

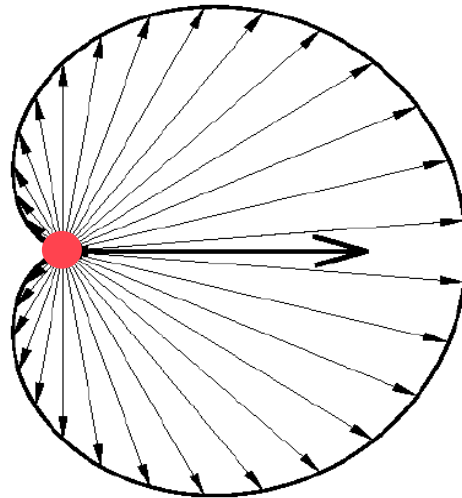
# Computer Simulations for Interpreting $\mu$ SR Experiments: Beyond DFT

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**ISIS Muon Group, STFC**



**1**

**Where is the moon? What have been tried and how we could complement it. Our version of the UEP method.**

**2**

**DFT combined with Ab Initio Random Searching and Machine Learning.  
Some examples**

**3**

**How to accelerate High Throughput Calculations: CASTEP vs DFT+.**

**4**

**Conclusions. Work in progress. Future plans.**

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## EXPERIMENTAL APPROACH

• Muonated Fe: follow the evolution of the muon frequency shift in a transverse field experiment as a function of the applied stress in a single Fe crystal (PRB **32**, 293, 1985).

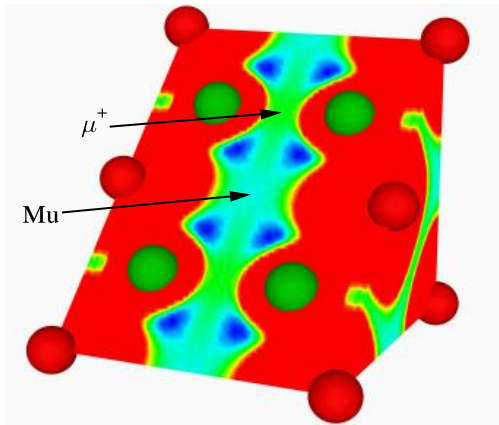
## COMBINED THEORETICAL / EXPERIMENTAL APPROACH

• Muonated LiF and Cu(py<sub>z</sub>)(NO)<sub>3</sub>: the theoretical calculations are used for testing different potential muon stopping sites.

## THEORETICAL APPROACH?

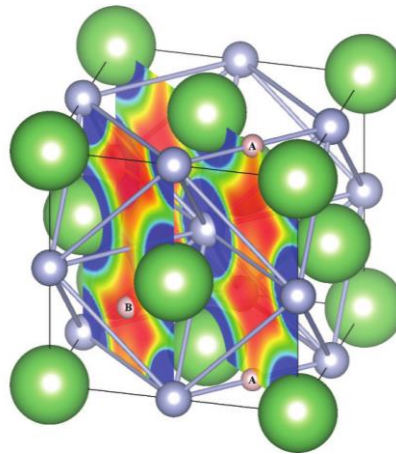
• Analysis of the DFT's electrostatic potential of the bulk material. This is known as the **Unperturbed Electrostatic Potential Method (UEP)**

$\mu^+$  and  $\mu^+e^-$  in CaF



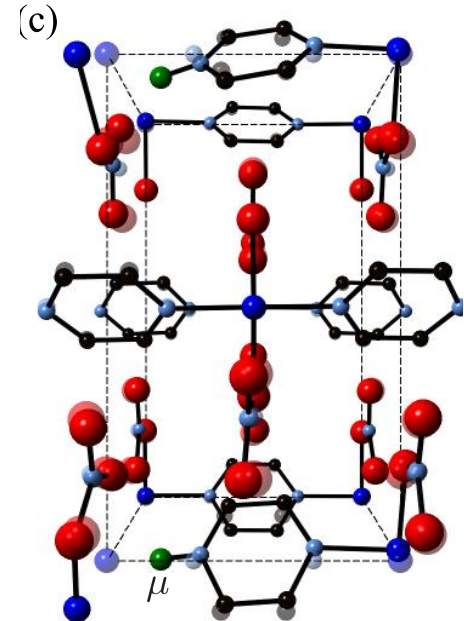
PRB **87**, 121108(R) (2013)

