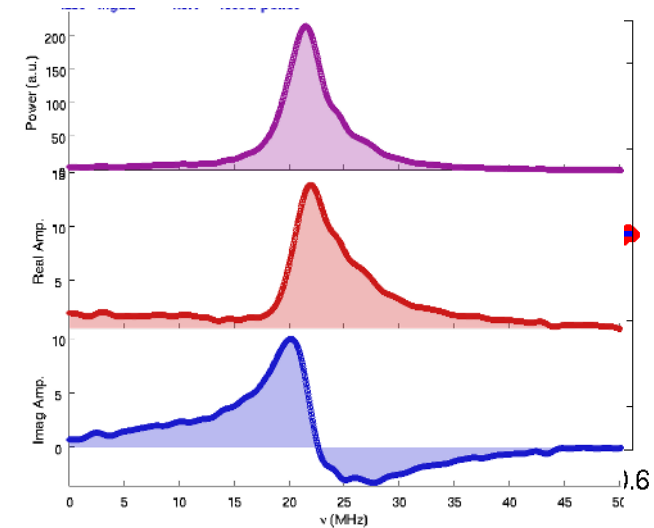
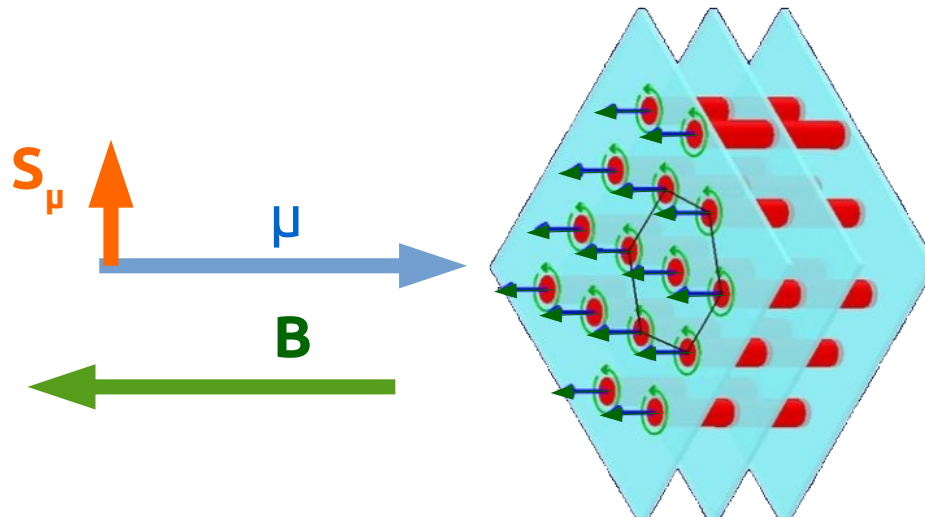


$H = H_{c2}$

Imagine

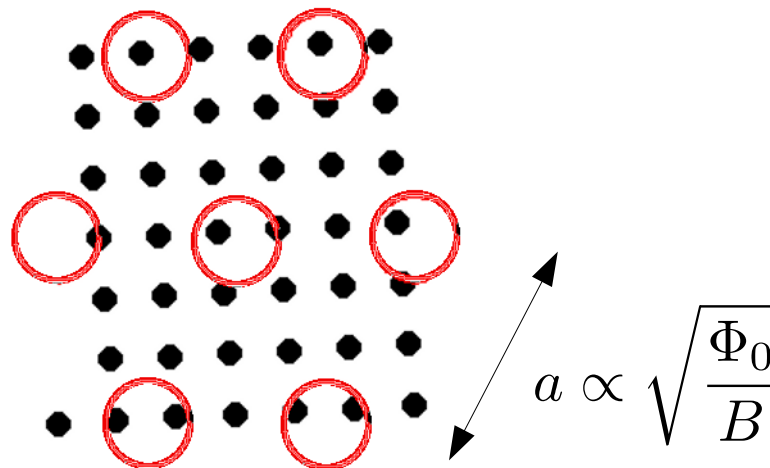


Q2: Homogeneously implant muons in a bulk FL. What do you expect to measure?



Field distribution in the FL

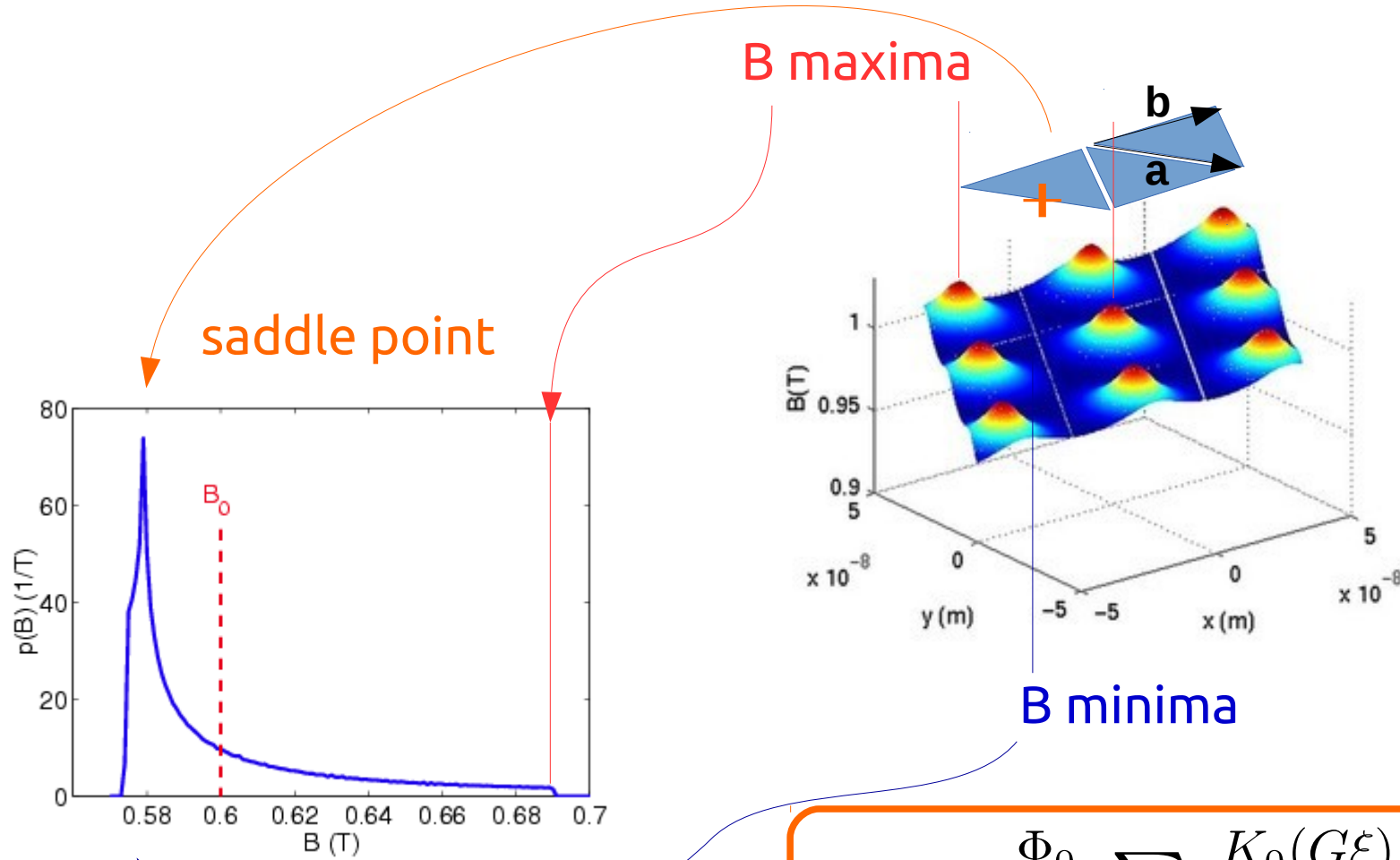
- the Flux Lattice is incommensurate to the crystal lattice