$\mu^+$  in YF<sub>3</sub>



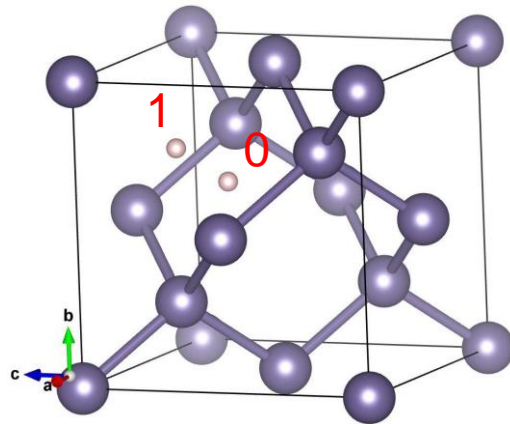
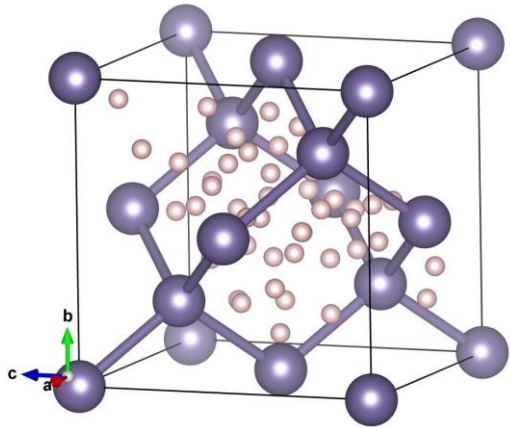
PRB **87**, 115148 (2013)

$\mu^+$  and  $\mu^+e^-$  in Cu(py<sub>z</sub>)(NO)<sub>3</sub>



PRB **91**, 144417 (2015)

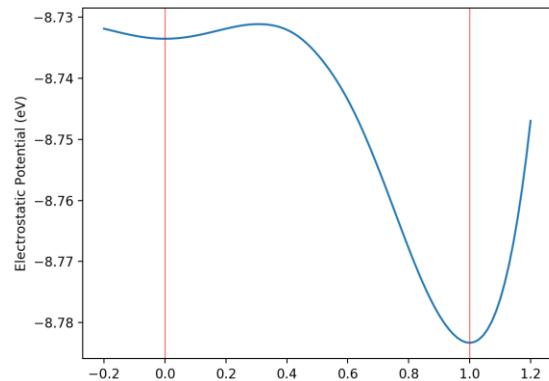
Ge



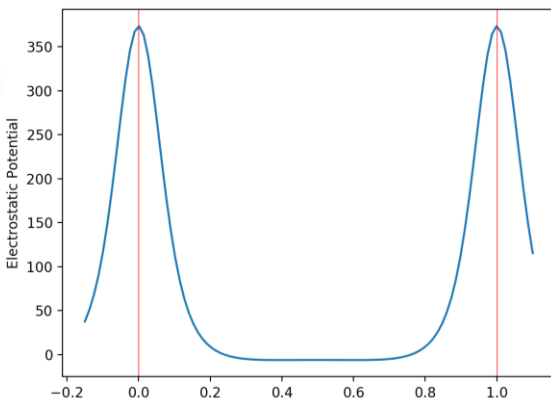
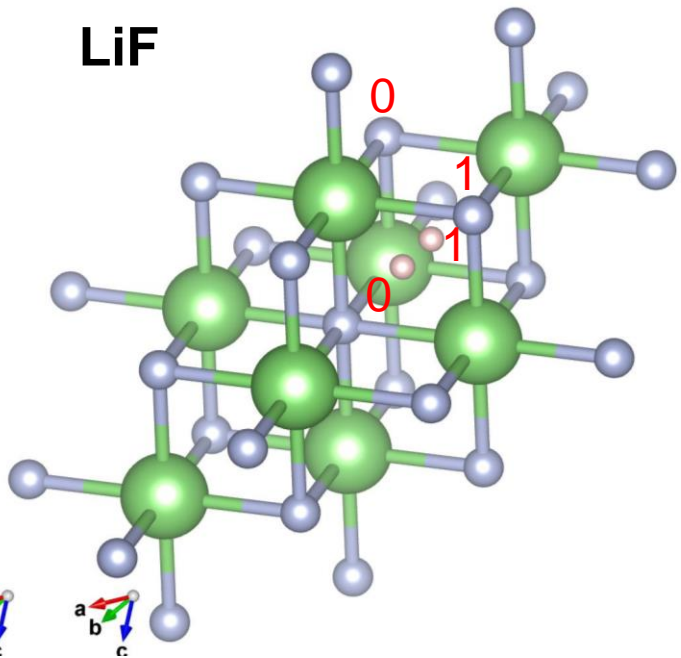
- Calculate electrostatic potential of unperturbed host material using DFT
- Randomly locate  $\mu^+$  in the host's unit cell (Ge in example)

- Calculate classical forces on the  $\mu^+$ .
- Relax  $\mu^+$  to the potential minima. Identify clusters.
- Create supercell and test sites.

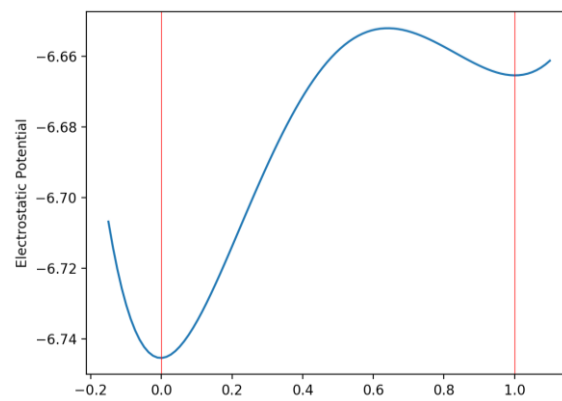
- Plot potential along the line joining 0-1.
- 1 is more likely to be a stopping site.



# LiF

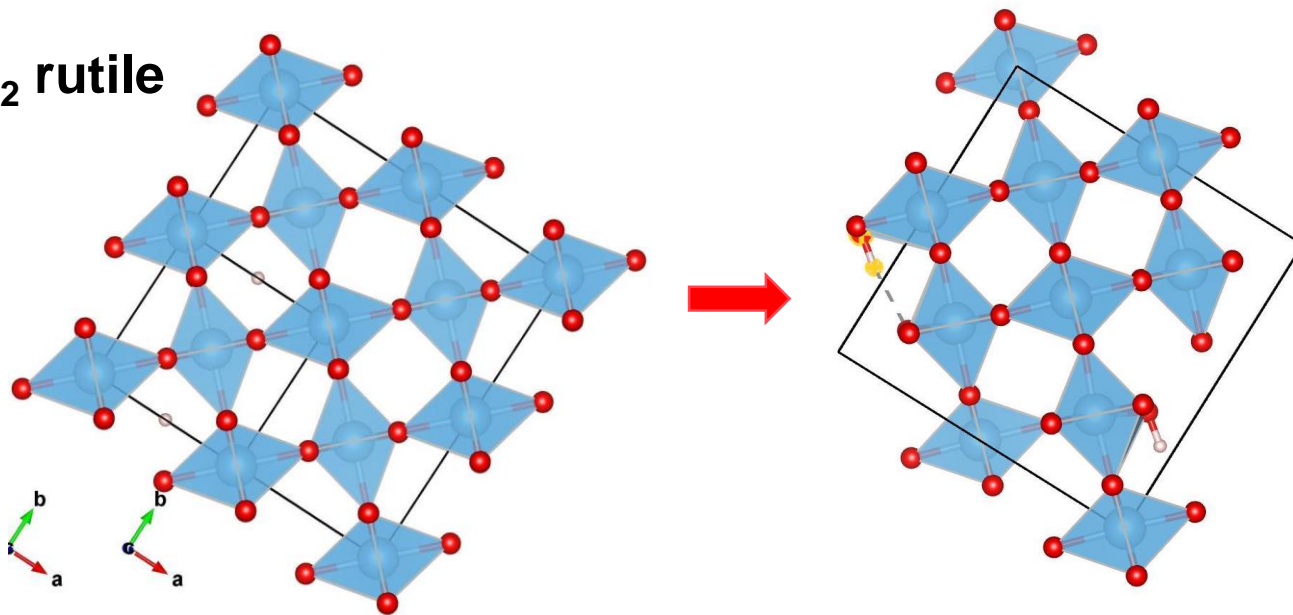


F-F potential



Mu-Mu potential

# TiO<sub>2</sub> rutile



Testing on:

- KCl
- CdS
- ZnO
- MgO
- GaAs
- (Thomas Dack)**

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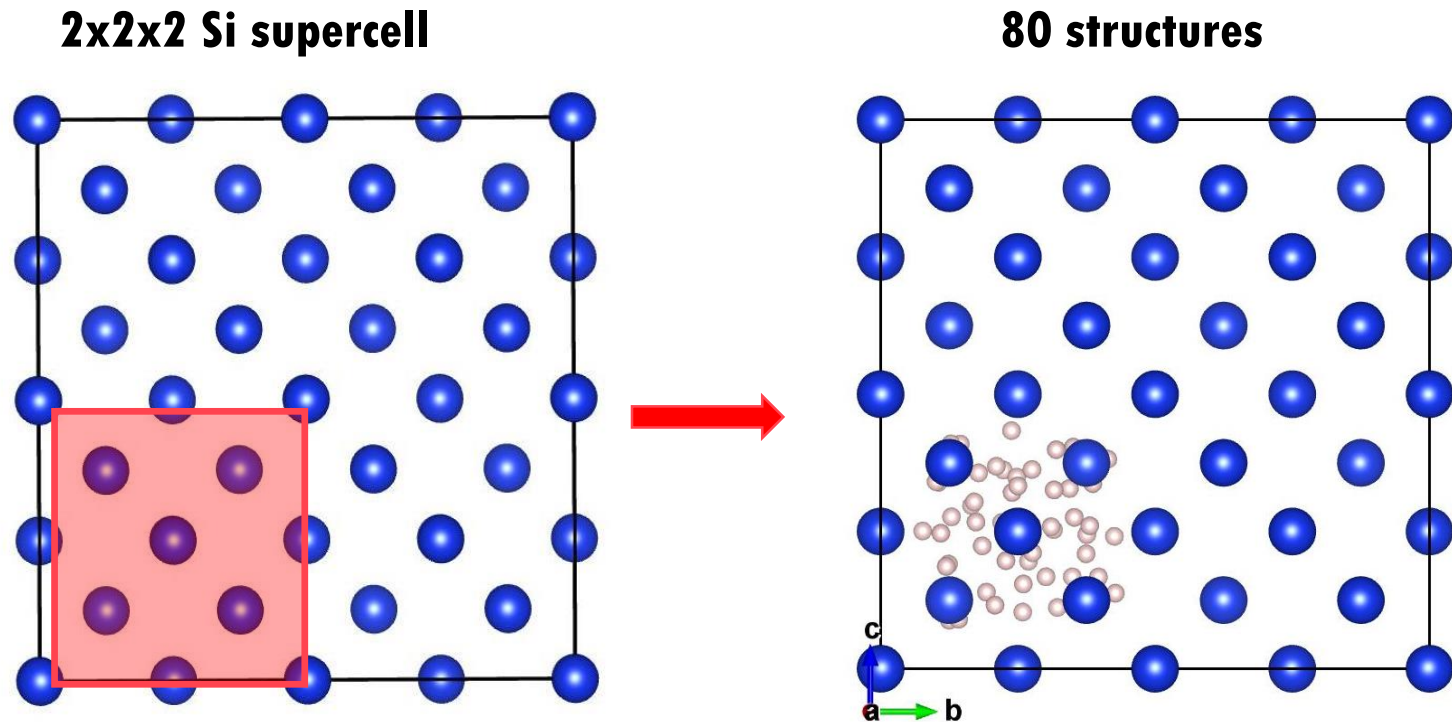
**3**