- whereas muons are interstitials in the crystal lattice
- dense random sampling

Field distribution in the FL

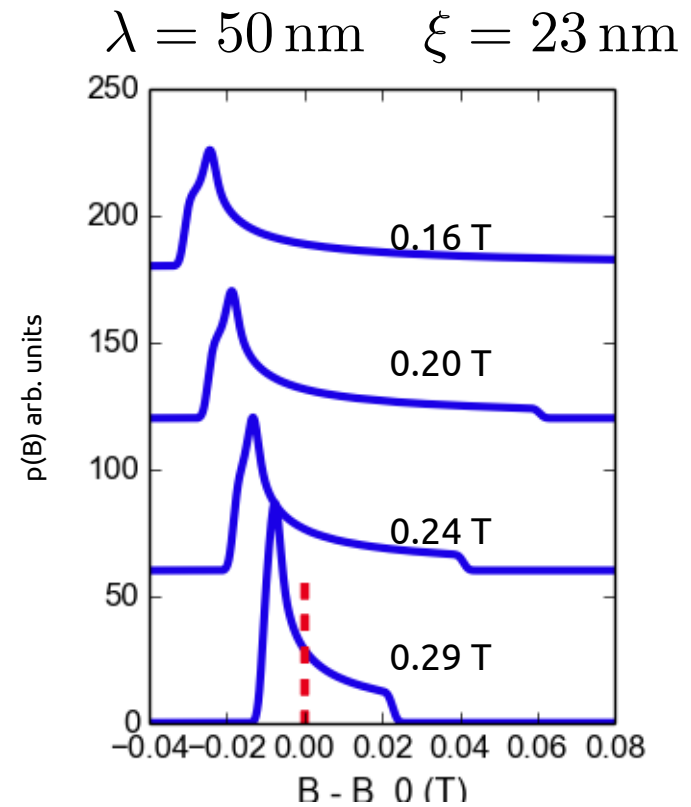
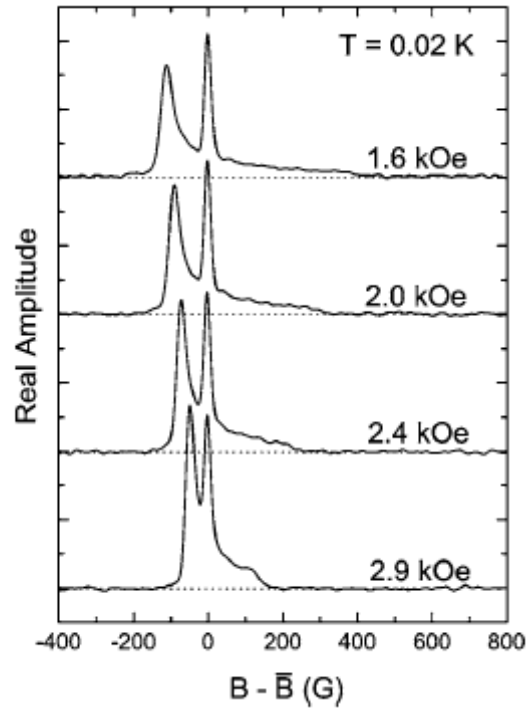
- GL equations predict



$$B(\mathbf{r}) = \frac{\Phi_0}{\mathbf{a} \cdot \mathbf{b}} \sum_{\mathbf{G}} \frac{K_0(G\xi)}{1 + G^2 \lambda^2} e^{i\mathbf{G} \cdot \mathbf{r}}$$