How to accelerate High Throughput Calculations: CASTEP vs DFT+.

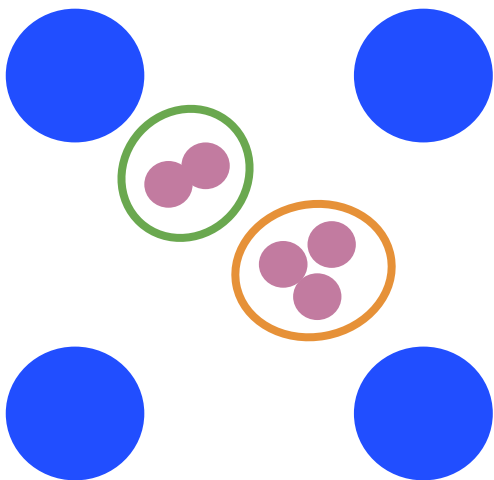
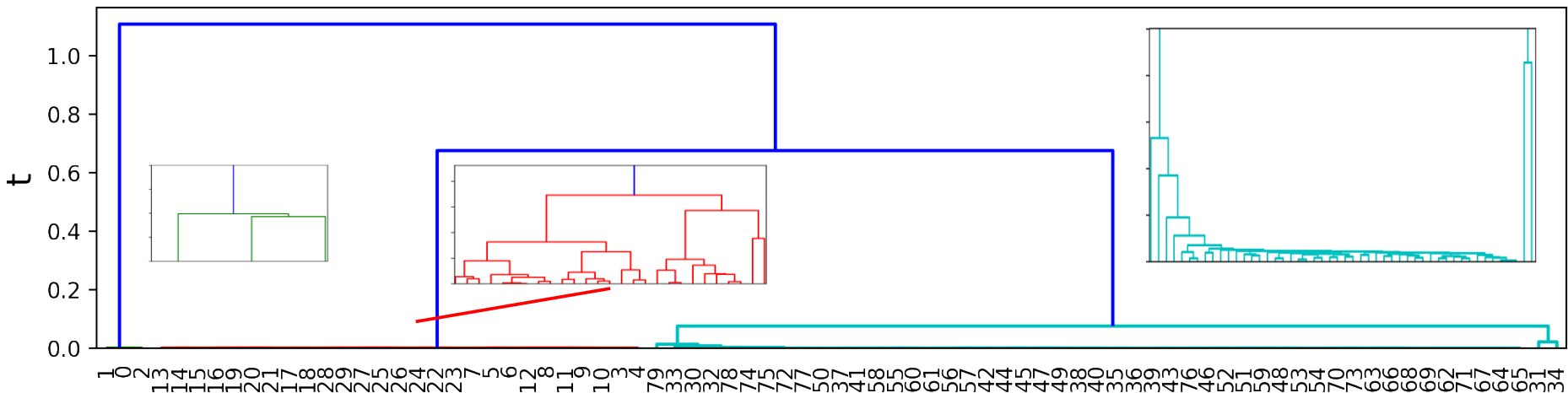
**4**

Conclusions. Work in progress. Future plans.

- 1) **Build 2x2x2 Si supercell**
- 2) **Define region to randomly locate muonium pseudo-atoms**
- 3) **Generate muonated structures placing muonium in randomised positions within the chosen region**
- 4) **Relax structures using calculated DFT forces**



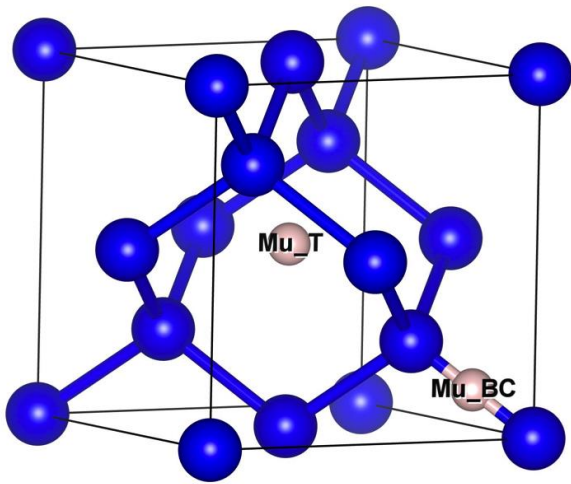
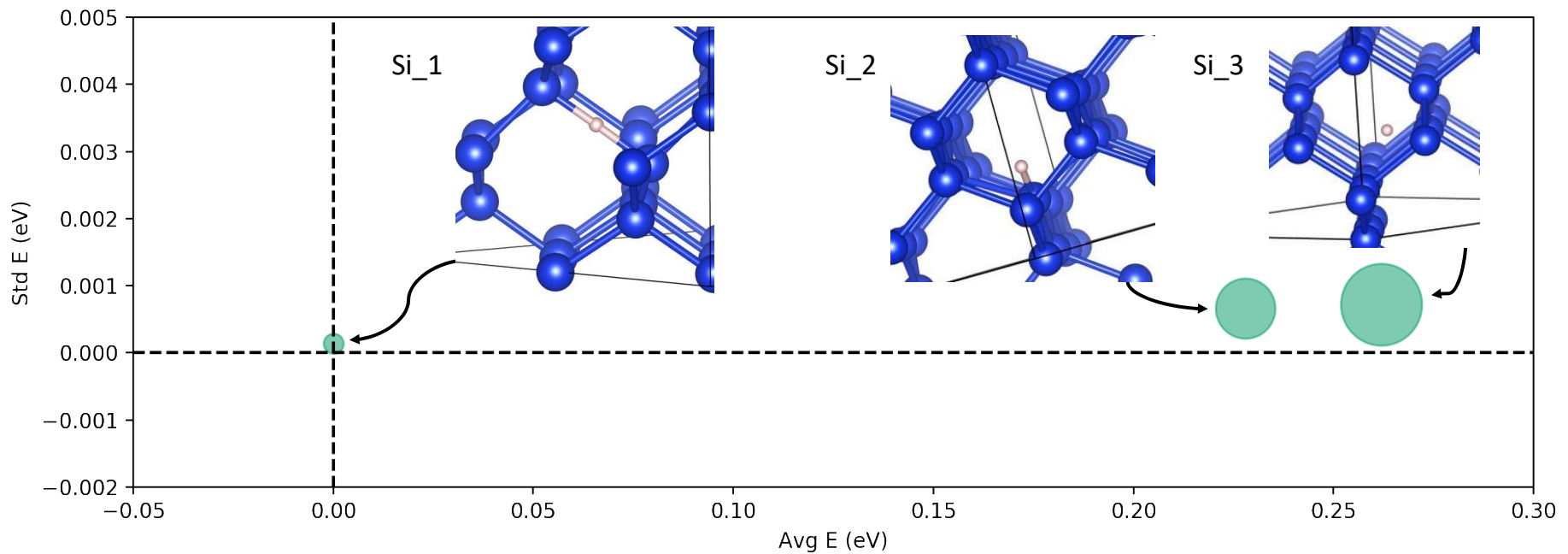




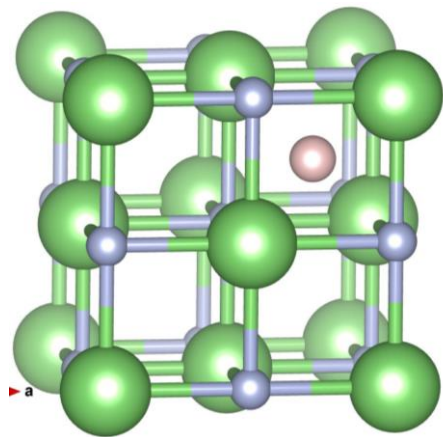
- **Define  $n$ D vector:  $(E_T, Q_1, Q_2, Q_3, \dots)$**
- **Look for “closeness” in  $n$ D space**
- **Hierarchical clustering**
- **3 clusters identified**