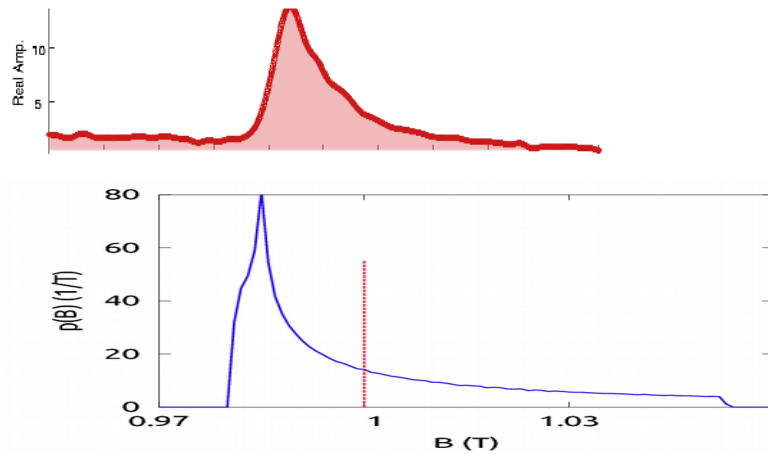
Experimental case Vanadium

M. Laulajainen PHYSICAL REVIEW B 74, 054511 (2006)



Quick and dirty multigaussian fit

Comparison with polycrystal data

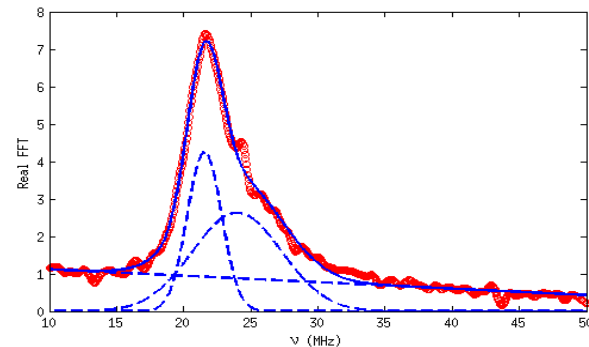


$$B(r) \otimes \exp\left(-\frac{r^2}{2\sigma^2}\right)$$

is it worth while?

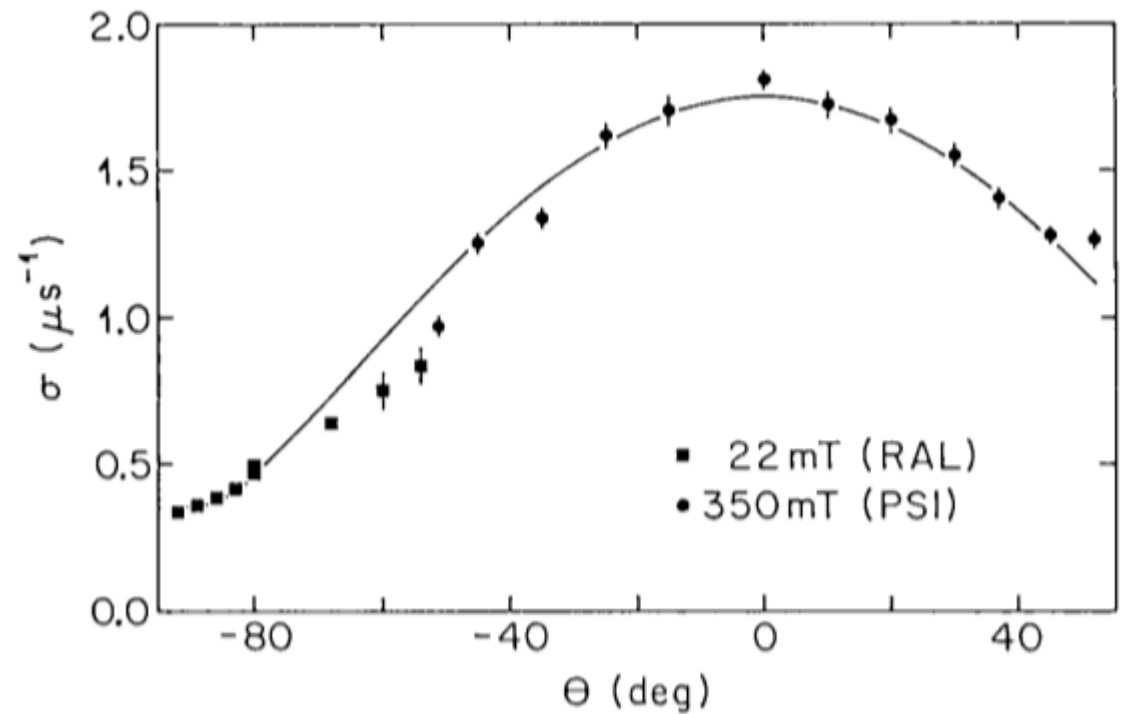
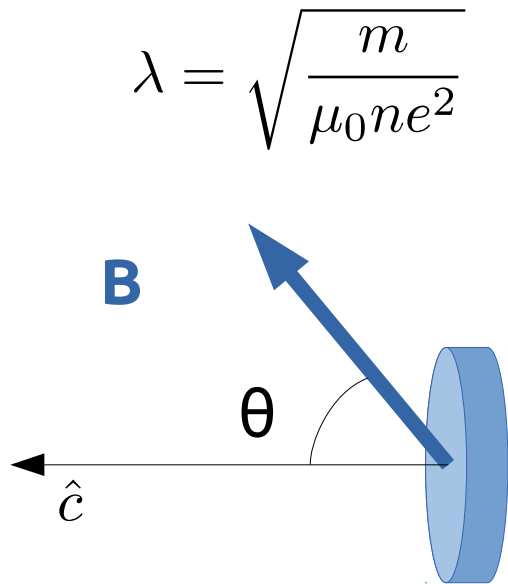
Second moment

$$\langle \Delta B^2 \rangle = \left(\frac{\Phi_0}{\mathbf{a} \cdot \mathbf{b}} \right)^2 \sum_{\mathbf{k} \neq 0} \frac{K_0^2(k\xi)}{(1 + \underbrace{k^2 \lambda^2}_{k\lambda > 1})^2} \propto \frac{1}{\lambda^4}$$



$$\sigma = \gamma_{\mu} \sqrt{\langle \Delta B^2 \rangle} \propto \frac{1}{\lambda^2}$$

Anisotropic penetration



$$\begin{bmatrix} m_a & 0 & 0 \\ 0 & m_a & 0 \\ 0 & 0 & m_a c \end{bmatrix} \rightarrow \begin{bmatrix} \lambda_{ac} & 0 & 0 \\ 0 & \lambda_{ac} & 0 \\ 0 & 0 & \lambda_{aa} \end{bmatrix}$$

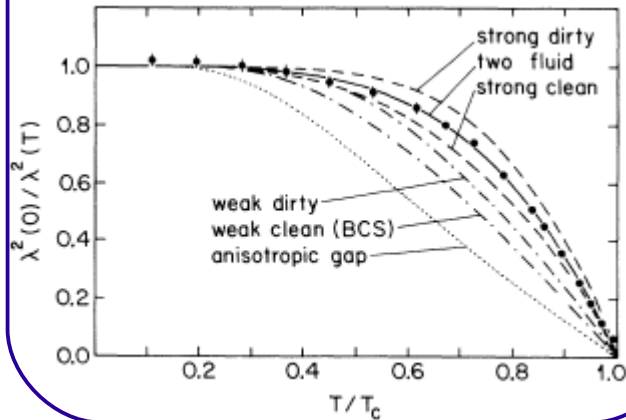
$$\sigma \propto \frac{1}{\lambda_{ac} \lambda_{aa}} \left[\sin^2 \theta + \left(\frac{\lambda_{ac}}{\lambda_{aa}} \right) \cos^2 \theta \right]$$

E.M. Forgan *et al.* Hyperfine Interactions 63, 71

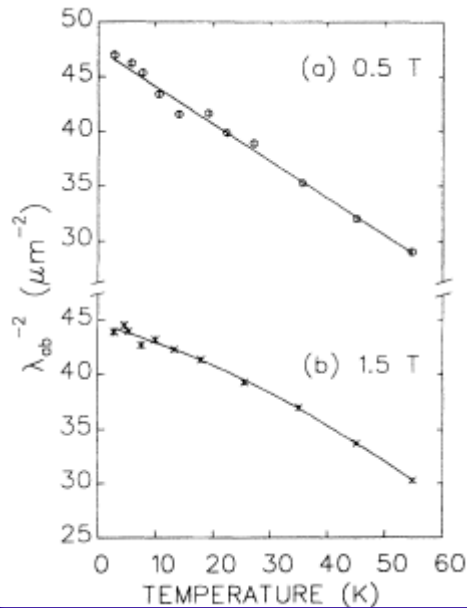
$\sigma(T)$: gap fits

YBCO_{6.95} powders (!)