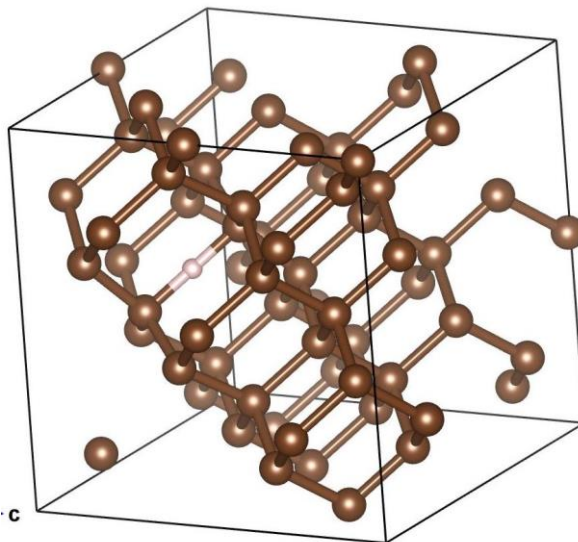
SOPRANO



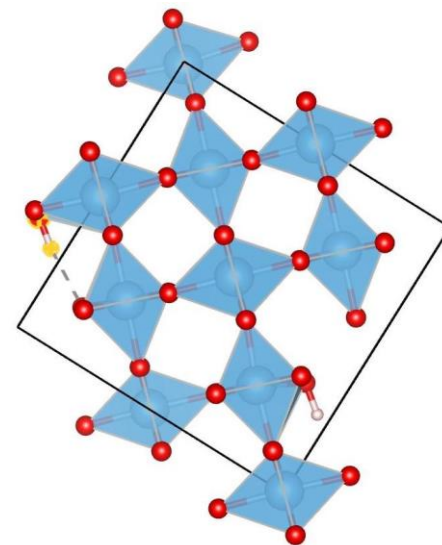
- **Identified 3 clusters**
- **Use k-means clustering**
- **Identified the  $Mu_T$  and  $M_{BC}$  in Silicon.**
- **High throughput method.**