B. PÜMPIN *et al.* PRB42 8019 (1990)



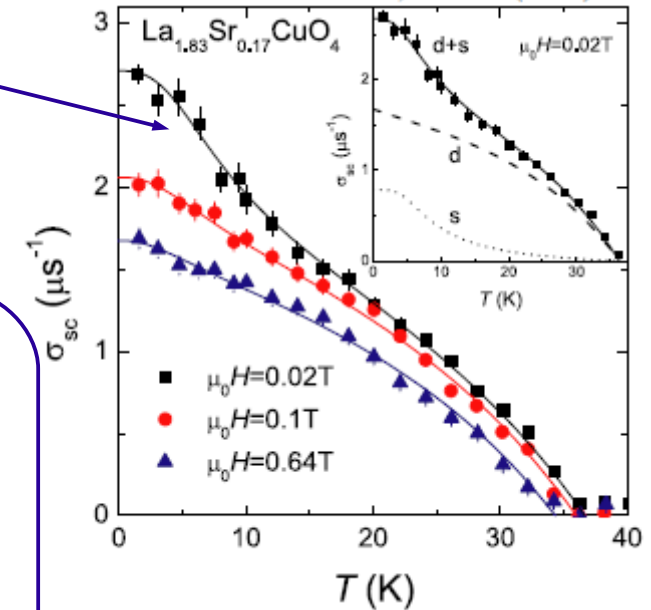
d-wave: lines of nodes



s-wave n_s

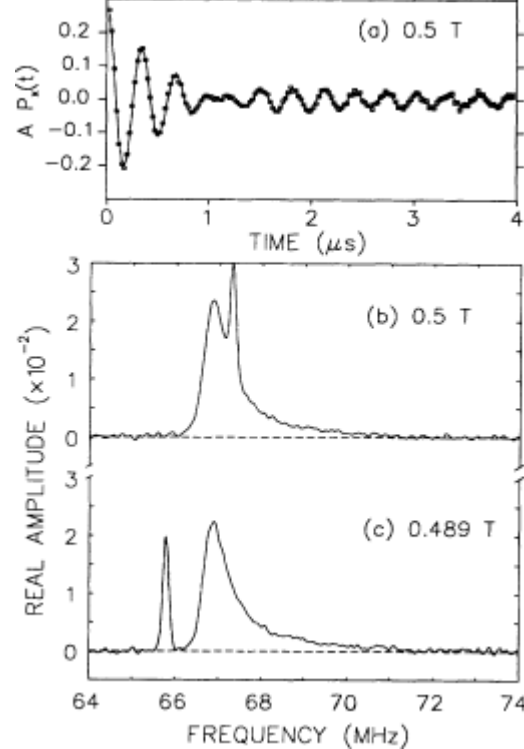
La_{1.83}Sr_{0.17}CuO₄ crystal

R. Khasanov, PRL 98, 057007 (2007)



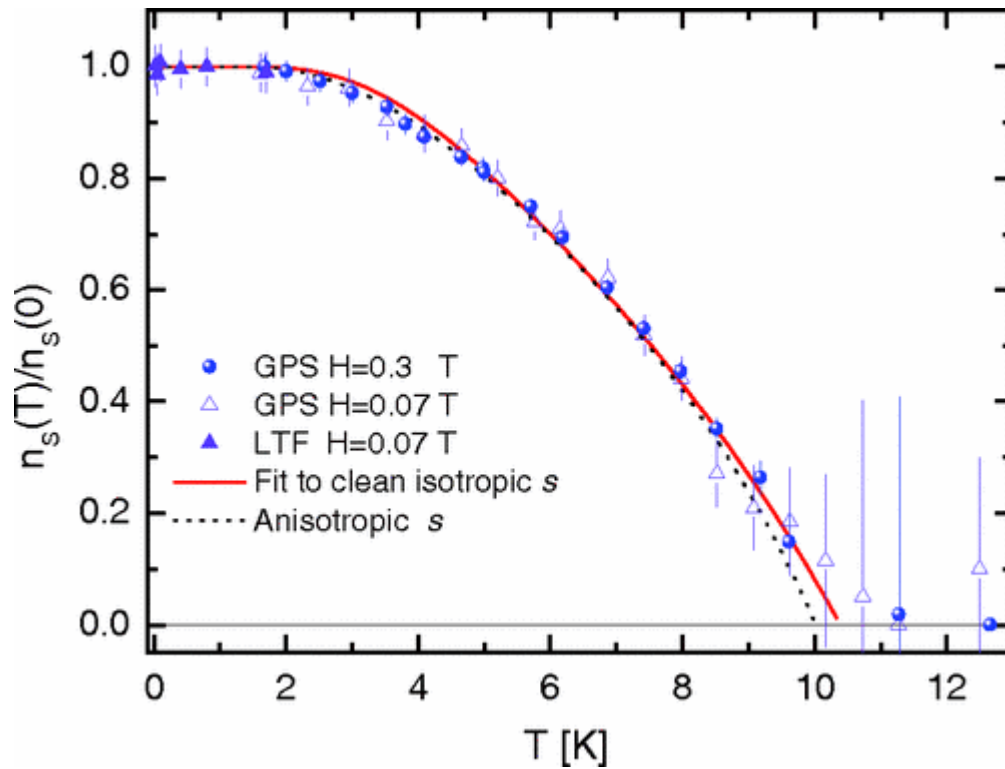
YBCO_{6.95} crystal

PHYSICAL REVIEW B, VOLUME 65, 094512



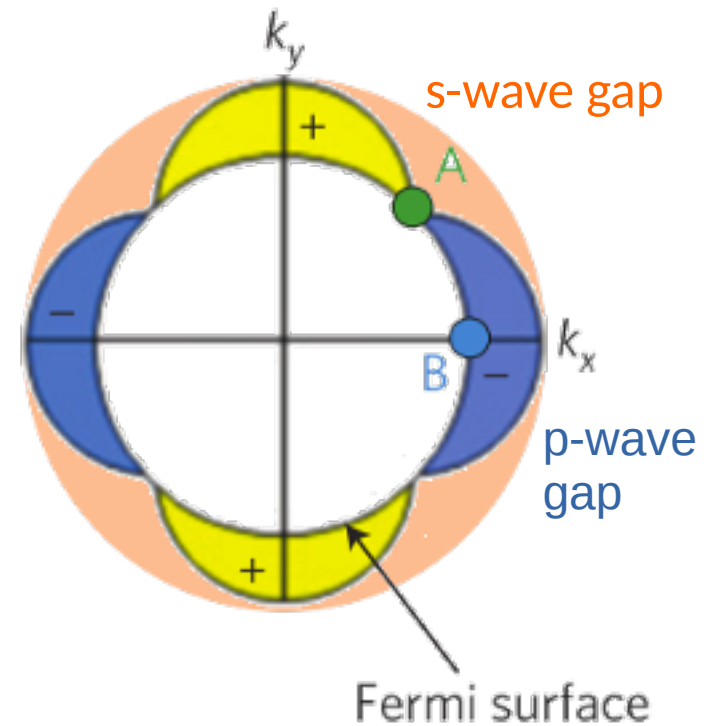
Field cool, then
shift field down
(pinned flux lattice)

BiS₂ ≈ CuO₂: conventional or unconventional superconductor?

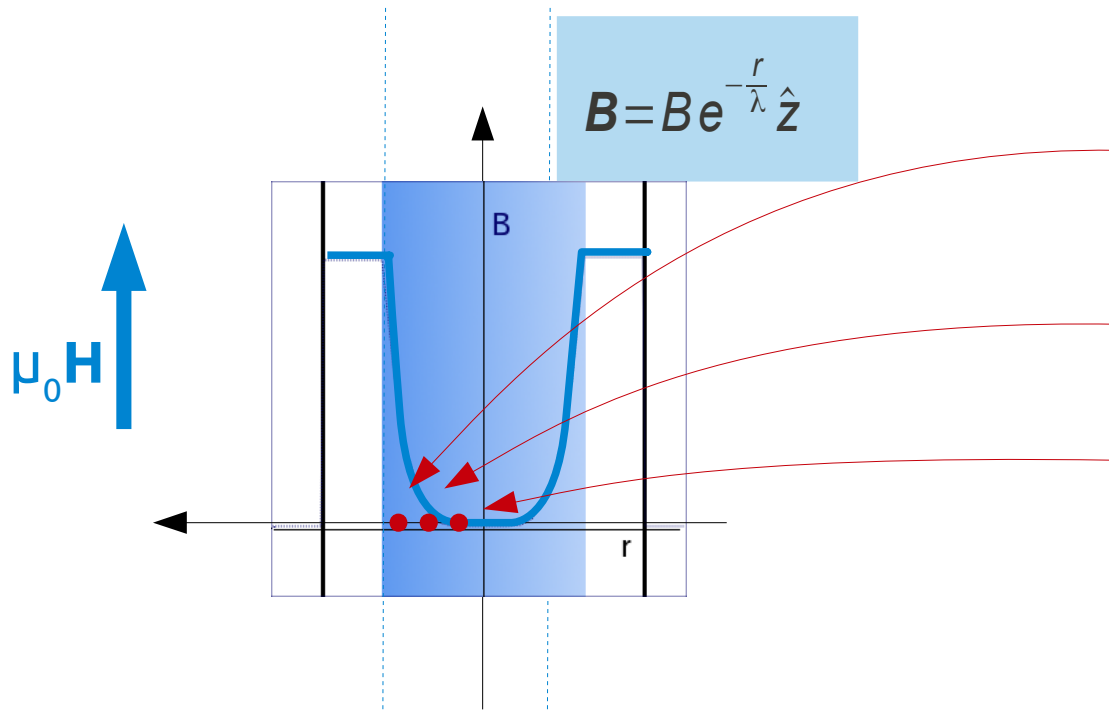


s-wave, not d-wave

gap, i.e cost to break a Cooper pair

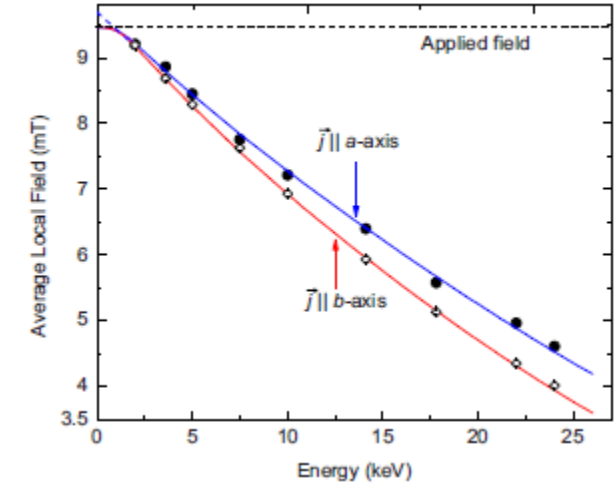
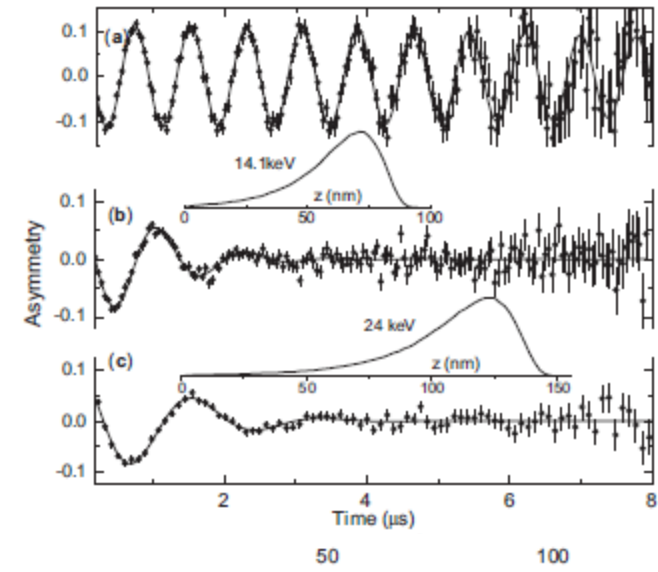


Low Energy muons London penetration depth



Field parallel to the surface
decays exponentially with
a penetration depth λ

Single crystal $\text{YBa}_2\text{Cu}_3\text{O}_{6.92}$



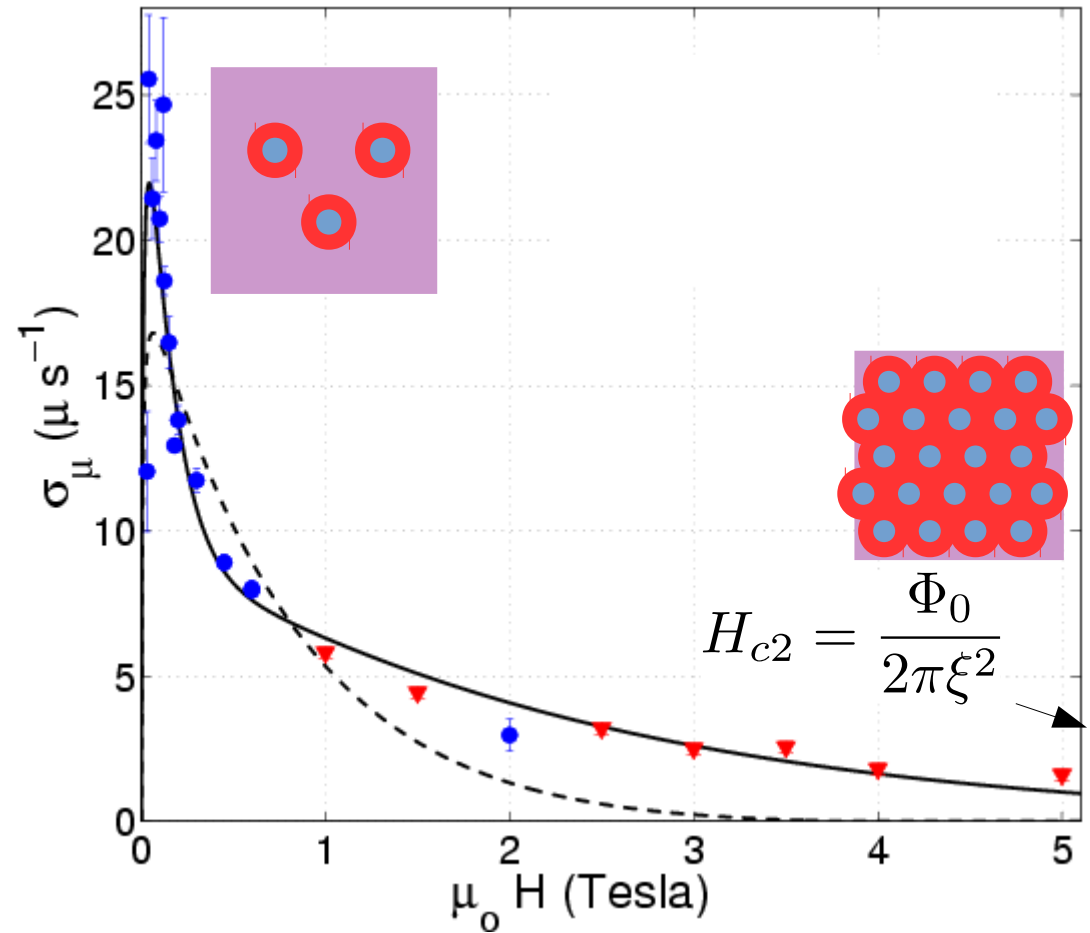
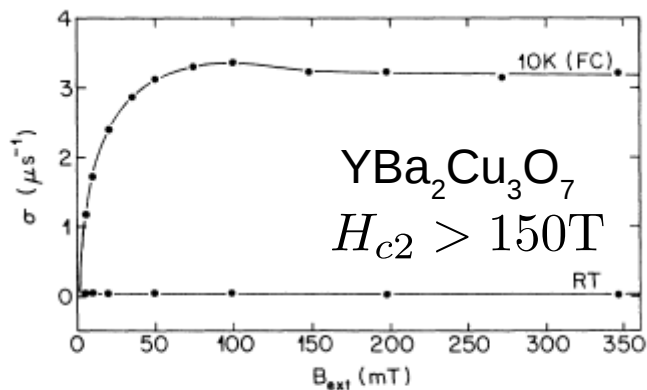
R. Kiefl et al. PRB 81 180502 (2010)