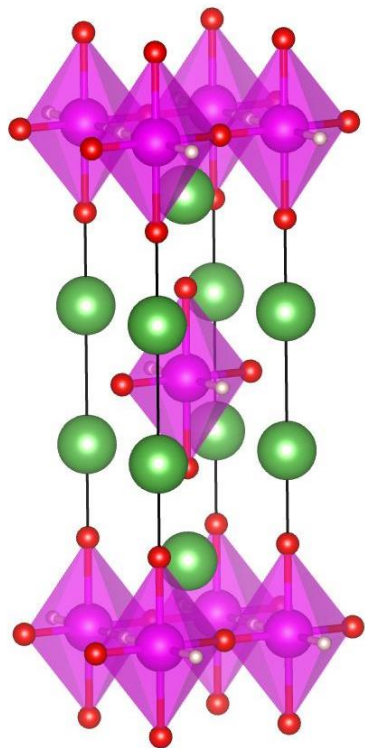
**LiF**



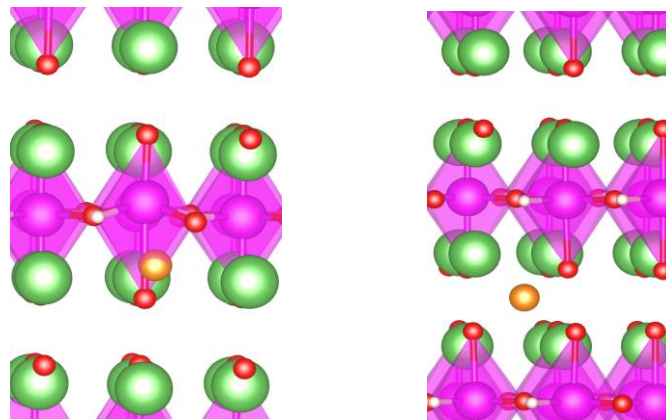
**Diamond**



**TiO<sub>2</sub>- rutile**



**La<sub>2</sub>LiHO<sub>3</sub>**



Site 1

Site 2

**High throughput method.**

Collaboration  
with University of  
Oslo, Norway  
and ISIS

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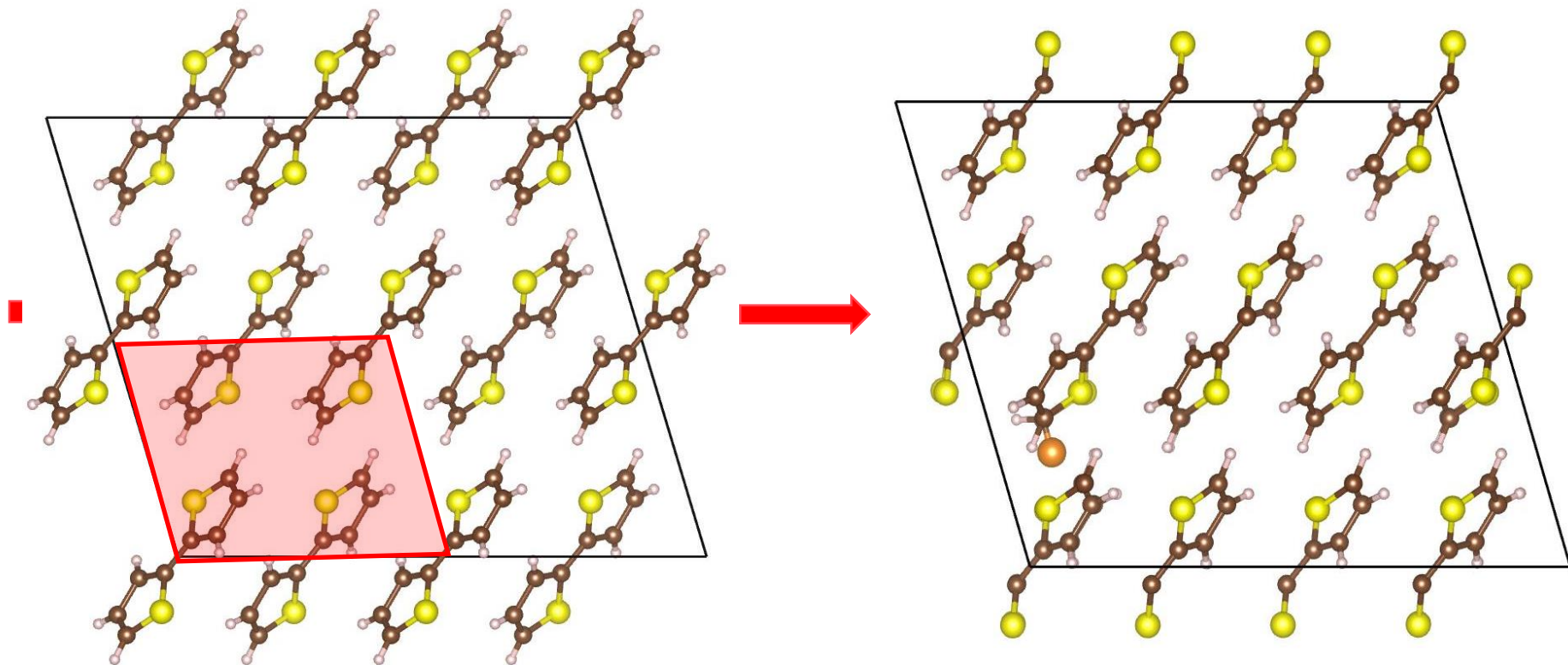
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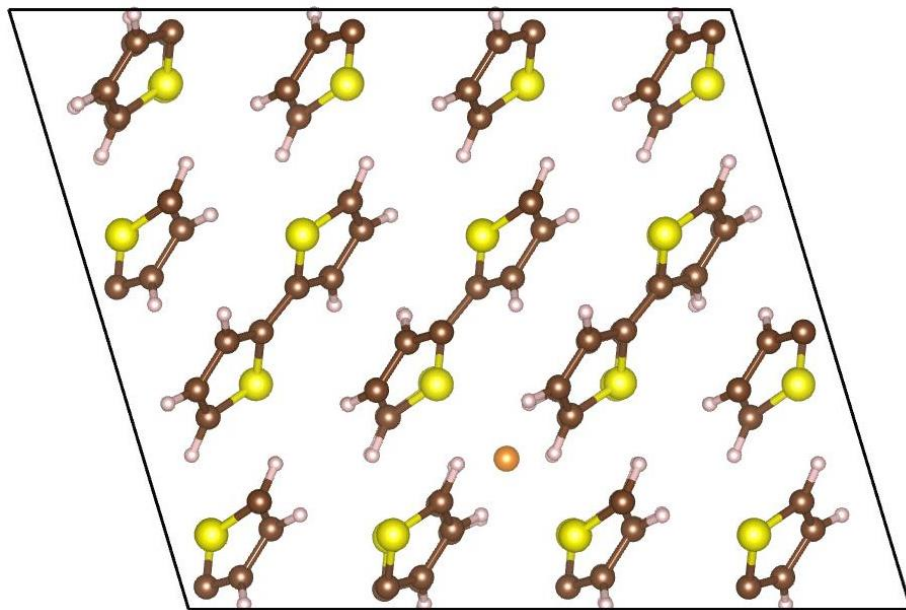
**Conclusions. Work in progress. Future plans.**

- 1) **Build 2x2x2 Bithiophene supercell**
- 2) **Define region to randomly locate muonium pseudo-atoms**
- 3) **Generate muonated structures placing muonium in randomised positions within the chosen region**
- 4) **Relax structures using calculated **DFTB+ forces**. **Reliable parameters for organic systems.****