MgB₂: two gaps

$$\sigma_\mu = \gamma_\mu \sqrt{\langle \Delta B^2 \rangle}$$

$$\propto \frac{1}{\lambda^2} = \frac{\mu_0 n_s e^2}{m}$$

B. PÜMPIN *et al.* PRB42 8019 (1990)



S. Serventi Phys. Rev. Lett. 93 217003

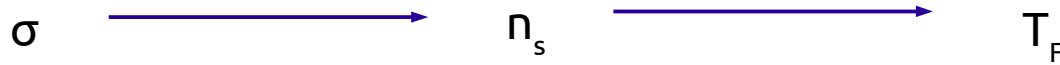
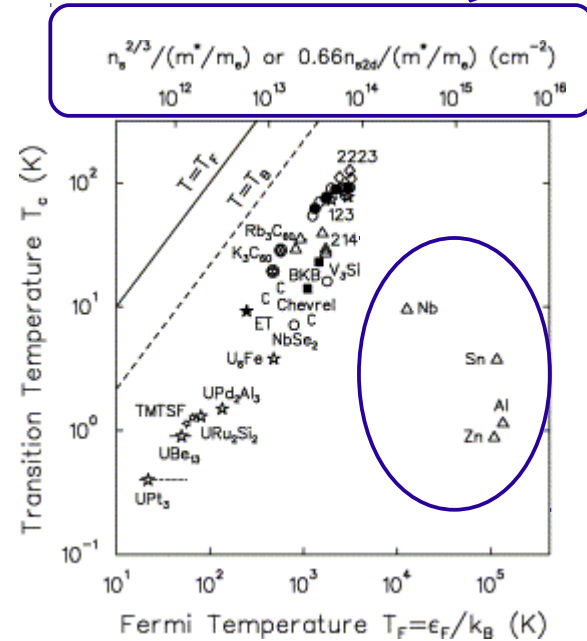
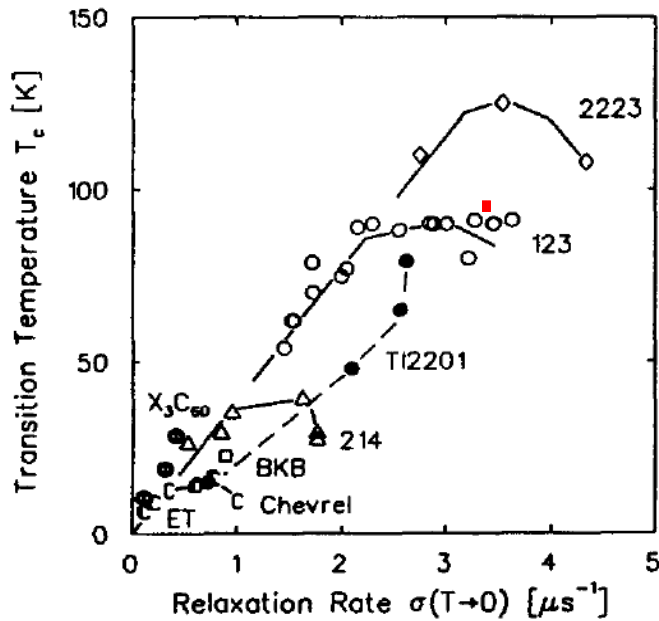
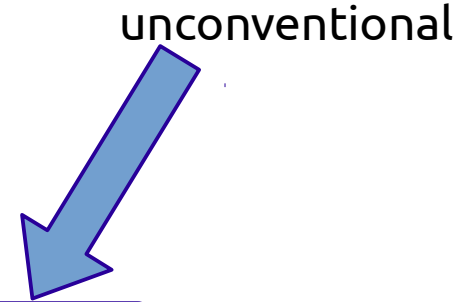
FIG. 2. Depolarization rate σ as a function of the external field B_{ext} (FC) for a sintered YBa₂Cu₃O_x sample at 10 K and at room temperature (RT), respectively. The lines are guides to the eye.

Uemura plot

At T=0:
$$\sigma_{\mu} = \gamma_{\mu} (\langle B^2 \rangle - \langle B \rangle^2)^{\frac{1}{2}} \propto \frac{1}{\lambda^2} \propto \frac{n_s}{m^*}$$