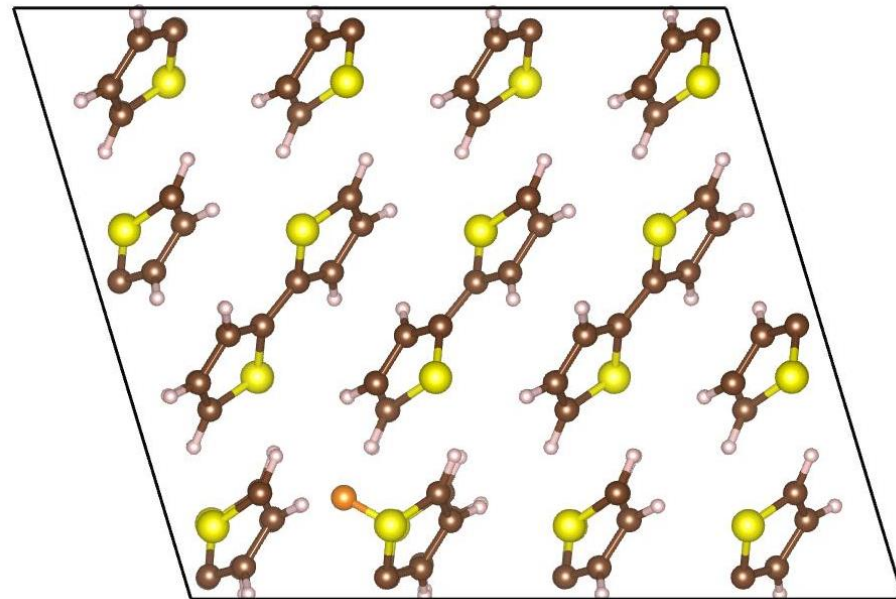


- 1) Divide the sites in 'floating' and 'bounded' sites
- 2) Reduce all muonated structures to asymmetric unit cell
- 3) Define  $nD$  vector:  $(E_T, x, y, z)$
- 4) Look for "closeness" in  $nD$  space
- 5) Hierarchical clustering
- 6) Found five stopping sites

Work done with  
Samuel Jackson



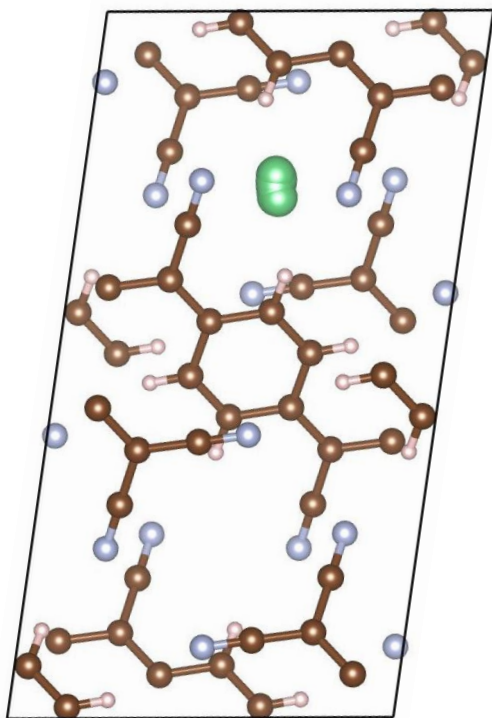
Floating site



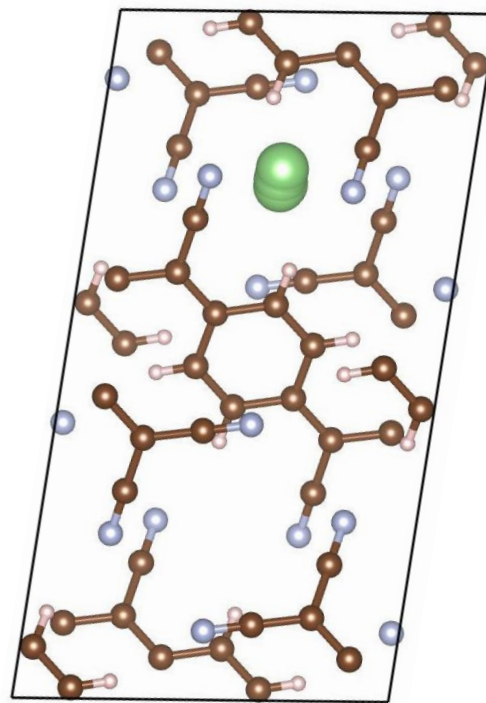
Bounded site

Sites in reasonable agreement with experiments (Except from the floating site)

- **Method at least two orders of magnitude faster than the one using standard DFT.**
- **Tested for bithiophene and benzene and finalizing tests for TCNQ.**
- **Only works in organic materials composed simple atoms (Br, C, Ca, Cl, F, H, I, K, Mg, N, Na, O, P, S, Zn)**
- **Are floating sites real?**



TCNQ CASTEP



TCNQ DFTB+

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- We are developing computational methods to **estimate the stopping sites of muons** in crystalline materials. These methods **complement** the known methodologies used for predicting the muon stopping sites. In fact, we have developed our own flavor of the UEP method. We are testing the UEP method with a set of materials
- Our methods utilize **DFT and DFTB+ calculations**, combined with the **random generation** of potential muonated structures and the use of **machine learning techniques** to efficiently search for clusters in these structures.
- The **Python library Soprano** is used to implement the method and identify the clusters
- Our methods **predicted** muon stopping sites in Si, Ge, Diamond, LiF, TiO<sub>2</sub>, La<sub>2</sub>LiHO<sub>3</sub>, Bithiophene, Bencene and TCNQ.
- Extend the method to other DFT codes.
- Working on the implementation of these techniques for a general user.
- Will work on computational tools for interpreting quadrupolar level crossing resonance (QLCR) results in muSR (Beamtime requested for experiments).
- Will work on quantum tunnelling of muonium via radical states in molecular solids (Beamtime requested for experiments).
- The problem of quantum effects.



**JOCHYM**



**STURNIOLO**



**LIBORIO**



**PRATT**



**JACKSON**



**DACK**



**COTTRELL**