Y.J Uemura et al. Phys Rev Lett. 62, 2317 (1989) **500 cit.**

Y.J Uemura et al. Phys Rev Lett. 66, 2665 (1991) **300 cit.**



Phase diagrams

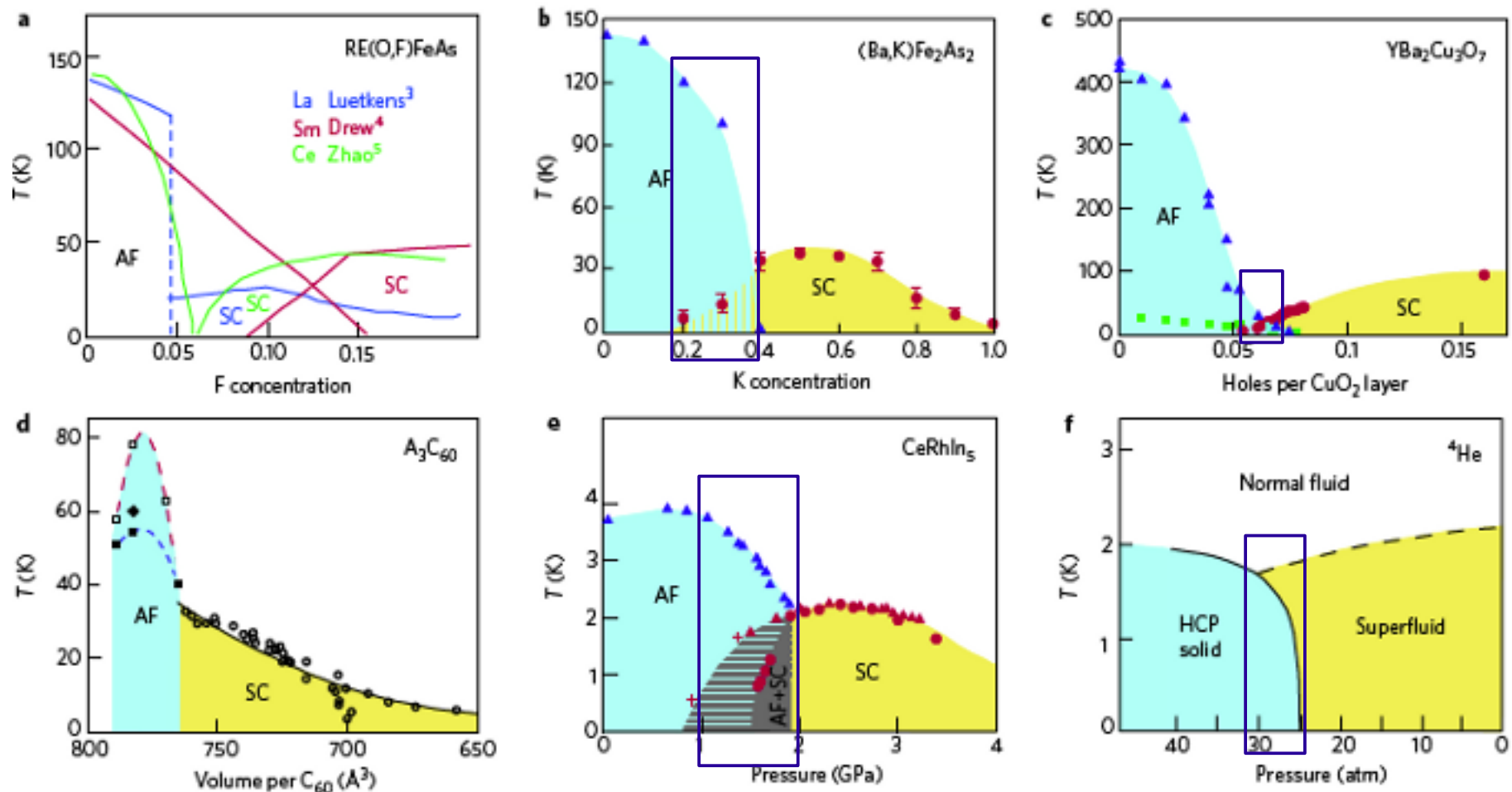
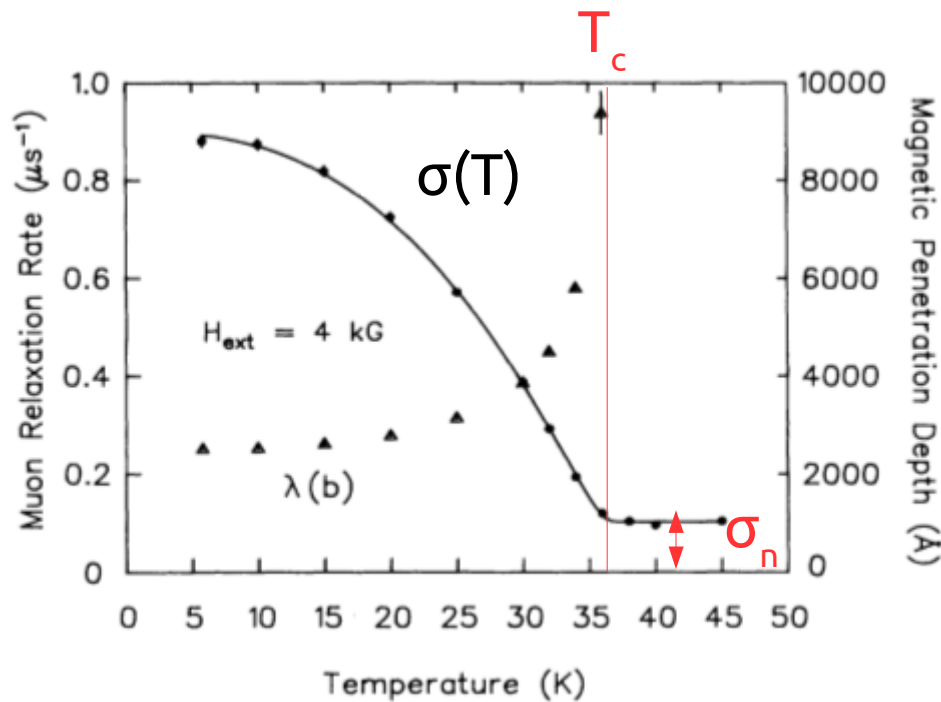


Fig. 11.1 Examples of phase diagrams showing a commonalities of unconventional superconducting compound [Uem09]
 c. YBaCuO_{6+x}, is from S. Sanna Phys Rev Lett. 93 207001 (2004)

Y.J. Uemura Nature Materials 8 253 (2009)

Imagine



Q3: How do we subtract the nuclear relaxation rate σ_n ?

In quadrature:
$$\gamma_\mu^2 \langle \Delta B^2 \rangle_\mu = \gamma_\mu^2 \langle \Delta B^2 \rangle_{FL} + \sigma_n^2$$

Recap

- Muons map the internal field distribution
- Two length scales, λ (currents, fields) and ξ (gap, wave function)
- Refined model (full distribution) for single crystal studies
- Rough model (second moment) for comparative studies
- $\sigma(T) \propto \lambda^{-2}(T)$: gap(s), symmetries
- coexistence with magnetism

That's it ...